

*Two-phase flow model for energetic proton  
beam induced pressure waves in mercury target  
systems in the planned European Spallation  
Source*

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Budapest*



# Outline

- *Motivation*

*spallation, some aspects of neutron physics, general remarks, cavitation*

- *The idea of a thermo-hydraulical model,*

*gentle introduction into shock-waves (ideal gas)*

*general thermo-hydraulics for water*

*Equation of states for Hg, proton – Hg interaction*

*some new results*

- *Summary and Outlook*

## *Informations:*

**ESS General:** <http://neutron.neutron-eu.net/>

**ISIS (UK):** <http://www.isis.rl.ac.uk>

**SNS (USA):** <http://neutrons.ornl.gov/>

**JPARC (Japan):** <http://j-parc.jp/index-e.html/>

**3rd High-Power Targetry Workshop**

**September 10 – 14, 2007, Bad Zurzach, Switzerland**

**organized by the Paul Scherrer Institut, Villigen PSI**

<http://asq.web.psi.ch/hptrgts>

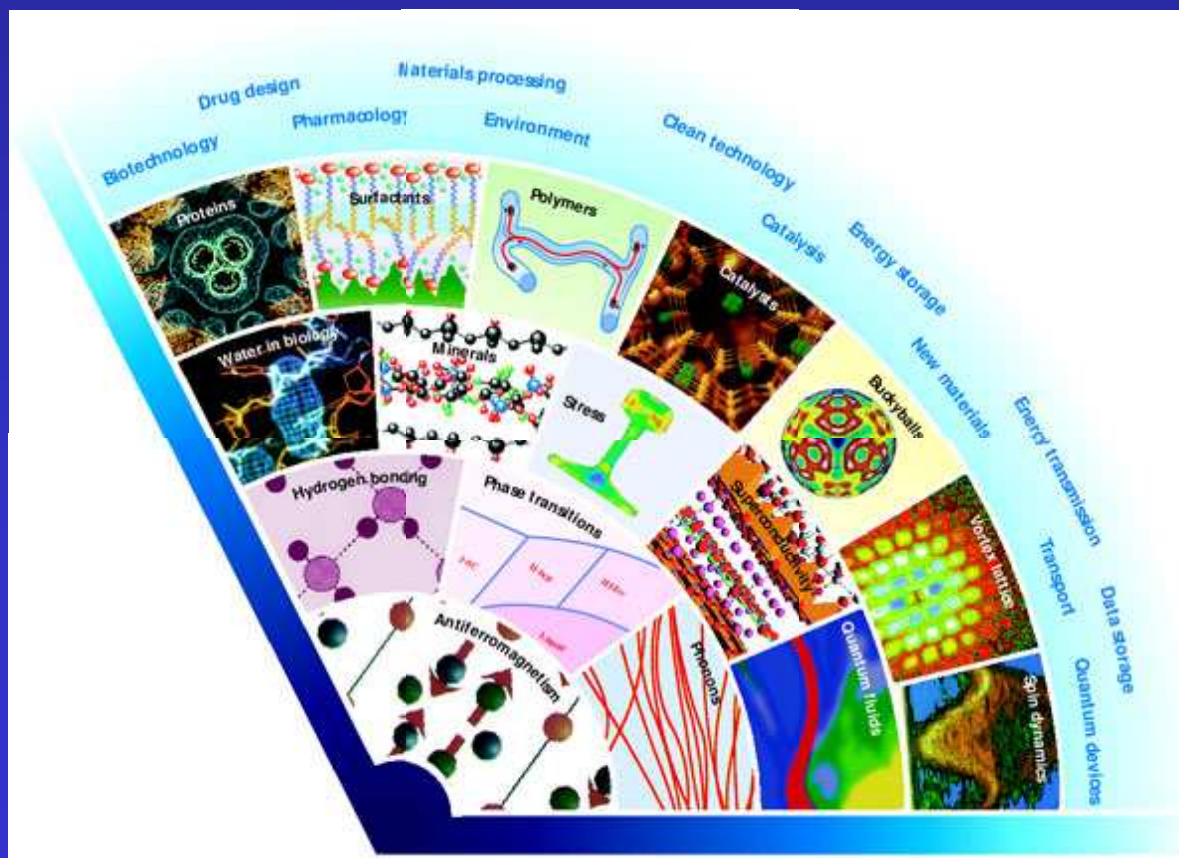
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(from where some slides/data of the following talk were borrowed)

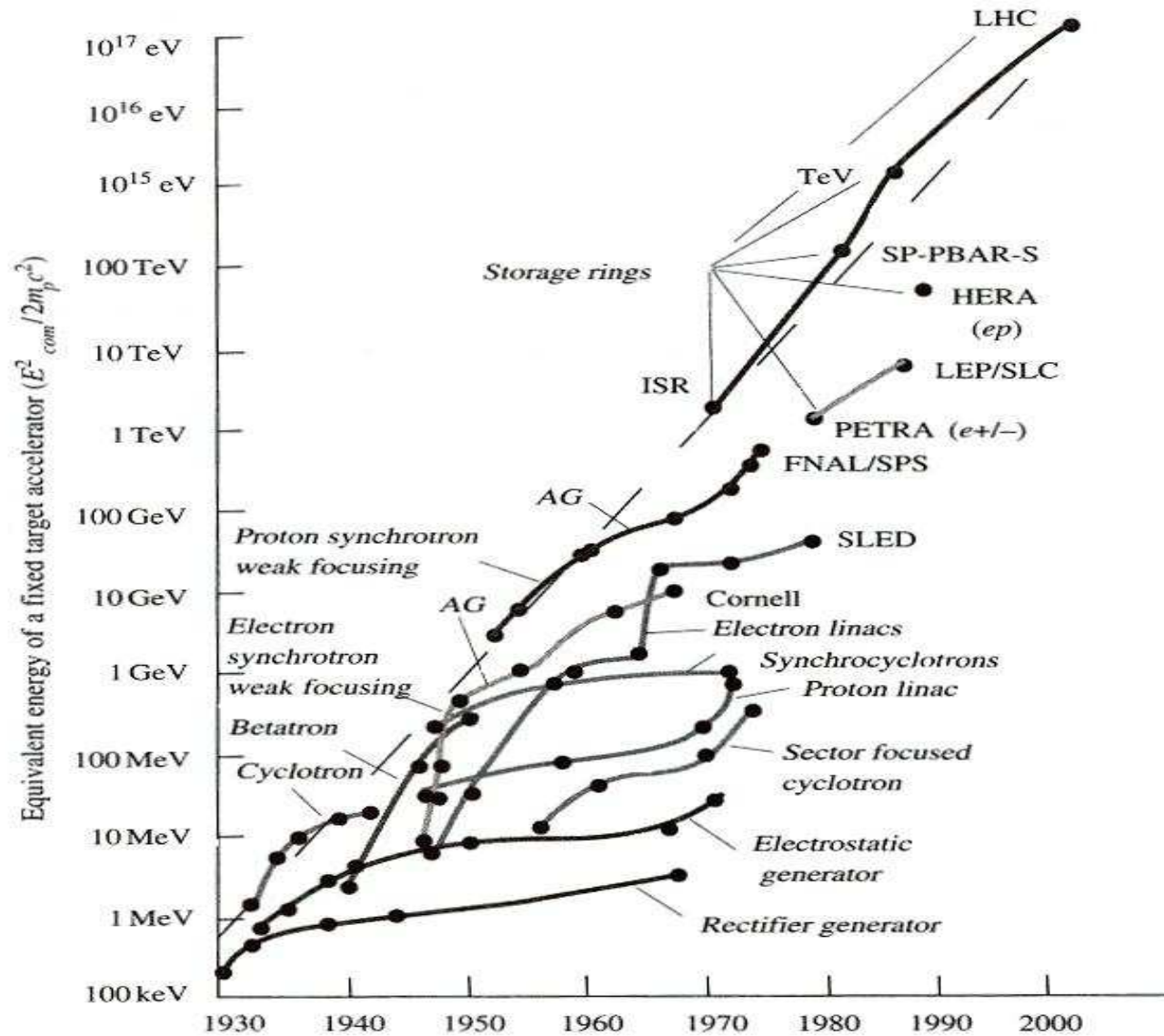
# Motivation I

*Low energy neutrons scattering is one fundamental material research method without destruction (beyond X-ray, and electron scattering)*

*neutrons are enable the structure and dynamics of condensed matter to be probed on a microscopic scale ranging from the subatomic to the macromolecular*



# Motivation II



*the produced heat limits the maximal neutron flux in fission sources*



# Motivation III

Relative large european neutron  
Scientific community

Price 0.9 - 1.3 billion (10E9) Euro

3 Countries are candidating  
Spain (Bilbao)

Sweden (Lund)

Hungary (Debrecen)

Hungary is responsible for  
Thermo-hydraulic, radiation-  
protection and environmental Studies

