

Dedicated to the Memory of J. Zimányi

# The Origin of Thermal Hadron Production

Helmut Satz

Universität Bielefeld, Germany

basic observation in all high energy multihadron production

## thermal production pattern

Fermi, Landau, Pomeranchuk, Hagedorn

- species abundances  $\sim$  ideal resonance gas at  $T_H$
- universal  $T_H \simeq 150 - 200$  MeV for all (large)  $\sqrt{s}$
- thermal transverse momentum spectra with same  $T_H$

caveats: baryon density, strangeness, jets, flow

basic observation in all high energy multihadron production

## thermal production pattern

Fermi, Landau, Pomeranchuk, Hagedorn

- species abundances  $\sim$  ideal resonance gas at  $T_H$
- universal  $T_H \simeq 150 - 200$  MeV for all (large)  $\sqrt{s}$
- thermal transverse momentum spectra with same  $T_H$

caveats: baryon density, strangeness, jets, flow

begin by summarizing experimental situation  
in elementary collisions

# 1. Thermal Hadron Production

what is “thermal”?

- equal *a priori* probabilities for all states in accord with a given overall average energy  $\Rightarrow$  temperature  $T$ ;
- partition function of ideal resonance gas

$$\ln Z(T) = V \sum_i \frac{d_i}{(2\pi)^3} \phi(m_i, T)$$

Boltzmann factor  $\phi(m_i, T) = 4\pi m_i^2 T K_2(m_i/T)$

- relative abundances 
$$\frac{N_i}{N_j} = \frac{d_i \phi(m_i, T)}{d_j \phi(m_j, T)}$$

- transverse momenta 
$$\frac{dN}{dp_T^2} \sim \exp -\frac{1}{T} \sqrt{m_i^2 + p_T^2}.$$

## Abundances

$e^+e^-$ , LEP Data [\[Becattini 1996\]](#)

Fit relative abundances to ideal  
resonance gas of all hadronic  
resonances, with  $M \leq 1.7$  GeV,  
two parameters  $T$  and  $\gamma_s$

$$T = 169.9 \pm 2.6 \text{ MeV}$$

$$\gamma_s = 0.691 \pm 0.053$$

$$\chi^2/\text{dof} = 17.2/12$$

estimate systematic error by  
varying resonance gas scheme,  
contributing resonances

$e^+e^- \sqrt{s} = 91.2 \text{ GeV}$				
species	measured			fit
$\pi^+$	8.53	$\pm$	0.40	8.72
$\pi^0$	9.18	$\pm$	0.82	9.83
$K^+$	1.18	$\pm$	0.052	1.06
$K^0$	1.015	$\pm$	0.022	1.01
$\eta$	0.934	$\pm$	0.13	0.908
$\rho^0$	1.21	$\pm$	0.22	1.16
$K^{*+}$	0.357	$\pm$	0.027	0.349
$K^{*0}$	0.372	$\pm$	0.027	0.343
$\eta'$	0.13	$\pm$	0.05	0.1070
$p$	0.488	$\pm$	0.059	0.484
$\phi$	0.10	$\pm$	0.0090	0.167
$\Lambda$	0.185	$\pm$	0.0085	0.152
$\Xi^-$	0.0122	$\pm$	0.00079	0.011
$\Xi^{*0}$	0.0033	$\pm$	0.00047	0.00391
$\Omega$	0.0014	$\pm$	0.00046	0.000782

$$\underline{T = 170 \pm 3 \pm 6 \text{ MeV}}$$

similar analyses carried out for

- $e^+e^-$  at  $\sqrt{s} = 14, 22, 29, 35, 43$  GeV
- $pp$  at  $\sqrt{s} = 19.4, 23.8, 26.0, 27.4$  GeV
- $p\bar{p}$  at  $\sqrt{s} = 200, 500, 900$  GeV
- $\pi^+p$  at  $\sqrt{s} = 21.7$  GeV
- $K^+p$  at  $\sqrt{s} = 11.5, 21.7$  GeV

similar analyses carried out for

- $e^+e^-$  at  $\sqrt{s} = 14, 22, 29, 35, 43$  GeV
- $pp$  at  $\sqrt{s} = 19.4, 23.8, 26.0, 27.4$  GeV
- $p\bar{p}$  at  $\sqrt{s} = 200, 500, 900$  GeV
- $\pi^+p$  at  $\sqrt{s} = 21.7$  GeV
- $K^+p$  at  $\sqrt{s} = 11.5, 21.7$  GeV