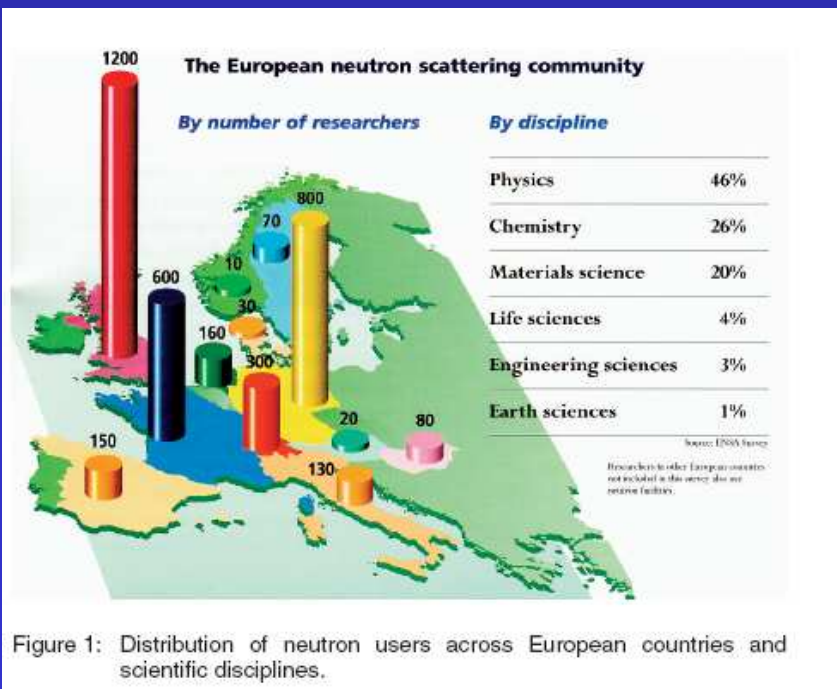
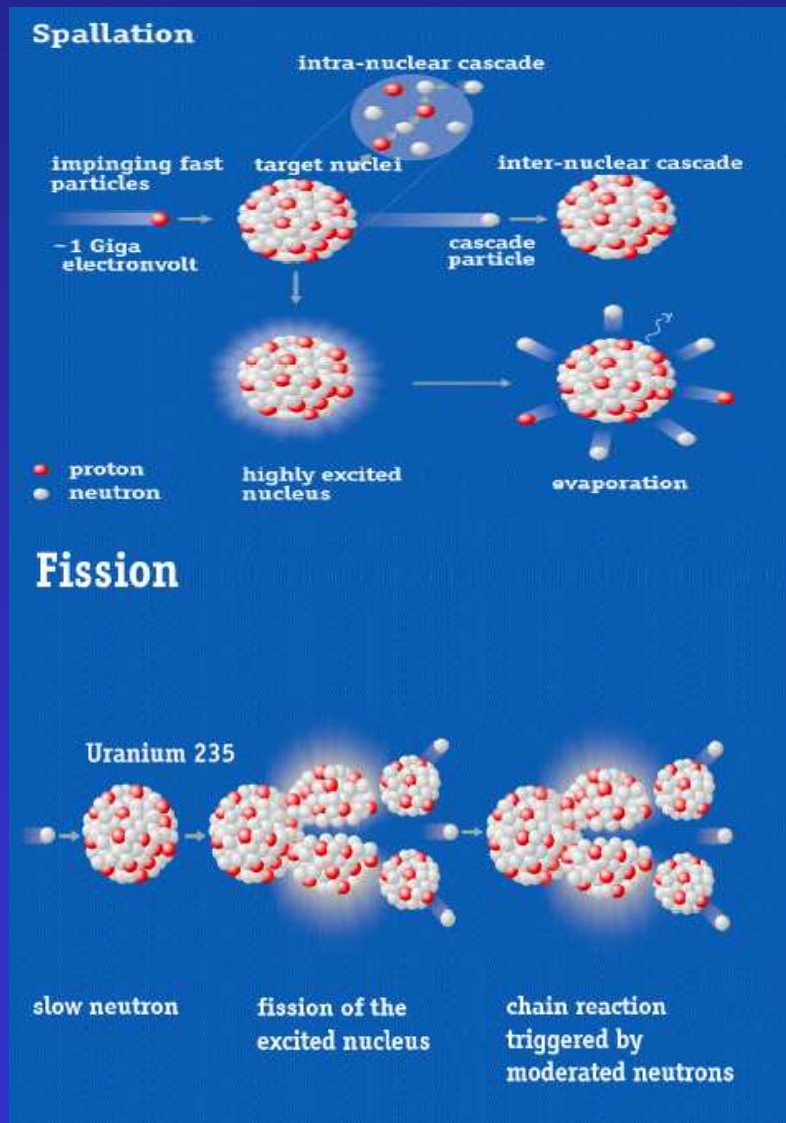


Figure 1: Distribution of neutron users across European countries and scientific disciplines.



# The Spallation process



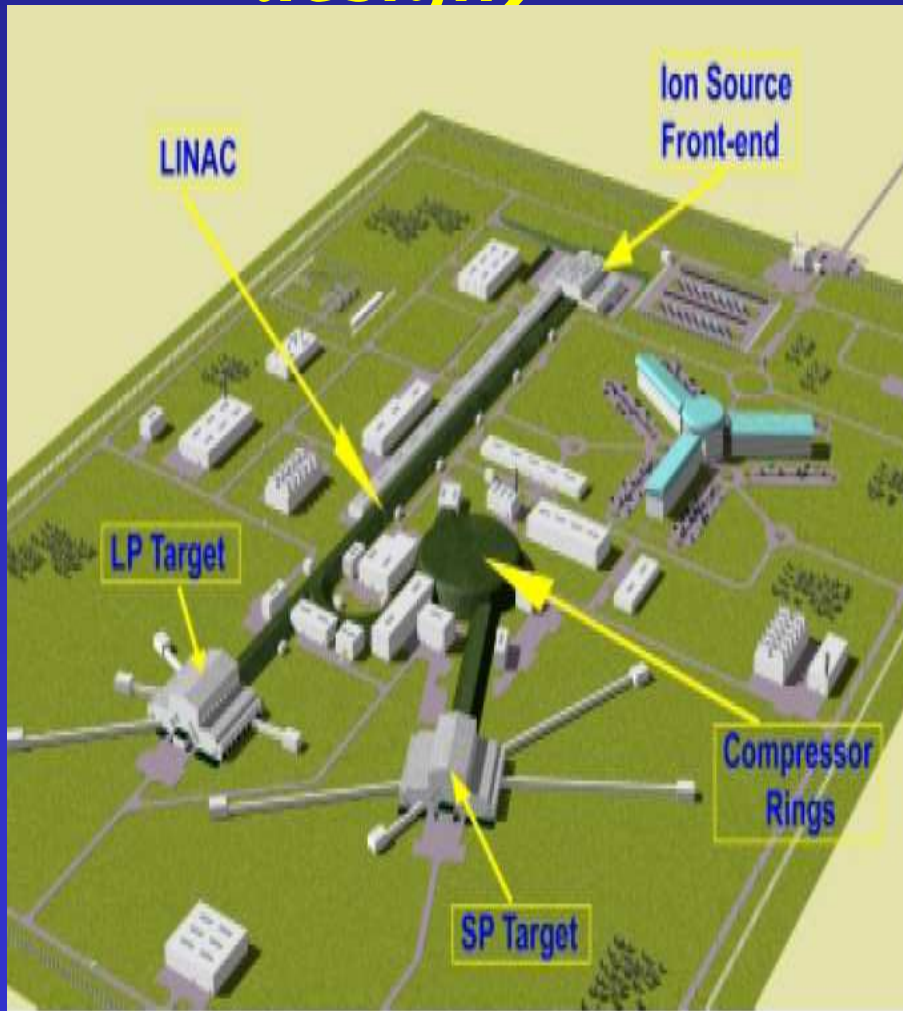
*It is a two step nuclear process, produces about 10 neutrons (and lot more, eg. mesons) without chain-reaction*

*the spectrum of the produced neutrons are favourable than other sources*

*the intensity & shape & length*

*of the neuron pulses are also fortunate*

# A general spallation source (SNS, JSNS, ISIS, former ESS design)

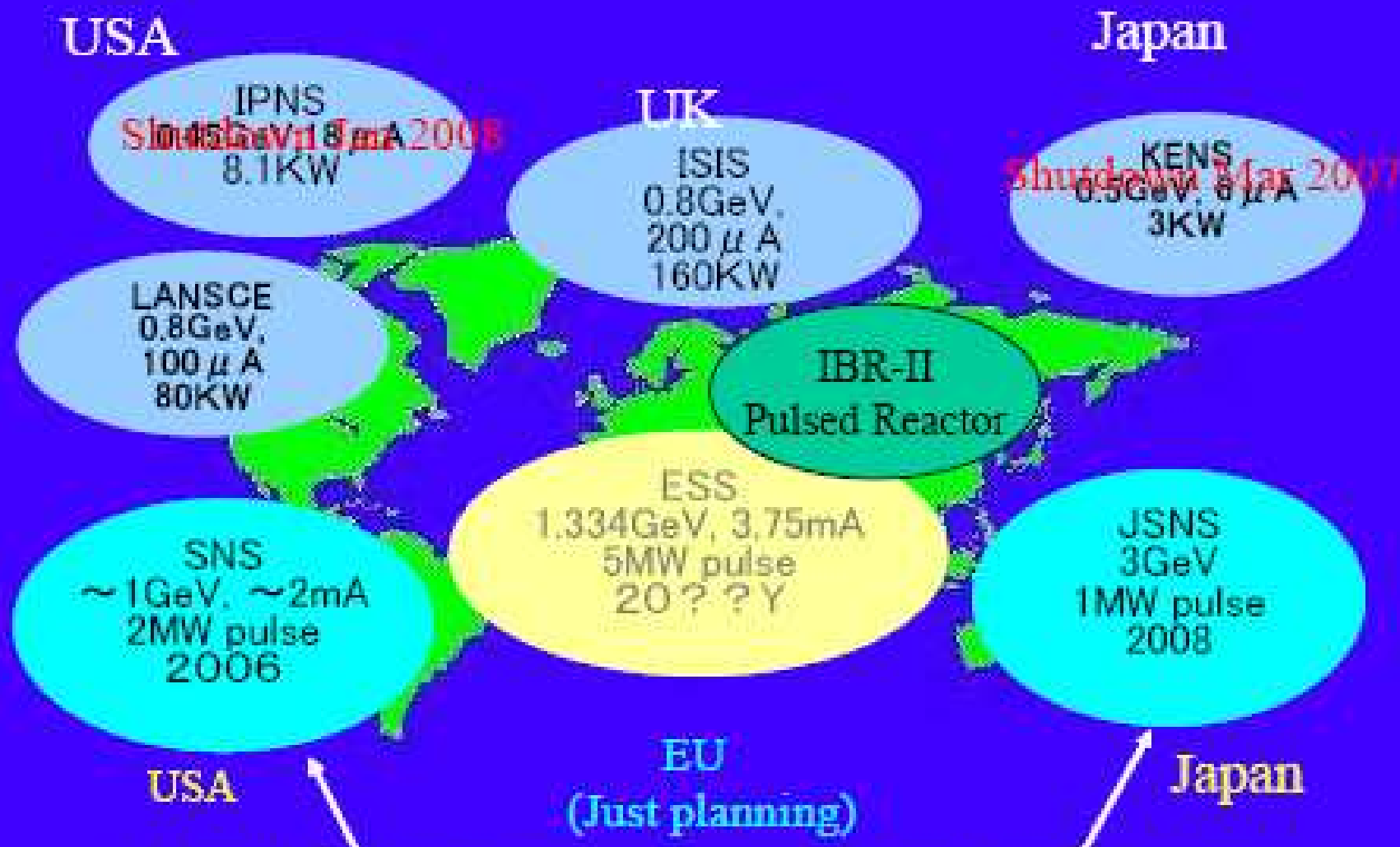


**Table 1.1-1:** Long and short pulses within the acceleration system

	SP	LP	
PRF (pulses per second)	50	16 <sup>2</sup> / <sub>3</sub> ●	
Beam pulse half width, 1 ring (ms)	0.48	2.0 ●	
Beam duty factor	4.8%	3.3%	
Non-chopped beam current (mA)	114	114	
Chopping factor	70%	70%	100%
Final energy (MeV)	1334	1334 ●	
Peak beam power (MW)	107	107	152
Mean beam power (MW)	5.1	3.5	5.1 ●
Pulse gaps, ring separation (ms)	0.1		
<b>NC-Linac</b>			
Total linac length (m)	769	769 ●	
Peak RF power (nominal)(MW)	186	236 (100%)	
Wall plug RF power (30 % RF control included) (MW)	34	24	
<b>SC-Linac</b>			
Total linac length (m)	432	432	
Peak RF power (nominal)(MW)	121	167 (100 %)	
Wall plug RF power (30 % RF control included)(MW)	20	15	
Cryo power(MW)	1.5	1.5	



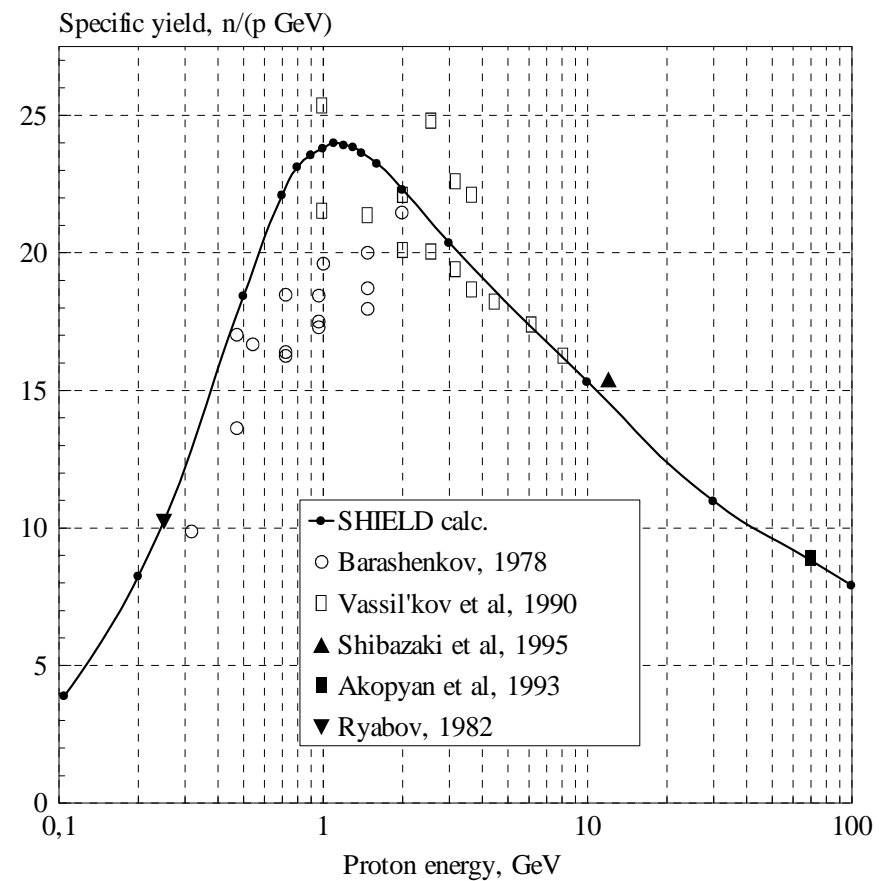
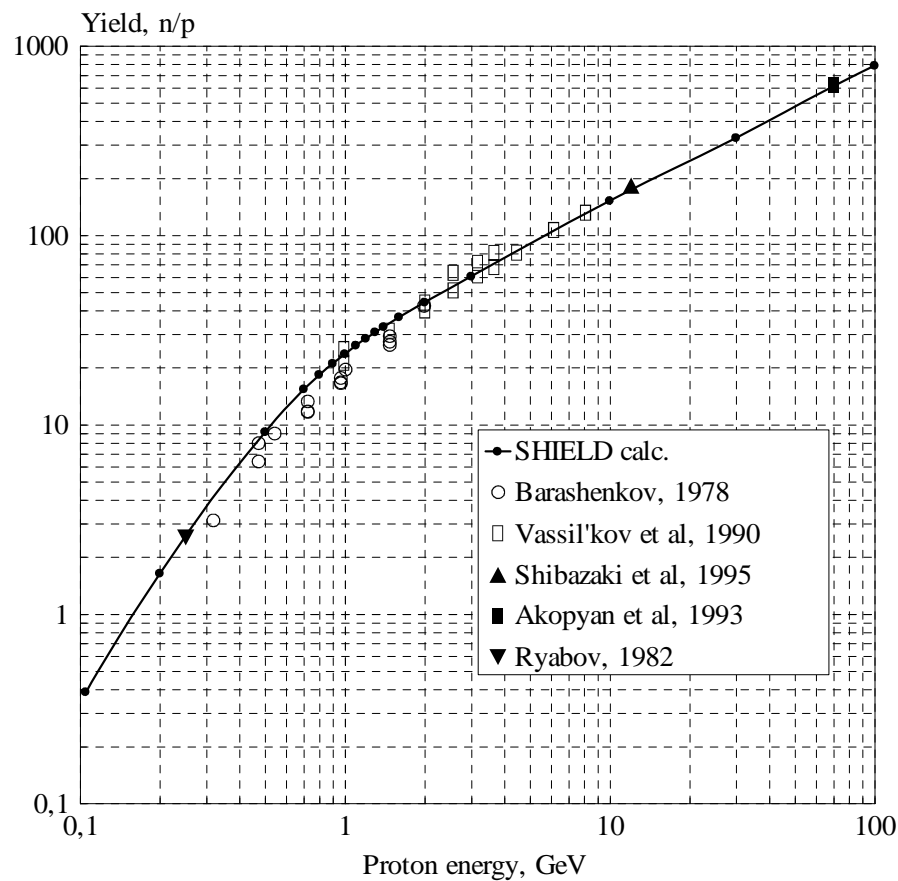
# Pulsed neutron sources in the world



New big neutron sources are all spallation sources.

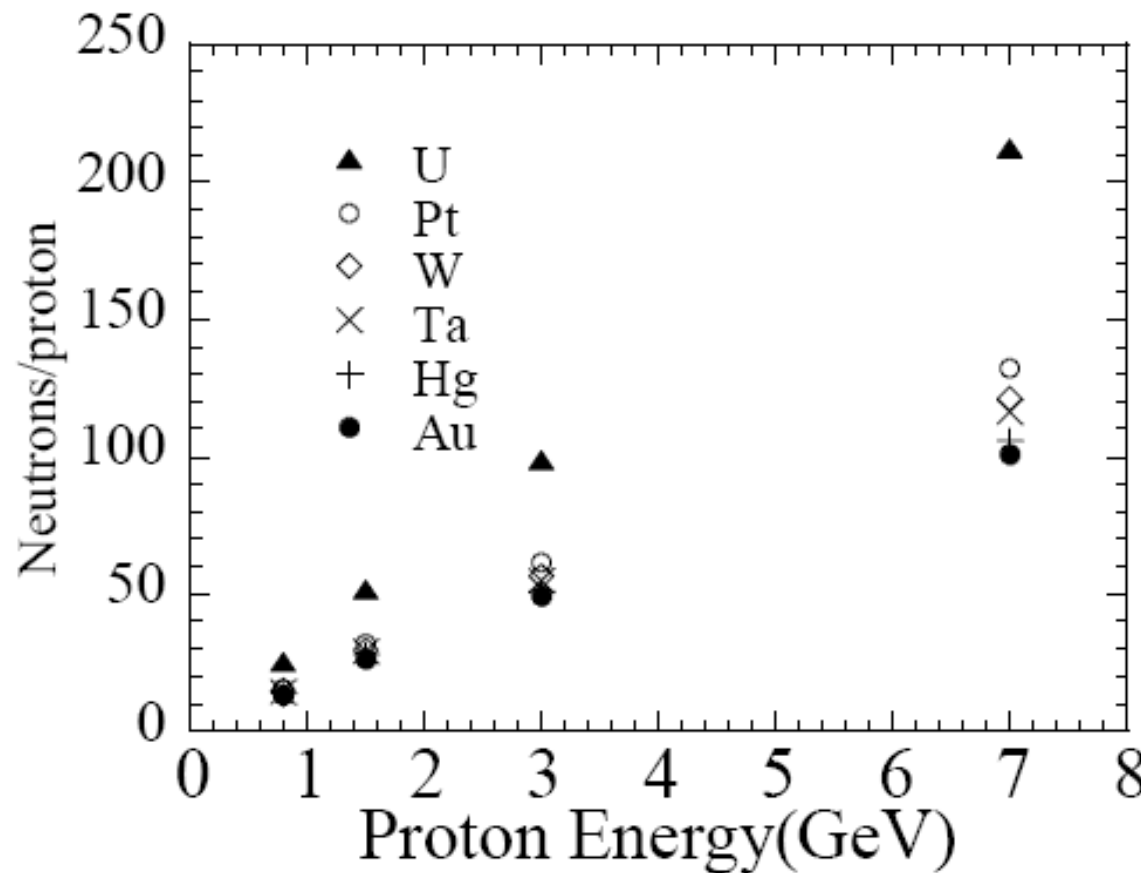
# Total and specific proton- neutron yield for a 20 cm geometry answer why

1.3 GeV



# Target materials

Neutron yield vs. proton energy



Neutron yield is not so different in heavy materials other than U producing fission neutron.

We have chosen Hg due to the reason that Hg can be used at higher power than 1 MW.