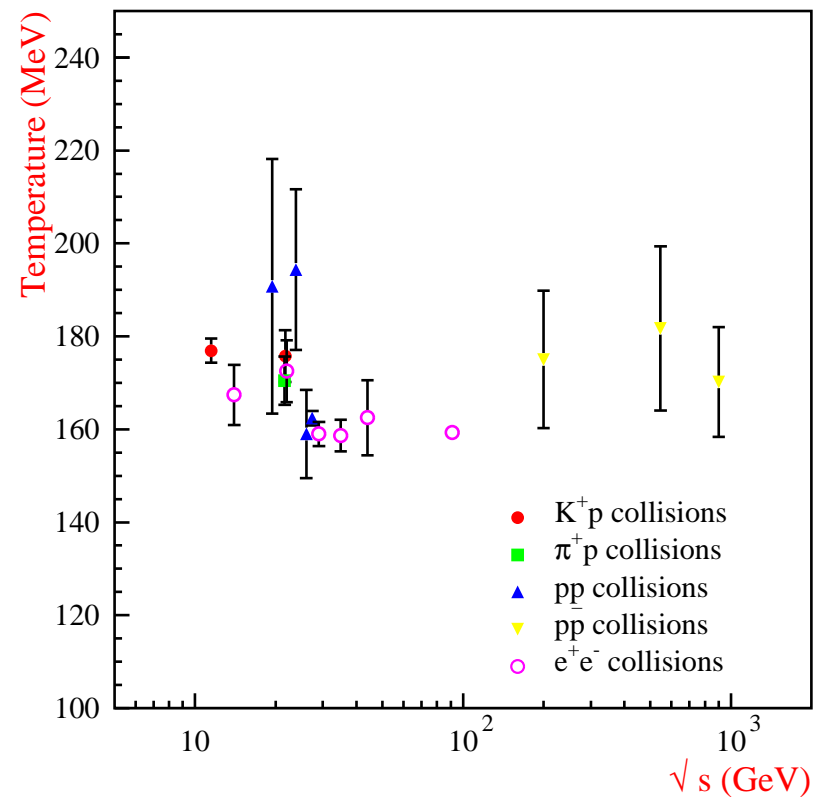
compilation [Becattini 2006](#)

Result:

$$\underline{T \simeq 170 \pm 20 \text{ MeV}}$$

independent of

- collision energy
- collision configuration



Heavy ion collisions  $\Rightarrow$  baryon density

- resonance gas at  $T, \mu_B$ ;  $\mu_B \downarrow$  for  $\sqrt{s} \uparrow$
- elementary high energy collisions  $\mu_B \simeq 0$
- species abundances in high energy heavy ion collisions  
(peak SPS, RHIC)



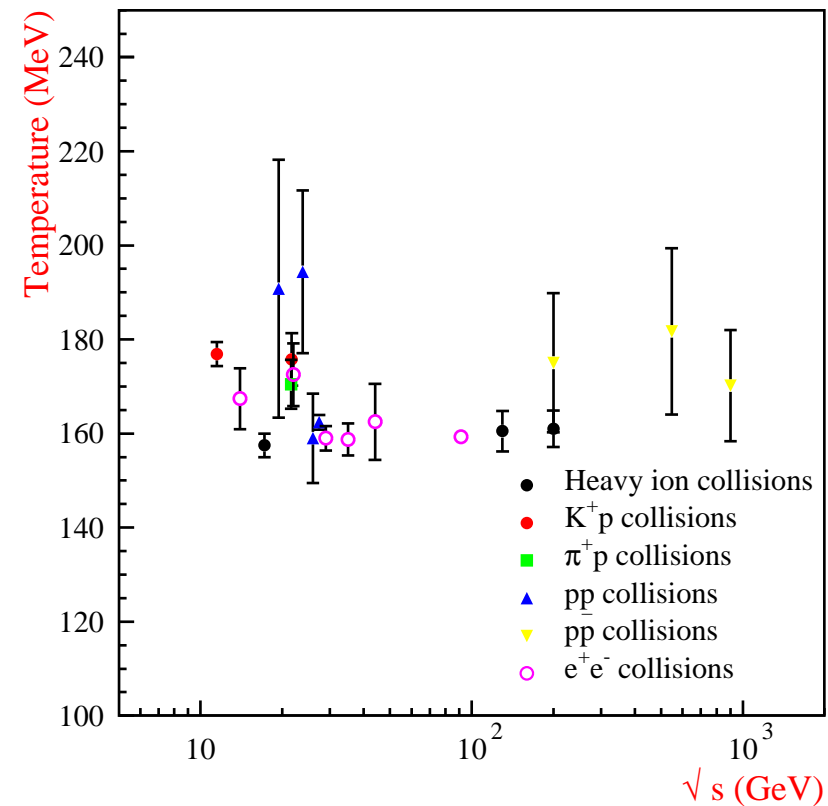
## Heavy ion collisions $\Rightarrow$ baryon density

- resonance gas at  $T, \mu_B$ ;  $\mu_B \downarrow$  for  $\sqrt{s} \uparrow$
- elementary high energy collisions  $\mu_B \simeq 0$
- species abundances in high energy heavy ion collisions (peak SPS, RHIC)

compilation [Becattini 2006](#)

Result:

same hadronization temperature  
for high energy heavy ion and  
elementary collisions,  
independent of collision energy



## Conclude:

**Hadron abundances** in all high energy collisions ( $e^+e^-$  annihilation, hadron-hadron interactions and heavy ion collisions) are those of an ideal resonance gas at a universal temperature

$$T_H \simeq 170 \pm 20 \text{ MeV.}$$

NB: **Transverse momentum spectra** in elementary collisions are in accord with such thermal behaviour.

return later to baryon number dependence & flow in heavy ion collisions

Conclude:

**Hadron abundances** in all high energy collisions ( $e^+e^-$  annihilation, hadron-hadron interactions and heavy ion collisions) are those of an ideal resonance gas at a universal temperature

$$T_H \simeq 170 \pm 20 \text{ MeV.}$$

NB: **Transverse momentum spectra** in elementary collisions are in accord with such thermal behaviour.

return later to baryon number dependence & flow in heavy ion collisions

**WHY?**

Why should **high energy collisions** produce a **thermal medium**?