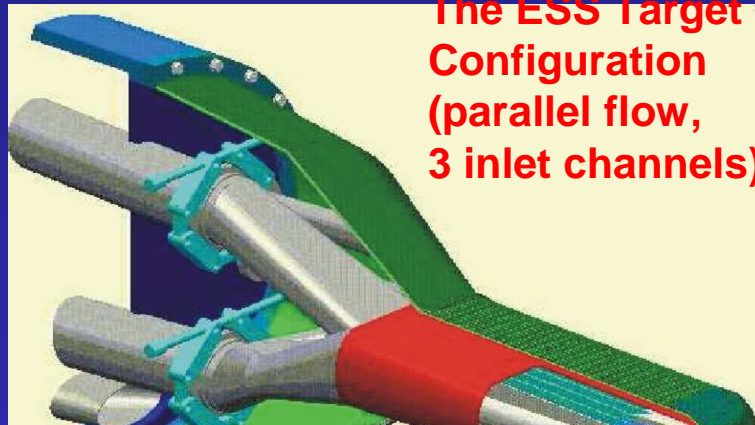
# Target Concepts

(I will show all of them)

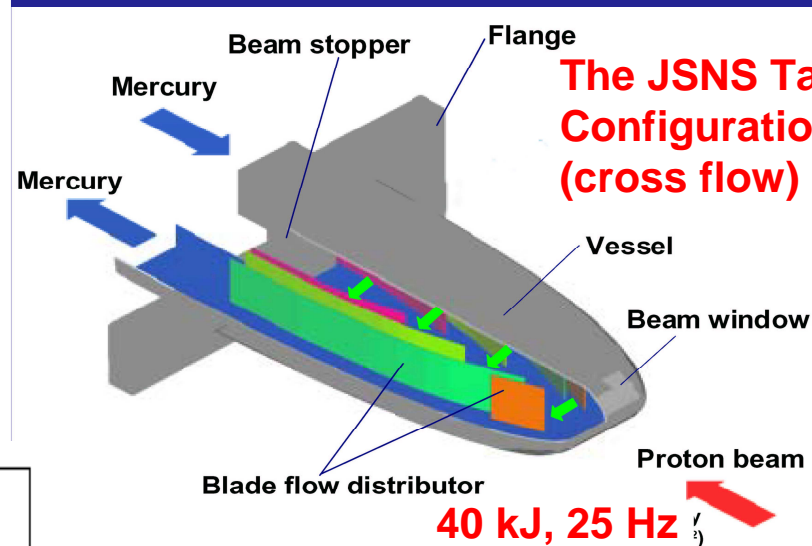
- Solid Rotating(tested in Jülich, never worked)  
Fixed(ISIS, UK)
- Liquid Hg(SNS, JSNS, ESS??)  
Lead-Bismuth Eutectic(SINQ in PSI)  
Major Problems, Shock-Waves, Cavitation Damages,  
Leakage, unknown life expectancy  
Solutions: target wall hardening, non-condensable  
gas injection

ESS target is still in question but Hg is the favorite

# The ESS-SNS-JSNS Hg Target Concepts



**The ESS Target Configuration (parallel flow, 3 inlet channels)**

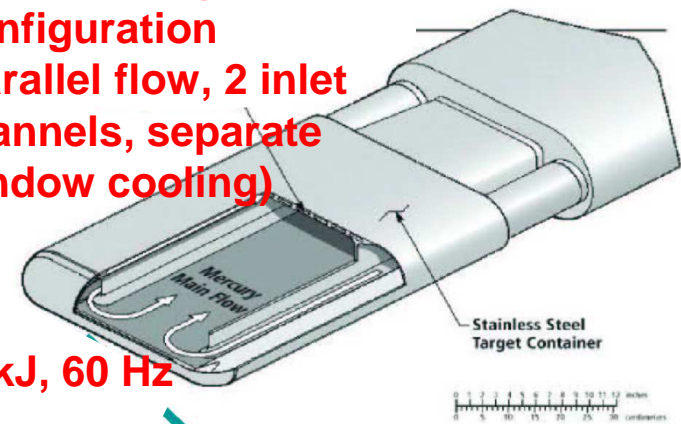


**The JSNS Target Configuration (cross flow)**

**40 kJ, 25 Hz**

	SP Short Pulse	LP Long Pulse
Two target stations		
Beam power	5 MW	5 MW
Energy of protons	1.334 GeV	1.334 GeV
Time structure of proton pulse	2 x 0.6 $\mu$ s	2.0 ms
Energy content of proton pulses	100 kJ	300 kJ
Repetition rate	50 Hz	16 <sup>2</sup> / <sub>3</sub> Hz
Proton beam diameter at target (parabolic 2D-density distribution)	6 x 20 cm <sup>2</sup>	6 x 20 cm <sup>2</sup>
Target type	Flowing mercury horizontal injection	Flowing mercury horizontal injection
Number of moderators (viewed faces)	2 (4)	2 (4)
Average thermal flux	3.1 x 10 <sup>14</sup> n/cm <sup>2</sup> s	3.1 x 10 <sup>14</sup> n/cm <sup>2</sup> s
Peak thermal neutron flux	1.3 x 10 <sup>17</sup> n/cm <sup>2</sup> s	1.0 x 10 <sup>16</sup> n/cm <sup>2</sup> s
Decay time of flux	150 $\mu$ s	150 $\mu$ s

**The SNS Target Configuration (parallel flow, 2 inlet channels, separate window cooling)**

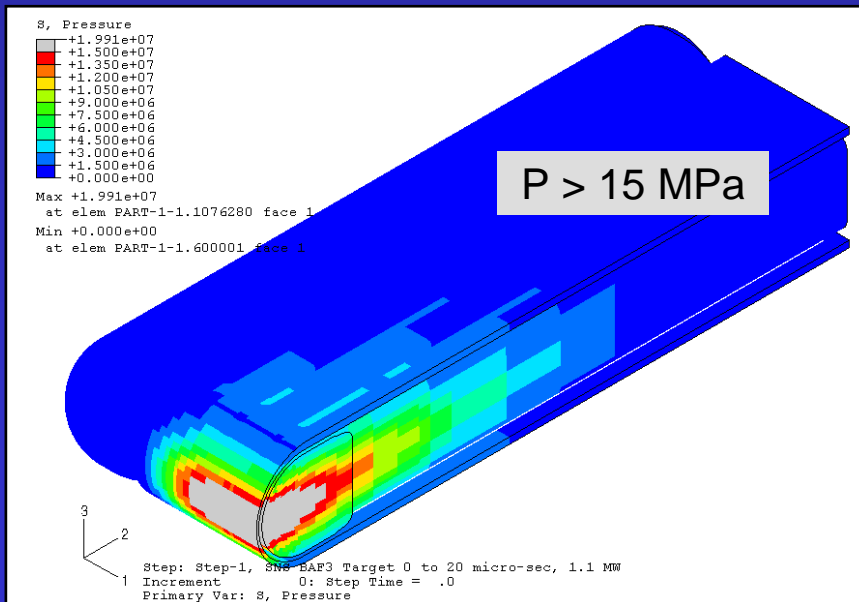


**33 kJ, 60 Hz**

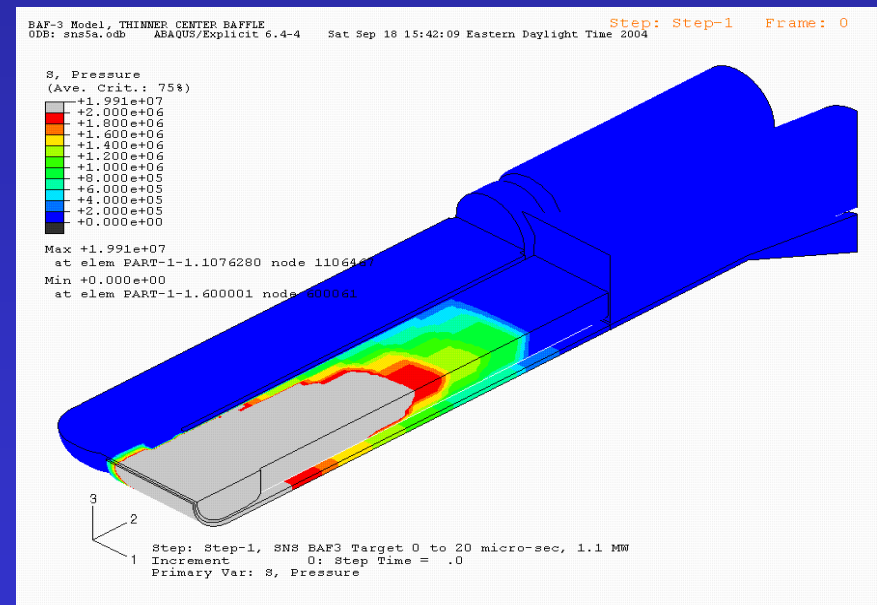


# Simulation techniques applied to SNS mercury target

Detailed stress and temperature analysis with ANSYS FINE  
Even two-phase flow thermohydraulical simulations,  
forecasting large degree of cavitation WELL WELL...



Mercury pressure right after beam pulse  
( $P_{max} = 19.9 \text{ MPa}$  @ 1.1 MW)

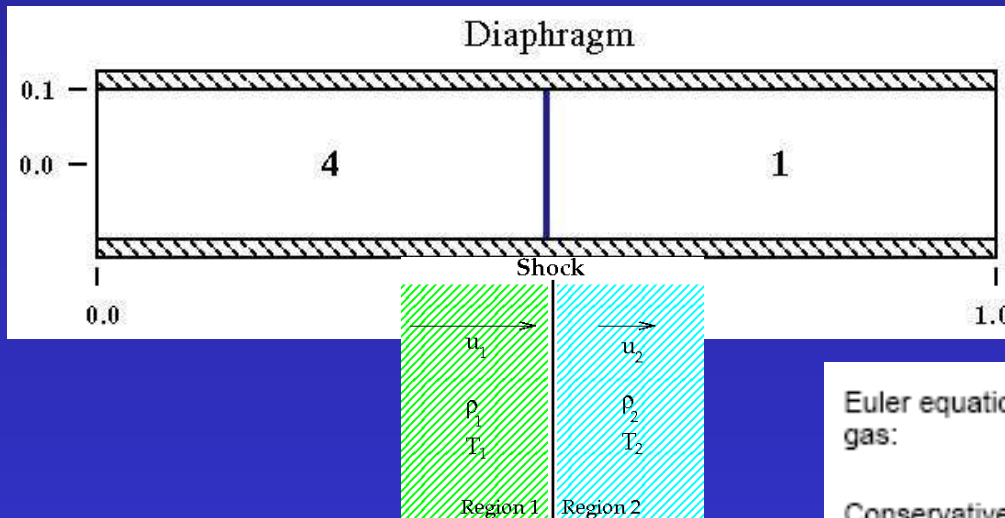


Stress at time of maximum stress  
( $S_{max} = 176 \text{ MPa}$  @ 0.114 ms)

# Gentle introduction on shock

## waves, two-phase flow

Def: a surface of discontinuity propagating in a gas at which density and velocity experience abrupt changes  
 → we call it a shock wave (Zemplén Győző 1905)



basic experimental setup  
 (shock tube)

mathematical description:  
 conservation laws,  
 continuity, momentum(Euler)  
 energy equation + Equation of state

Euler equations of single-phase compressible quasi-1D flow of ideal gas:

Conservative form

$$\begin{bmatrix} A\rho \\ A\rho v \\ AE \end{bmatrix}_t + \begin{bmatrix} A\rho v \\ A(\rho v^2 + p) \\ Av(E + p) \end{bmatrix}_x = \begin{bmatrix} 0 \\ p \\ 0 \end{bmatrix} \frac{dA}{dx}$$