Multiple parton interactions  $\rightarrow$  kinetic thermalization?

nucleus-nucleus maybe;  $e^+e^-$ , hadron-hadron not

Is there another “non-kinetic” thermalization mechanism?

Is there a common origin of thermal production  
in all high energy collisions?

Why should **high energy collisions** produce a **thermal medium**?

Multiple parton interactions  $\rightarrow$  kinetic thermalization?

nucleus-nucleus maybe;  $e^+e^-$ , hadron-hadron not

Is there another “non-kinetic” thermalization mechanism?

Is there a common origin of thermal production  
in all high energy collisions?

Passing colour charge **disturbs vacuum**, vacuum recovers  
by hadron production according to maximum entropy

What does that mean?

Why should **high energy collisions** produce a **thermal medium**?

Multiple parton interactions  $\rightarrow$  kinetic thermalization?

nucleus-nucleus maybe;  $e^+e^-$ , hadron-hadron not

Is there another “non-kinetic” thermalization mechanism?

Is there a common origin of thermal production  
in all high energy collisions?

Passing colour charge **disturbs vacuum**, vacuum recovers  
by hadron production according to maximum entropy

What does that mean?

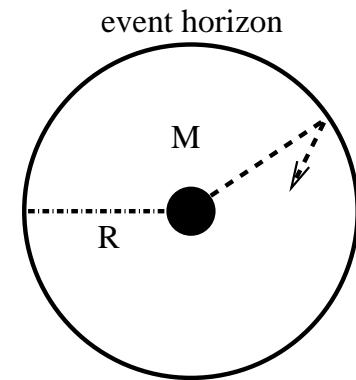
**Conjecture: Colour confinement  $\sim$  black hole physics**

[Paolo Castorina, Dmitri Kharzeev, HS 2007]

## 2. Black Holes and Event Horizons

- black hole

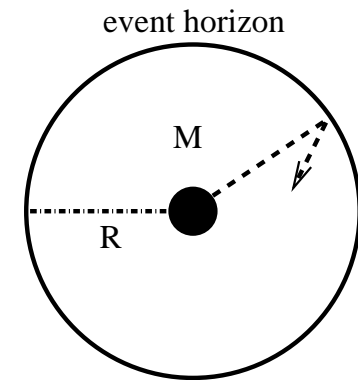
neutron star after gravitational collapse  
large mass  $M$  and compact size  
gravitation so strong that matter &  
light are confined  $\Rightarrow$  event horizon  $R$   
no communication with outside, but...



## 2. Black Holes and Event Horizons

- black hole

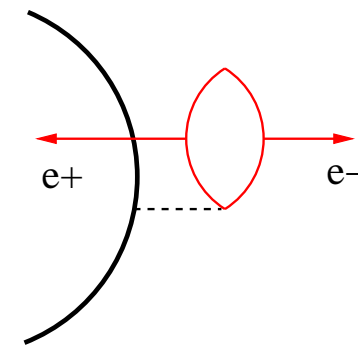
neutron star after gravitational collapse  
large mass  $M$  and compact size  
gravitation so strong that matter &  
light are confined  $\Rightarrow$  event horizon  $R$   
no communication with outside, but...



[Hawking 1975]

- Hawking radiation

quantum effect  $\sim$  uncertainty principle  
vacuum fluctuation  $e^+e^-$  outside event  
horizon, with  $\Delta E \Delta t \sim 1$   
if in  $\Delta t$ ,  $e^+$  falls into black hole,  
then  $e^-$  can escape; equivalent:  
 $e^-$  tunnels through event horizon





- Quantum Causality

no information about state of system beyond event horizon;  $e^+$  on one side,  $e^-$  on the other: EPR

$\Rightarrow$  Hawking radiation must be thermal

$$\frac{dN}{dk} \sim \exp\left\{-\frac{k}{T_{BH}}\right\}$$

with black hole temperature  $T_{BH} = \frac{\hbar}{8\pi c G M}$

relativistic quantum effect: disappears for  $\hbar \rightarrow 0$  or  $c \rightarrow \infty$

$\Rightarrow$  tunnelling through event horizon  $\rightarrow$  thermal radiation

- Quantum Causality

no information about state of system beyond event horizon;  $e^+$  on one side,  $e^-$  on the other: EPR

$\Rightarrow$  Hawking radiation must be thermal

$$\frac{dN}{dk} \sim \exp\left\{-\frac{k}{T_{BH}}\right\}$$

with black hole temperature  $T_{BH} = \frac{\hbar}{8\pi c G M}$

relativistic quantum effect: disappears for  $\hbar \rightarrow 0$  or  $c \rightarrow \infty$

$\Rightarrow$  tunnelling through event horizon  $\rightarrow$  thermal radiation

- Unruh relation

[Unruh 1976]

event horizon arises for systems in uniform acceleration

mass  $m$  in uniform acceleration  $a$

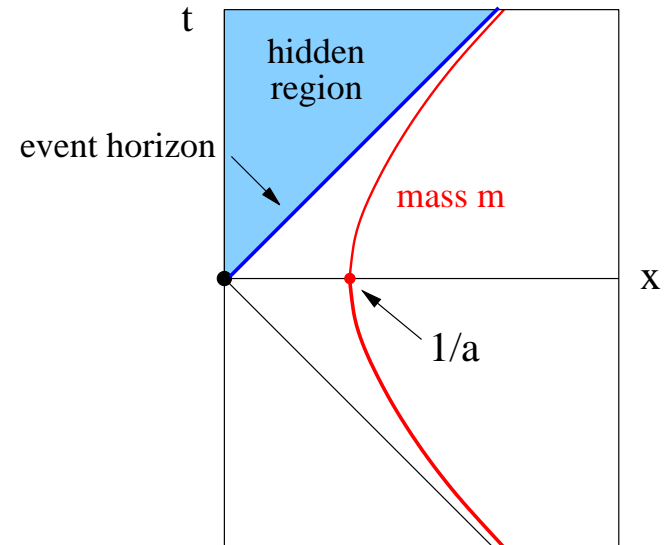
$$\frac{d}{dt} \frac{mv}{\sqrt{1-v^2}} = F$$

$$v = dx/dt, F = ma, c = 1$$

solution: hyperbolic motion

$$x = \frac{1}{a} \cosh a\tau$$

$$t = \frac{1}{a} \sinh a\tau$$

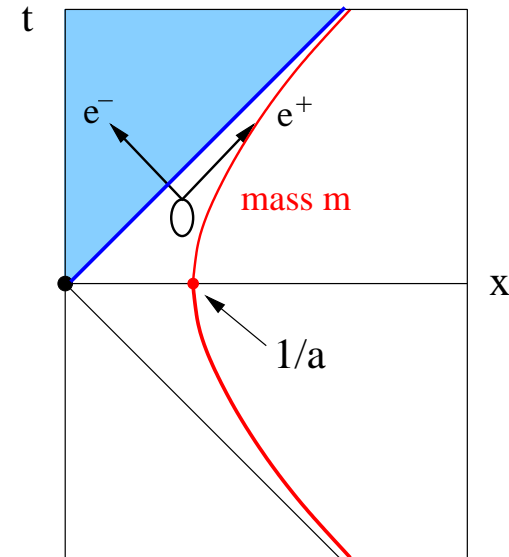


$\exists$  event horizon:  $m$  cannot reach hidden region  
observer in hidden region cannot communicate with  $m$

$m$  passes through vacuum, can use part of acceleration energy to excite vacuum fluctuations on-shell

$e^+$  absorbed in detector on  $m$   
 $e^-$  disappears beyond event horizon

“quantum entanglement”  
 $\sim$  Einstein-Podolsky-Rosen effect



observer on  $m$  as well as observer in hidden region have  
incomplete information:  $\Rightarrow$  each sees thermal radiation

observer on  $m$ :  
physical vacuum = thermal medium of temperature  $T_U$

Unruh temperature  $T_U = \frac{\hbar a}{2\pi c}$  again relativistic quantum effect

for observer in hidden region, Unruh radiation:

passage of  $m \Rightarrow$  thermal radiation of temperature  $T_U$

Black hole event horizon  $R = 2GM$  (Schwarzschild radius)

$$F = ma = G \frac{Mm}{R^2} \Rightarrow a = \frac{GM}{R^2} = \frac{1}{4GM}$$

$$\Rightarrow T_U = \frac{a}{2\pi} = \frac{1}{8\pi GM} = T_{BH}$$

recover Hawking result

for observer in hidden region, Unruh radiation:

passage of  $m \Rightarrow$  thermal radiation of temperature  $T_U$

Black hole event horizon  $R = 2GM$  (Schwarzschild radius)

$$F = ma = G \frac{Mm}{R^2} \Rightarrow a = \frac{GM}{R^2} = \frac{1}{4GM}$$

$$\Rightarrow T_U = \frac{a}{2\pi} = \frac{1}{8\pi GM} = T_{BH}$$

recover Hawking result

In general:

[T. D. Lee 1986, Parikh & Wilczek 2000]

event horizon  $\sim$  information transfer forbidden

$\Rightarrow$  quantum tunnelling  $\sim$  thermal radiation

Relation to QCD?

Gravitation:

matter and light confined to restricted region of space (“black hole”)

QCD:

coloured quarks and gluons confined to restricted region of space, colourless from the outside (“white hole”)

Hadrons as black hole analogue in strong interaction physics?

[Recami & Castorina 1976, Salam & Strathdee 1978]

Schwarzschild radius of nucleon

$$R_g^n = 2 G m \simeq 1.3 \times 10^{-38} \text{ GeV}^{-1} \simeq 3 \times 10^{-39} \text{ fm}$$

Volume of nucleon too big by  $10^{100}$  to be a gravitational  
black hole

Gravitation  $\rightarrow$  strong interaction:  $Gm^2 \rightarrow \alpha_s$ , hence

$$R_s^n = \frac{2\alpha_s}{m} \simeq 1 \text{ fm}$$

if  $\alpha_s \simeq 2 - 3$ .