Non-conservative vectorial form:  $\frac{\partial \vec{\psi}}{\partial t} + \underline{C} \frac{\partial \vec{\psi}}{\partial x} = \vec{S}$

Conservative variables are used in vector

$$\vec{\psi} = [A\rho, A\rho v, A\rho e] \quad \left( E = \rho e = \rho u + \frac{1}{2} \rho v^2 \right)$$

Equation of state (ideal gas):  $E = \frac{p}{\gamma - 1} + \frac{1}{2} \rho v^2 \quad \gamma = \frac{c_p}{c_v}$

# Gentle introduction on shock waves, two-phase flow

the measurable physical quantities change in time non-continuously, (non-continuous solutions for partial differential equations)

in a real shock wave physical quantities grow up in approx. 2-4 free mean path of a particle

( $10^{-2}$  mm at normal  $p$ ,  $T$ , quick phenomena no time for diffusion, heat exchange)

the given equations have different wave solutions with different wave propagation velocities

Jacobian matrix:

$$\underline{C} = \begin{bmatrix} 0 & 1 & 0 \\ (\gamma-3)v^2/2 & (3-\gamma)v & \gamma-1 \\ (\gamma-1)v^3/2 - v\dot{h} & h - (\gamma-1)v^2 & \gamma v \end{bmatrix}$$

Diagonalized:

$$\underline{C} = \underline{L} \cdot \underline{\Lambda} \cdot \underline{L}^{-1} \quad \left( c^2 = \frac{\gamma p}{\rho} \right) \quad h = e + p/\rho$$

Eigenvalues:

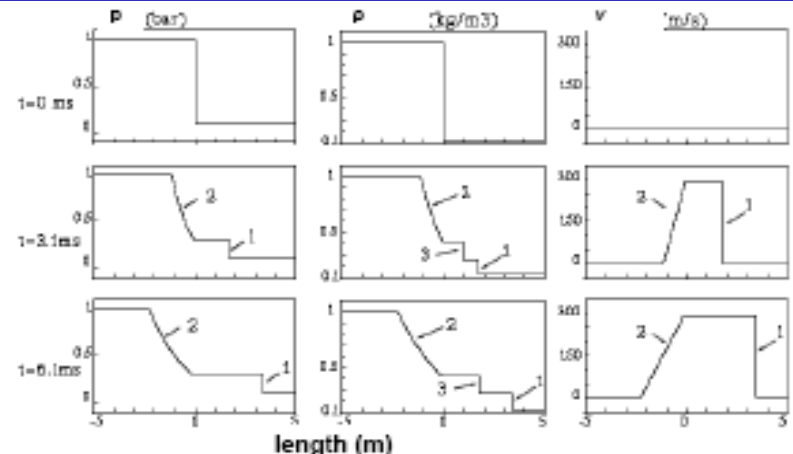
$$\underline{\Lambda} = \begin{bmatrix} v+c & 0 & 0 \\ 0 & v-c & 0 \\ 0 & 0 & v \end{bmatrix}$$

Eigenvectors

$$\underline{L} = \begin{bmatrix} 1 & 1 & 1 \\ v+c & v-c & v \\ h+cv & h-cv & v^2/2 \end{bmatrix}$$

characteristic-upwind schemes

8



1- shock wave, 2- rarefaction wave, 3 - contact discontinuity

# *Gentle introduction on shock waves, two-phase flow*

*Shock wave in shock tube for ideal gas:*

*(movies)*

*density wave* *run\_rhot.bat*

*pressure wave* *run\_p.bat*

*speed wave* *run\_v.bat*

# *The main problem with shock waves, at high-temperature & high-speed hydrodynamics*

fine stuff

*Equation of motion: continuity + Euler + energy*

*Equation of state, (any kind) comes from classical thermodynamics, assume thermal equilibrium e.g. Van der Waals EOS*

Not valid!

*„Generalized Thermodynamics” (1958) DeGroot*

*„If the temperature gradient is larger than 1000 K/cm usual thermodynamics does not work”*

*there is no definition **even** for temperature & pressure for non-equilibrium thermodynamical system*

*way out → microscopic theory, local equilibrium in small cells...*



# Gentle introduction on shock waves, two-phase flow

- 1D single phase flow can be generalised for 2 phases,  $\longrightarrow$  averaging over the volume (void fraction,  $\alpha$ )

- Different models, with different number of equ.s from 3 up to 7 equation models are available, with different physical backgrounds

$$\frac{\partial \vec{\psi}}{\partial t} + \underline{\underline{C}} \frac{\partial \vec{\psi}}{\partial x} = \vec{S}$$

$$\vec{\psi} = (\rho_m, v_m, p_m)$$

$$\vec{\psi} = (\rho_m, \rho_g, \rho_m v_m, \rho_m u_m)$$

$$\vec{\psi} = (\rho_g, \rho_f, \rho_m v_m, \rho_f u_f, \rho_g u_g)$$

$$\vec{\psi} = (\rho_g, \rho_f, \rho_g v_g, \rho_f v_f, \rho_g u_g, \rho_f u_f)$$

$$\vec{\psi} = (\rho_g, \rho_f, \rho_g v_g, \rho_f v_f, \rho_g u_g, \rho_f u_f, 7^{th} \text{ variable}) \text{ could be a two pressure model}$$

mixture density, velocity, energy is defined

we use this one, well tested, single pressure for both phase phases

# *The numerical scheme of WAHA(our physical model)*

$$\frac{\partial \vec{\psi}}{\partial t} + \underline{C} \frac{\partial \vec{\psi}}{\partial x} = \vec{S}$$

$$\vec{\psi} = ( p, \alpha, v_f, v_g, u_f, u_g )$$

*6 coupled first order partial differential equations,  
no second-order derivatives,  
non-conservative variables*

*High resolution, non-dispersive shock capturing  
first order explicit finite difference schema with  
second order corrections*

R. Saurel, R. Abgrall, A Multiphase Godunov method for compressible multfluid and multiphase flows, *J. Comp. Physics* **150**, 425-467, 1999.

I. Tiselj, S. Petelin, Modelling of two-phase flow with second-order accurate scheme, *J. Comp. Physics* **136** (2) 503-521, 1997.

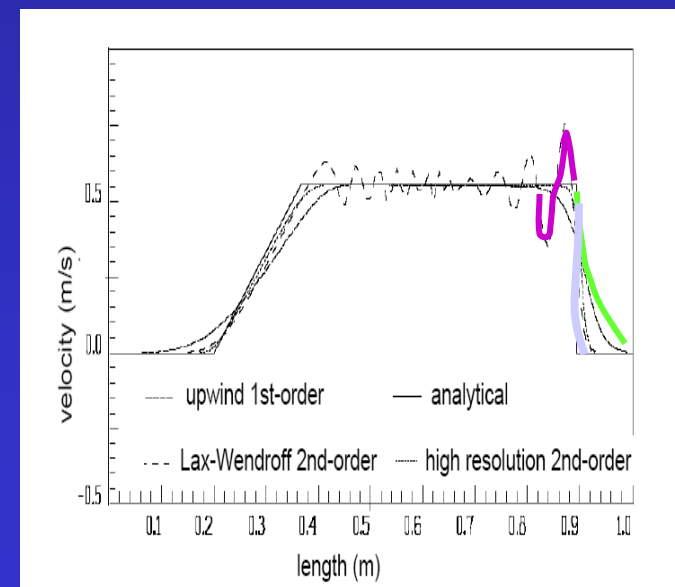
# Idea of the numerical method

- *Hyperbolic partial dif. equ. systems* → *non-continuous solutions*
- 
- *(jump initial condition is conserved in time)*
- *Special numerical method is needed*

$$\frac{\partial \vec{\psi}}{\partial t} + \underline{C} \frac{\partial \vec{\psi}}{\partial x} = \vec{S}$$

*(example: ideal gas shock wave)*

- *Pure 1st order method smears discontinuity*
- *Pure 2nd order creates unphysical oscillations*
- *Mixed method gives physically correct answer (flux limiters)*



# Flow maps, correlations

two-phase flows have very complex flow maps

→ these are the main uncertainties in the theory

*we use simplified flow maps*

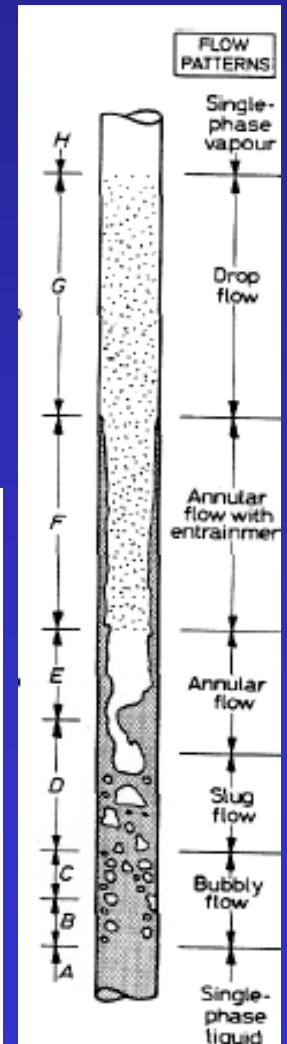
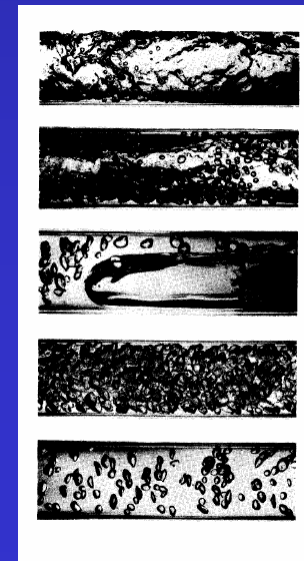
*stratified, bubbly, droplet flow with different correlations*