Hadron radius  $\sim$  “strong” Schwarzschild radius

Hadrons  $\sim$  “strong” black (or “white”) holes  
coloured inside, white outside



Gravitation  $\rightarrow$  strong interaction:  $Gm^2 \rightarrow \alpha_s$ , hence

$$R_s^n = \frac{2\alpha_s}{m} \simeq 1 \text{ fm}$$

if  $\alpha_s \simeq 2 - 3$ .

Hadron radius  $\sim$  “strong” Schwarzschild radius

Hadrons  $\sim$  “strong” black (or “white”) holes  
coloured inside, white outside

More generally:

consider interacting hadrons, multihadron production, in  
the framework of black hole physics concepts

Black hole: event horizon for **all** interactions

White hole: event horizon only for **strong** interactions

### 3. Pair Production and String Breaking

Basic process: two-jet  $e^+e^-$  annihilation, cms energy  $\sqrt{s}$ :

$$e^+e^- \rightarrow \gamma^* \rightarrow q\bar{q} \rightarrow \text{hadrons}$$

$q\bar{q}$  separate subject to constant confining force  $F = \sigma$

initial quark velocity  $v_0 = \frac{p}{\sqrt{p^2 + m^2}}$  ,  $p \simeq \sqrt{s}/2$

Solve  $ma = \sigma$  (hyperbolic motion): [Hosoya 1979, Horibe 1979]

$$\tilde{x} = [1 - \sqrt{1 - v_0\tilde{t} + \tilde{t}^2}] , \quad \tilde{x} = x/x_0 , \quad \tilde{t} = t/x_0$$

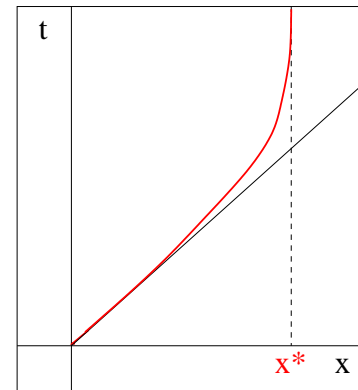
with

$$x_0 = \frac{m}{\sigma} \frac{1}{\sqrt{1 - v_0^2}} = \frac{m}{\sigma} \gamma = \frac{1}{a} \gamma$$

classical turning point  $v(t^*) = 0$  at

$$x^* = x(t^*) = \frac{m}{\sigma} \gamma [1 - \sqrt{1 - (v_0/2)^2}] \simeq \frac{\sqrt{s}}{2\sigma}$$

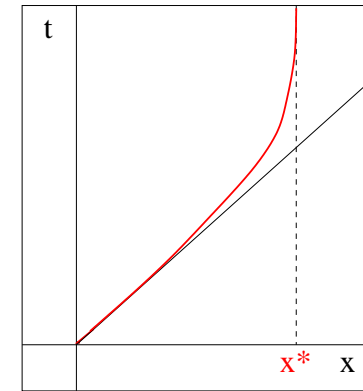
$q\bar{q}$  can separate arbitrarily far  
if  $\sqrt{s}$  is large enough



classical turning point  $v(t^*) = 0$  at

$$x^* = x(t^*) = \frac{m}{\sigma} \gamma [1 - \sqrt{1 - (v_0/2)^2}] \simeq \frac{\sqrt{s}}{2\sigma}$$

$q\bar{q}$  can separate arbitrarily far  
if  $\sqrt{s}$  is large enough

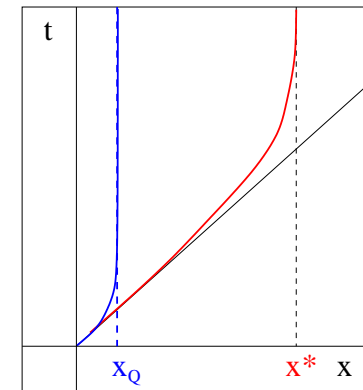


What's wrong?

classical event horizon

Strong field  $\Rightarrow$  vacuum unstable  
against pair production [Schwinger 1951]

when  $\sigma x > \sigma x_Q \equiv 2m$   
string connecting  $q\bar{q}$  breaks



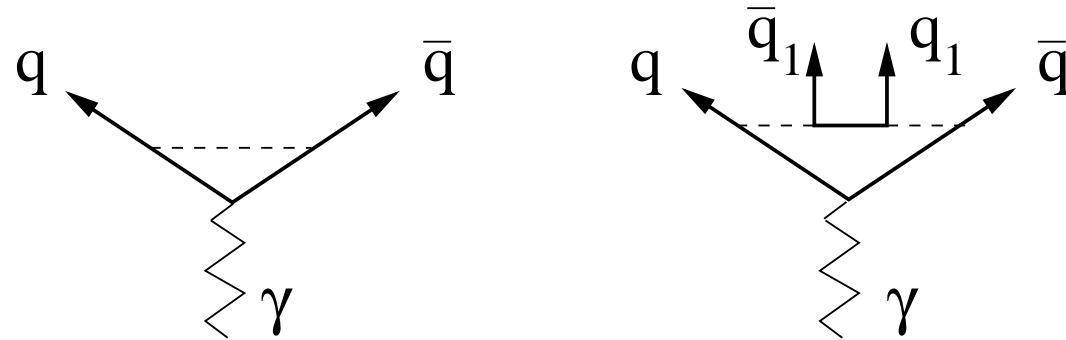
Result:

quantum event horizon

Hadron production in  $e^+e^-$  annihilation:

“inside-outside cascade”

[Bjorken 1976]



$q\bar{q}$  flux tube has thickness

$$r_T \simeq \sqrt{\frac{2}{\pi\sigma}}$$

$q_1\bar{q}_1$  at rest in cms, but

$$k_T \simeq \frac{1}{r_T} \simeq \sqrt{\frac{\pi\sigma}{2}}$$

$q\bar{q}$  separation at  $q_1\bar{q}_1$  production

$$\sigma x(q\bar{q}) = 2\sqrt{m^2 + k_T^2}$$

$q_1$  screens  $\bar{q}$  from  $q$ , hence string breaking at

$$x_q \simeq \frac{2}{\sigma} \sqrt{m^2 + (\pi\sigma/2)} \simeq \sqrt{\frac{2\pi}{\sigma}} \simeq 1 \text{ fm}$$

new flux tubes  $q\bar{q}_1$  and  $\bar{q}q_1$

stretch  $q_1\bar{q}_1$

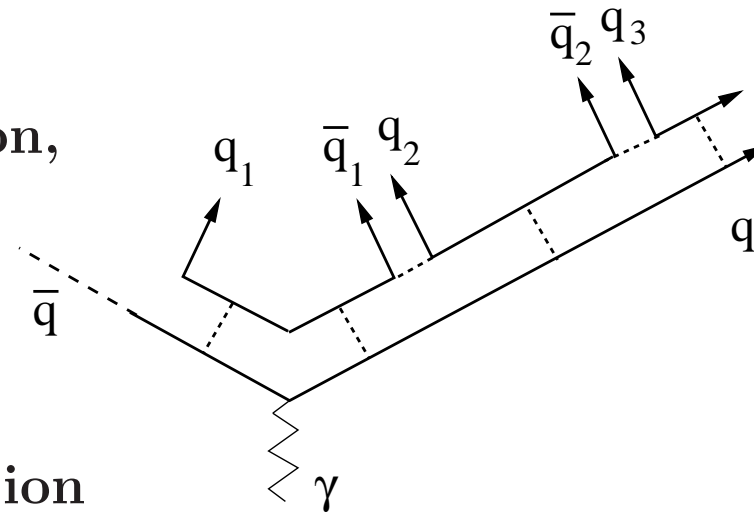
to form new pair  $q_2\bar{q}_2$

$$\sigma x(q_1\bar{q}_1) = 2\sqrt{m^2 + k_T^2}$$

equivalent:

$\bar{q}_1$  reaches  $q_1\bar{q}_1$  event horizon,  
tunnels to become  $\bar{q}_2$

emission of hadron  $\bar{q}_1 q_2$   
as Hawking radiation



self-similar pattern:

screening

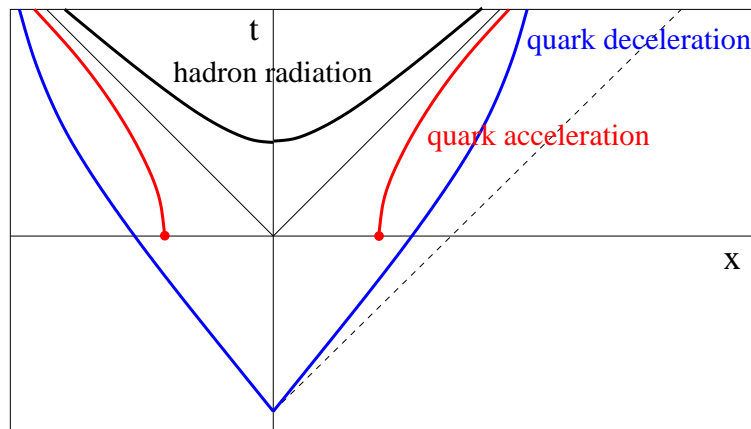
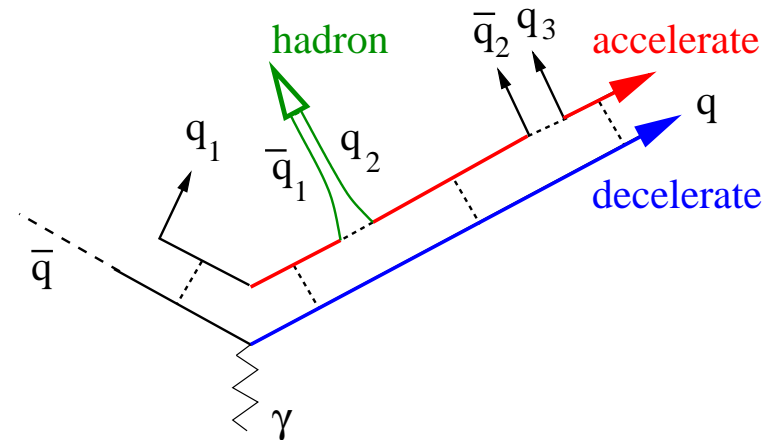
string breaking

tunnelling

quark acceleration

/deceleration

Hawking radiation



temperature of Hawking radiation: what acceleration?