*Heat-mass, energy, impulse transfer  
between phases*

*Wall friction steady state/dynamical*

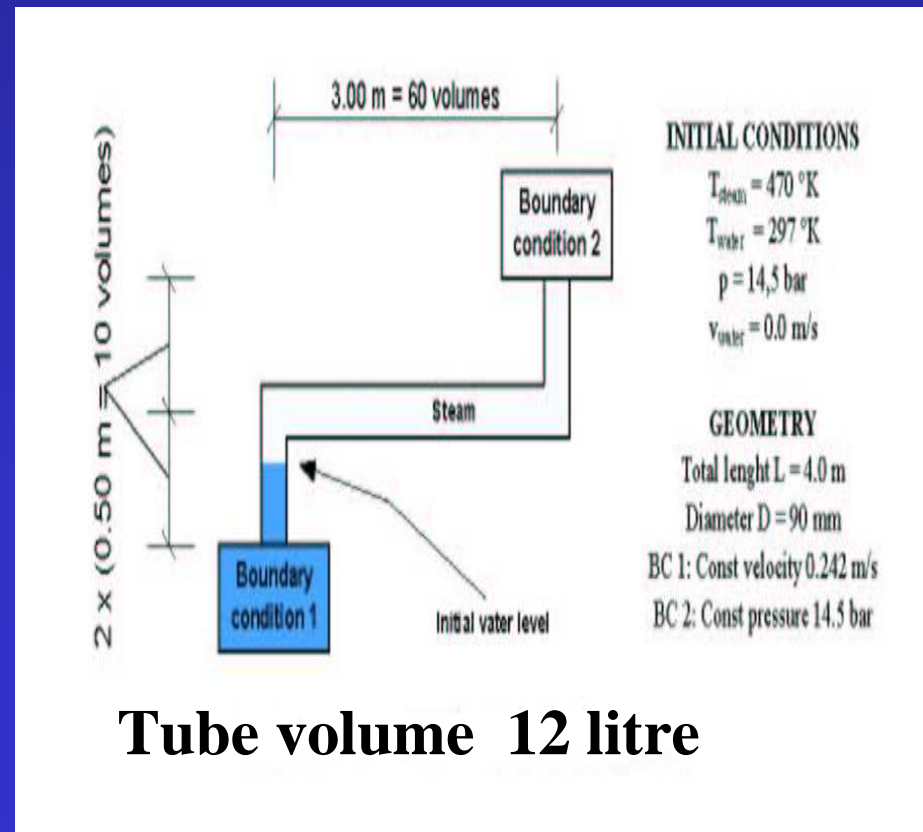
*Interphase friction*

*All can be switched on/off for different regimes  
For steam induced water hammer all correlations  
are needed*



# Our former aim/experience with WAHA

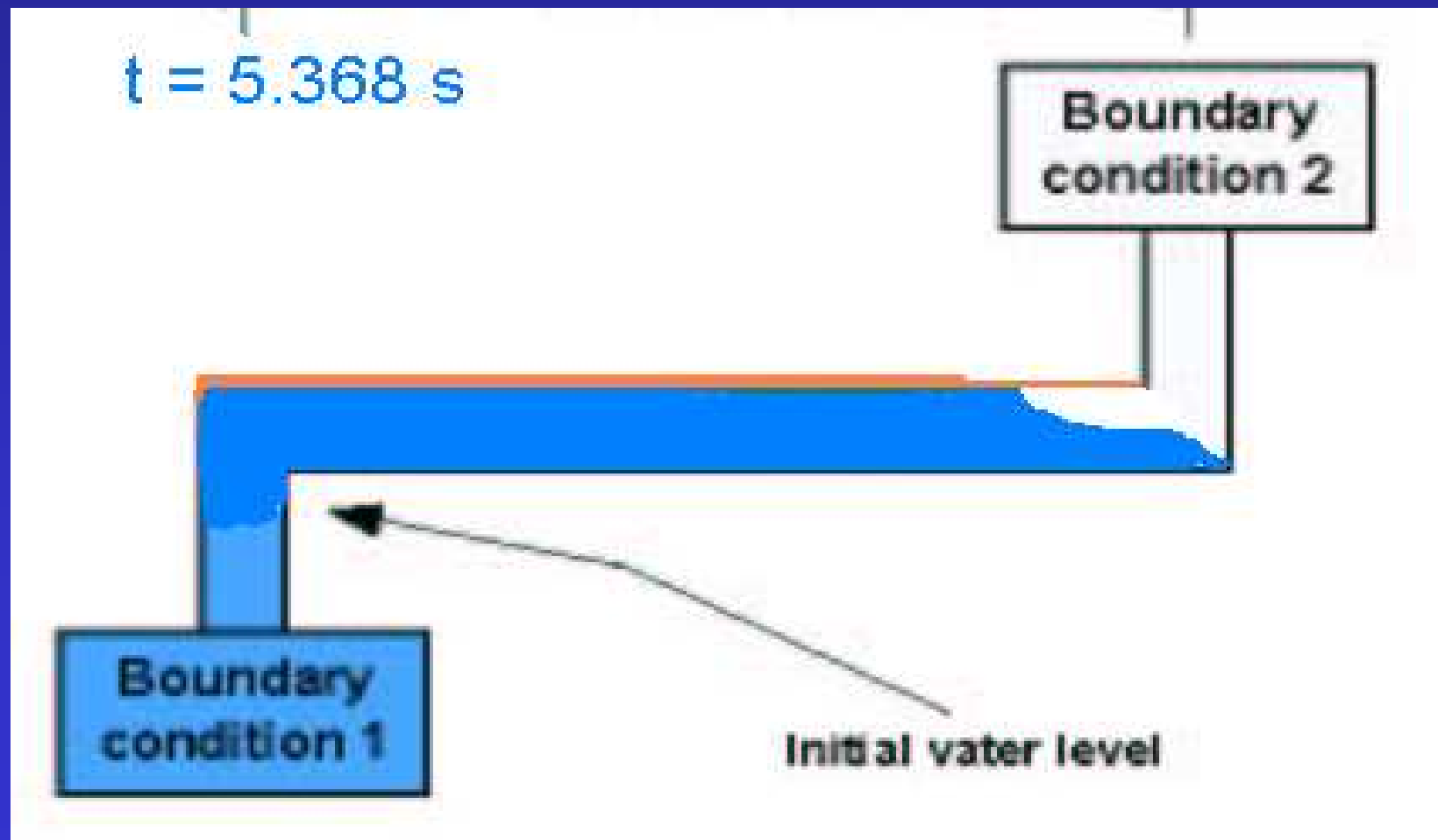
*study of the steam condensation induced water hammer phenomena,  
the most complex two-phase flow phenomena  
(experimental setup and the model scheme in numerical simulation)*





# *A possible mechanism for steam condensation induced water hammer*

*(some figures)*



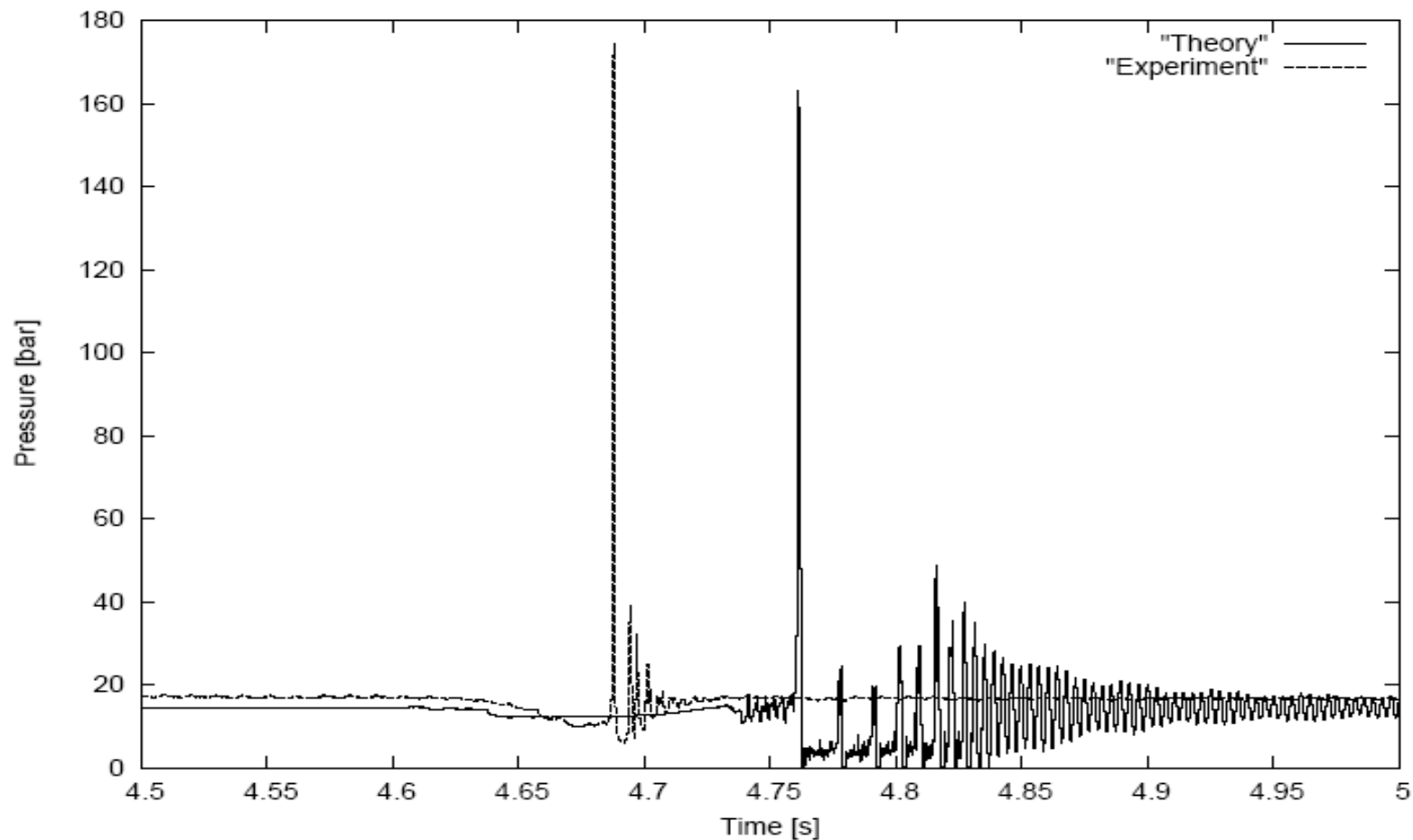
*A possible mechanism for  
steam condensation  
induced water  
hammer (animation)*

*The whole physical process: [kfki.avi](#)*

*a slow replay of the water hammer: [kfki\\_det.avi](#)*

# Analysis of the pressure peaks

(all the correlation / measurements)



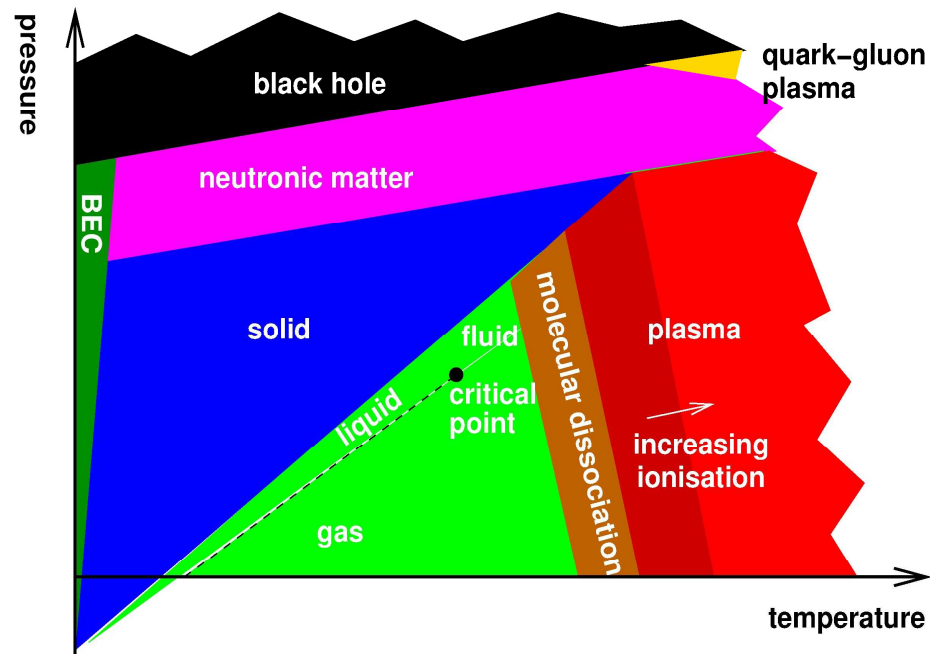
# *Idea, use the modified Bequ. model for proton - Hg interaction*

- *Basically two new points*
- *Not water but mercury (new & complete liquid- steam table), equation of state (EOS) (Subbotin correlation, surface tension, heat conduction, viscosity is known)*
- *Periodic driving from absorbed proton pulses, a new source term in both energy equations*

# How matter looks like

(On the way of an EOS for Hg)

Structure of the equation of state



Details depend on the material composition.

3 different type of EOS

$\rho(p, T)$  based on:

1) *microscopic, classical methods, particles in potential and/or quantum mechanical eg. density functional*

2) *mesoscopic calculations averaging of distribution functions*

3) *macroscopic, fenomenological,*

<http://public.lanl.gov/dswift>



# Different EOS for liquid-gas phase

$PV = nRT$  *ideal gas No phase transition 1834*

$$\left(P + \frac{a}{V^2}\right)(V - b) = RT \quad \text{Van der Waals 1873}$$

$$a = 3P_c \cdot V_c^2 \quad b = V_c/3.$$

• Berthelot

$$P = \frac{nRT}{V - nb} - \frac{n^2 a}{TV^2} = \frac{RT}{V_m - b} - \frac{a}{TV_m^2}$$

• Dieterici

$$P = \frac{nRT e^{-\frac{a}{RTV}}}{V - nb} = \frac{RT e^{-\frac{a}{RTV_m}}}{V_m - b}$$

• Redlich-Kwong

$$P = \frac{nRT}{V - nb} - \frac{n^2 a}{\sqrt{TV}(V - nb)} = \frac{RT}{V_m - b} - \frac{a}{\sqrt{TV_m}(V_m - b)}$$

$$\left(P + \frac{a(T)}{V(V + b)}\right)(V - b) = RT$$

*Soave-Redlich-Kwong 1972*

$$\left(P + \frac{a(T)}{V(V + b) + b(V - b)}\right)(V - b) = RT \quad \text{Peng-Robinson 1976}$$

$$\left(P + \frac{a(T)}{[V - b_1(T)][V - b_3]} - \frac{e}{[V - b_1(T)]^2[V - b_3]}\right)[V - b_1(T)] = RT$$

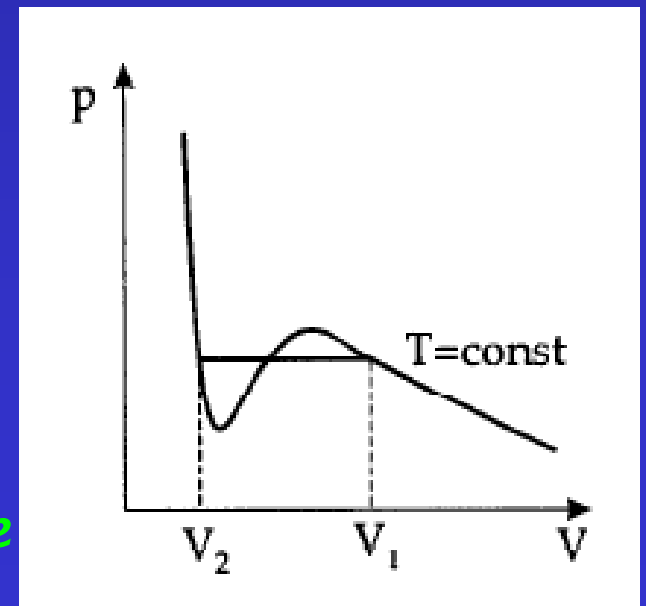
*Shell Research and Technology Center (cubic-4G) (oil industry)*

# How to create a steam table for Hg

For standard 2 phase-flow calculation a 6-fold table is needed:  
 $T$  (K),  $p$  (Pa),  $\rho_{\text{vap}}$  (kg/m<sup>3</sup>),  $u_{\text{vap}}$  (J/kg),  $\rho_{\text{liq}}$  (kg/m<sup>3</sup>),  $u_{\text{liq}}$  (J/kg)

from the EOS

the smallest and the largest real roots  
of the third order polinom at a given  $T$   
and  $P$  are proportional with the inverse of  
the liquid and steam densities,  
Maxwell construction for saturation pressure



# How to create a steam table for Hg

to calculate the internal energies is a bit more difficult

for liquid:  
just integrate

$$dU = C_V dT + \left[ T \left( \frac{\partial P}{\partial T} \right)_V - P \right] dV$$

additional experimental data (fitted function of)  
specific heat

$$C_p = C_v - T \left( \frac{\partial V}{\partial T} \right)_P^2 \left( \frac{\partial P}{\partial V} \right)_T$$

$$\alpha = \frac{1}{V} \left( \frac{\partial V}{\partial T} \right)$$

thermal expansion coefficients  
(fitting of experimental data)

for gas phase:  
just subtract  
vaporization enthalpy  
just fitting experimental data

6696 J. Chem. Phys., Vol. 119, No. 13, 1 October 2003

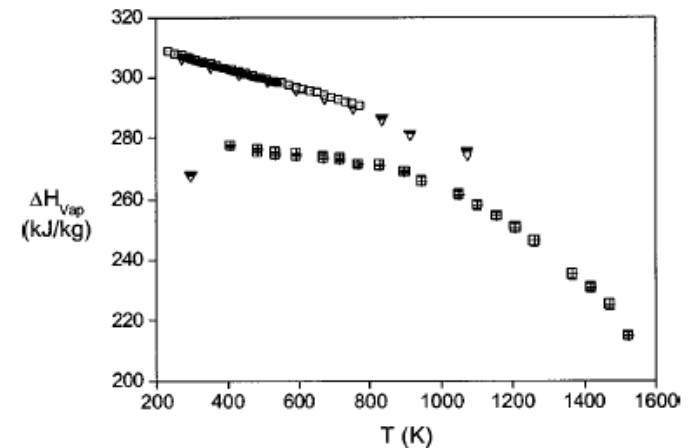
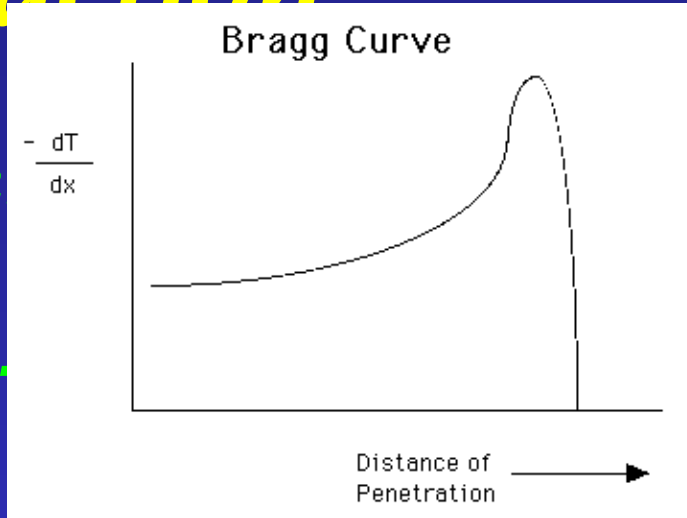


FIG. 6. Comparison of experimental heats of vaporization data (●—Ref. 26, half closed triangle—Ref. 27, □—Ref. 37) for mercury with molecular simulation data (⊞) obtained in this work by using Eq. (5).

This can be solved by Maple package ☺

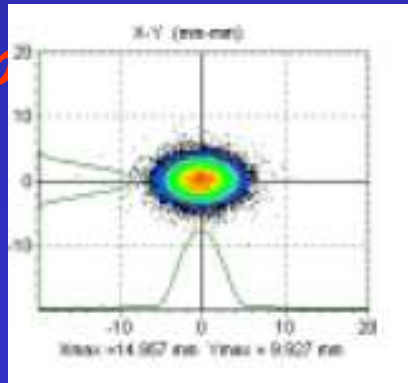
# Proton beam-Hg target interaction

- Accurate energy loss in Hg can be simulated with FLUKA, MARS, GEANT etc.