$$(\bar{q}_1 \rightarrow \bar{q}_2 \rightarrow \bar{q}_3 \rightarrow \dots)$$

bring quark on-shell

$$v = 0 \rightarrow v = k_T / (m^2 + k_T^2)^{1/2} \simeq 1$$

in virtuality time  $\Delta\tau = 1/\Delta E \simeq 1/2k_T$

$$a = \frac{\Delta v}{\Delta\tau} \simeq 2k_T \simeq \sqrt{2\pi\sigma} \simeq 1.1 \text{ GeV}$$

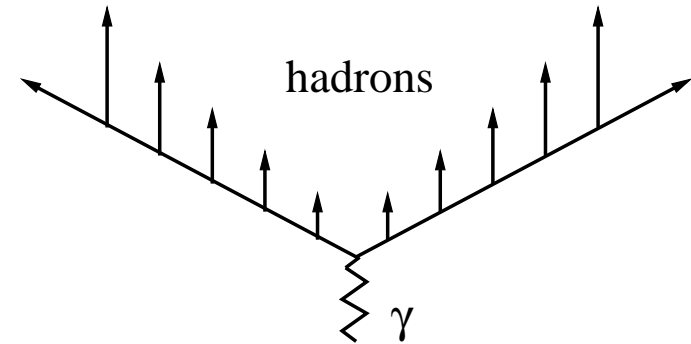
$\Rightarrow$  temperature of hadronic Hawking radiation

$$T_q = \frac{a}{2\pi} \simeq \sqrt{\frac{\sigma}{2\pi}} \simeq 180 \text{ MeV}$$

determines: hadron species abundances,  $p_T$  spectra



hadronization pattern:  
hadron multiplicity?



thickness of classical “overstretched” string:

$$R_T^2 = \frac{2}{\pi\sigma} \sum_{k=0}^K \frac{1}{2k+1} \simeq \frac{2}{\pi\sigma} \ln 2K \simeq \frac{2}{\pi\sigma} \ln \sqrt{s}$$

quantum breaking at  $x_q \sim r_T$ , hence hadron multiplicity

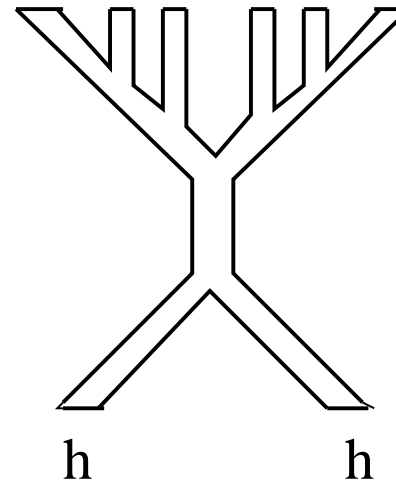
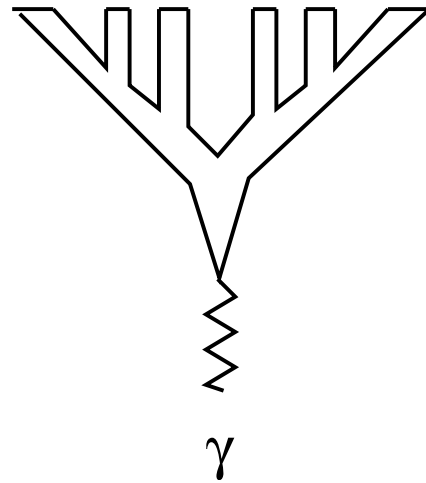
$$\nu(s) \simeq \frac{R_T^2}{r_T^2} \simeq \ln \sqrt{s}$$

NB: parton evolution (minijets), multiple jets lead to stronger increase  
parton saturation: see [Kharzeev & Tuchin](#)

generalize:

$e^+e^-$  annihilation  
white hole creation

hadron-hadron collision  
white hole fusion



both  $\rightarrow$  self-similar cascades

Heavy ion collisions  $\Rightarrow$

- baryon number
- centrality (“spin”)

## 4. Charged and Rotating Black Holes

Black holes: three (& only three) observable properties

mass  $M$ , charge  $Q$ , angular momentum  $J$

hence thermal Hawking radiation  $\Rightarrow T_H(M, Q, J)$

Origin of event horizon?

invariant space-time metric (time  $t$ , space  $r$ , latitude  $\theta$ )

$$ds^2 = f_t(M, Q, J) dt^2 - f_r(M, Q, J) dr^2 - f_\theta(M, Q, J) d\theta^2$$

event horizon:  $f_r \rightarrow \infty$

## 4. Charged and Rotating Black Holes

Black holes: three (& only three) observable properties

mass  $M$ , charge  $Q$ , angular momentum  $J$

hence thermal Hawking radiation  $\Rightarrow T_H(M, Q, J)$

Origin of event horizon?

invariant space-time metric (time  $t$ , space  $r$ , latitude  $\theta$ )

$$ds^2 = f_t(M, Q, J) dt^2 - f_r(M, Q, J) dr^2 - f_\theta(M, Q, J) d\theta^2$$

event horizon:  $f_r \rightarrow \infty$

•  $Q = J = 0$ : Schwarzschild BH

$$T_S(M) = \frac{1}{8\pi G M}$$

- $Q \neq 0, J = 0$ : Reissner-Nordström BH

$$T_{RN}(M, Q) = T_S(M) \left\{ \frac{4 \sqrt{1 - Q^2/GM^2}}{(1 + \sqrt{1 - Q^2/GM^2})^2} \right\} < T_S(M)$$

smaller than  $T_S(M)$  because Coulomb repulsion  
partially balances gravitational attraction