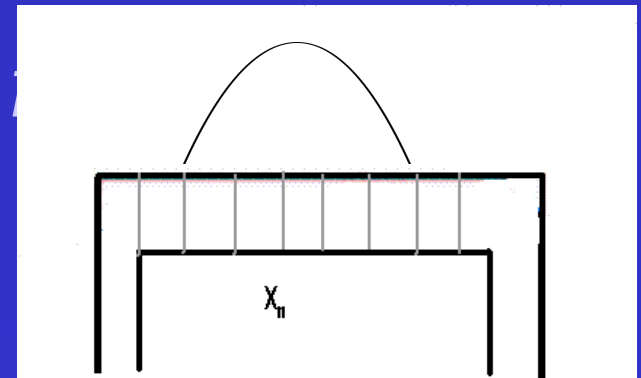
...Bragg peak) of proton with FLUKA, MARS, GEANT etc. ...heat deposition

- beam profile is quadratic (measured)



$$\rho(x,y) = \frac{3\lambda}{2\pi ab} \left[ 1 - \frac{x^2}{a^2} - \frac{y^2}{b^2} \right]^{\frac{1}{2}}$$

- We have 1D model → only



# The new source terms

- We consider proton beam-Hg interaction as a periodic sudden heat shock in the *energy* equation of the liquid and gas phase

$$\frac{\partial \vec{\psi}}{\partial t} + \underline{C} \frac{\partial \vec{\psi}}{\partial x} = \vec{S}$$

$$\frac{\partial A(1-\alpha) \rho_f u_f}{\partial t} + \frac{\partial A(1-\alpha) \rho_f u_f v_f}{\partial x} - p \frac{\partial A \alpha}{\partial t} + p \frac{\partial A(1-\alpha) v_f}{\partial x} = A(Q_{if} - \Gamma_g h_f^* + v_f F_{f,wall}) + E_{f,pulse}(x, t)$$

$$\frac{\partial A \alpha \rho_g u_g}{\partial t} + \frac{\partial A \alpha \rho_g u_g v_g}{\partial x} + p \frac{\partial A \alpha}{\partial t} + p \frac{\partial A \alpha v_g}{\partial x} = A(Q_{ig} + \Gamma_g h_g^* + v_g F_{g,wall}) + E_{g,pulse}(x, t)$$

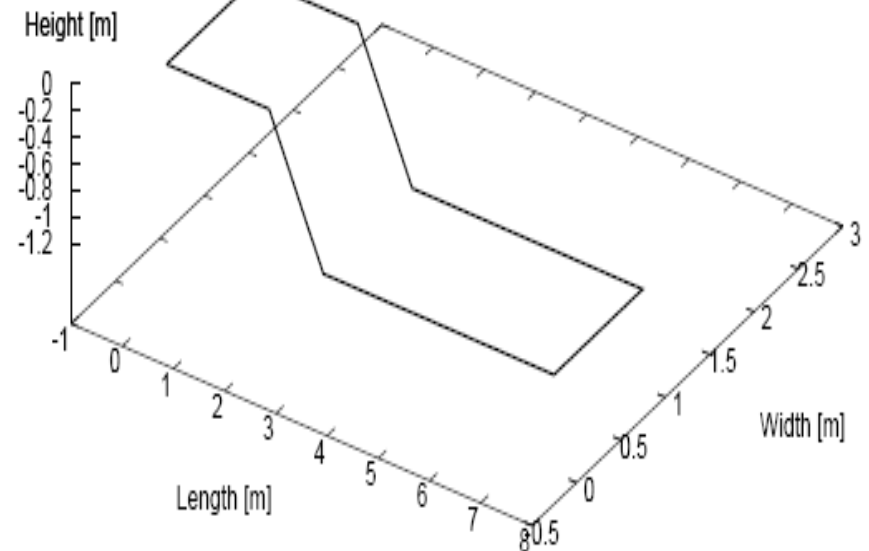
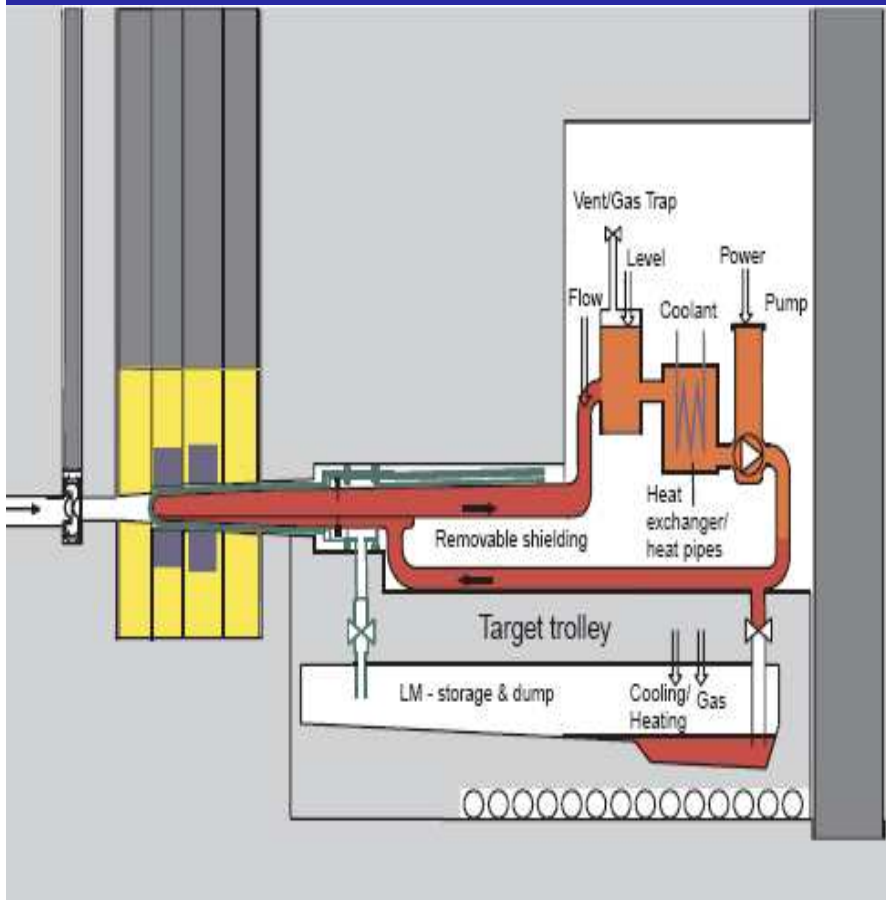
$$E_{g,pulse}(x, t) = \frac{\rho_g \alpha}{\rho_m} E_0 \sin^2 \left[ \frac{\Pi t}{\tau} \right] (1 - (x/x_s)^2)$$

$$E_{f,pulse}(x, t) = \frac{\rho_f (1 - \alpha)}{\rho_m} E_0 \sin^2 \left[ \frac{\Pi t}{\tau} \right] (1 - (x/x_s)^2)$$

*continuity, momentum equations will not be changed*

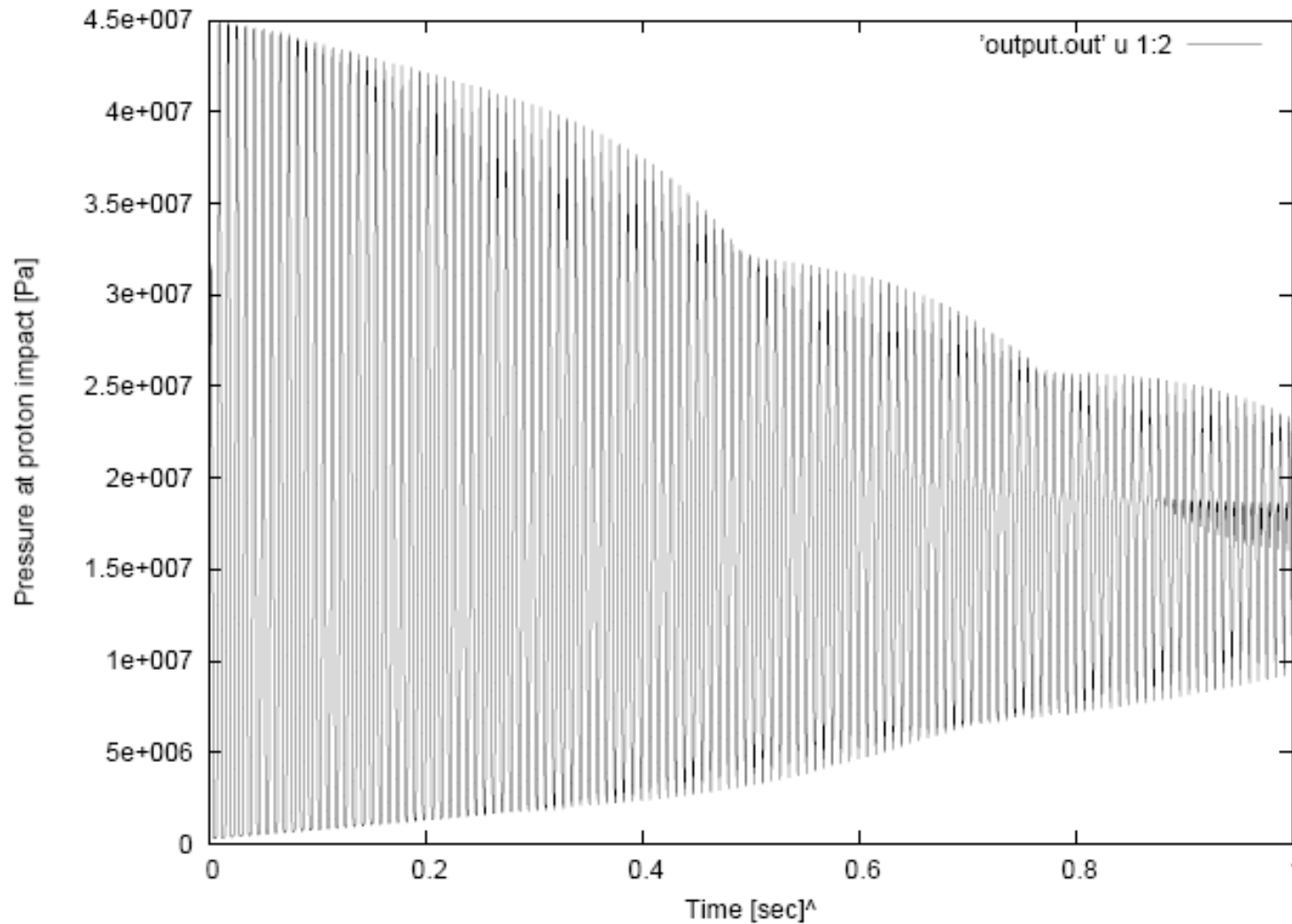
# The schematic scheme of the target

No sophisticated 3D model, like Fluent, Ansys of CFX NO ENGINEERING  
But better physics for boiling-condensation, 2 phase flow





# Our first results



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# Summary and Outlook

*we shortly presented the planned ESS apparatus, and the proton-mercury target system*

*gave a short/gentle introduction into shock waves/2phase flow ☺*

*introduced the WAHA3 model, which is feasible to describe shock waves, quick transients in two phase-flows*

*presented a model which is hopefully a good choice to understand some new physics in proton-Hg system*

*further work is in progress to clear out the dark points and present reasonable results*

I.F. Barna European Physical Journal B,  
Cite as: [arXiv:0805.3618v1](https://arxiv.org/abs/0805.3618v1) [cond-mat.other]

*There are liquid-metal (eq. Li) or liquid helium cooled systems as well... ☺  
(work for the next 20-30 years)*

*Thank you for*



*your attention!*

*Questions, comments, remarks?...*