- $Q \neq 0, J = 0$ : Reissner-Nordström BH

$$T_{RN}(M, Q) = T_S(M) \left\{ \frac{4 \sqrt{1 - Q^2/GM^2}}{(1 + \sqrt{1 - Q^2/GM^2})^2} \right\} < T_S(M)$$

smaller than  $T_S(M)$  because Coulomb repulsion  
partially balances gravitational attraction

- $Q = 0, J \neq 0$ : Kerr BH    ( $\rho = J/M$ )

$$T_K(M, J) = T_S(M) \left\{ \frac{4\sqrt{1 - \rho^2/(GM)^2}}{(1 + \sqrt{1 - \rho^2/(GM)^2})^2} \right\} < T_S(M)$$

smaller than  $T_S(M)$  because centrifugal force  
partially balances gravitational attraction

normally  $f_r \rightarrow \infty \Rightarrow f_t \rightarrow 0$

for rotating BH, two distinct solutions:

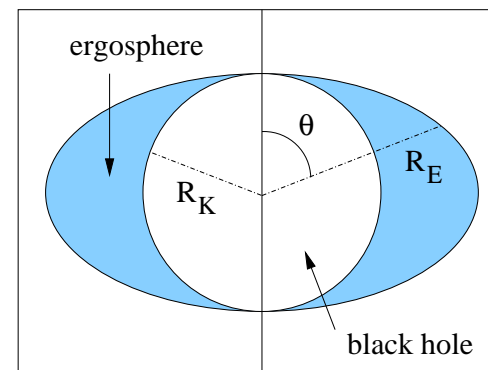
event horizon

$$f_r \rightarrow \infty \Rightarrow R_K = GM (1 + \sqrt{1 - \rho^2 / (GM)^2})$$

ergosphere

$$f_t \rightarrow 0 \Rightarrow R_E = GM (1 + \sqrt{1 - [\rho^2 / (GM)^2] \cos^2 \theta})$$

in ergosphere,  
rotational drag  
affects even light



## 5. Baryon Density and Non-Central Collisions

White holes: three (& only three) features  
observable in strong interactions:

$\sqrt{s}$ , net baryon number, angular momentum

$\sqrt{s}$  determines classical event horizon,  $\sim$  multiplicity

Hawking radiation at earlier quantum horizon,  
 $\Rightarrow T_H(\sigma)$ , not  $T_H(\sqrt{s})$



## 5. Baryon Density and Non-Central Collisions

White holes: three (& only three) features  
observable in strong interactions:

$\sqrt{s}$ , net baryon number, angular momentum

$\sqrt{s}$  determines classical event horizon,  $\sim$  multiplicity

Hawking radiation at earlier quantum horizon,  
 $\Rightarrow T_H(\sigma)$ , not  $T_H(\sqrt{s})$

baryon number  $\Rightarrow T_H(\sigma, \mu_B)$

angular momentum  $\Rightarrow T_H(\sigma, \text{centrality})$

## 5. Baryon Density and Non-Central Collisions

White holes: three (& only three) features  
observable in strong interactions:

$\sqrt{s}$ , net baryon number, angular momentum

$\sqrt{s}$  determines classical event horizon,  $\sim$  multiplicity

Hawking radiation at earlier quantum horizon,  
 $\Rightarrow T_H(\sigma)$ , not  $T_H(\sqrt{s})$

baryon number  $\Rightarrow T_H(\sigma, \mu_B)$

angular momentum  $\Rightarrow T_H(\sigma, \text{centrality})$

### ● Baryon Density

Coulomb repulsion  
vs. gravitation



baryon repulsion vs.  
vacuum pressure

Fermion pressure at  $T = 0$

$$P = \left( \frac{d_f}{24\pi^2} \right) \mu^4$$

against vacuum pressure

$$B \sim \langle G_{\mu\nu}^2 \rangle$$

leads to

$$\mu_0 = (2\pi^2 B)^{1/4}$$

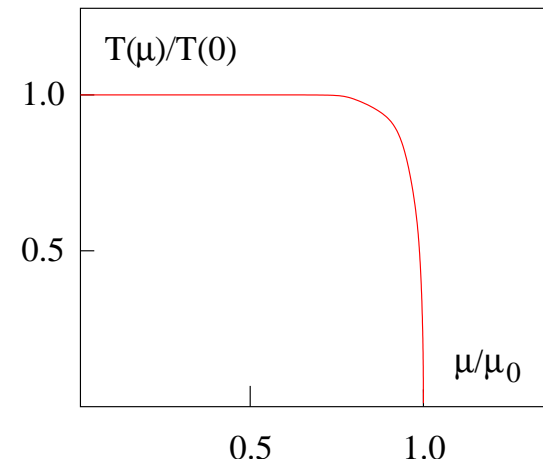
Fermion pressure at  $T = 0$        $P = \left( \frac{d_f}{24\pi^2} \right) \mu^4$

against vacuum pressure       $B \sim \langle G_{\mu\nu}^2 \rangle$

leads to       $\mu_0 = (2\pi^2 B)^{1/4}$

and hence to Hawking  
hadronization temperature

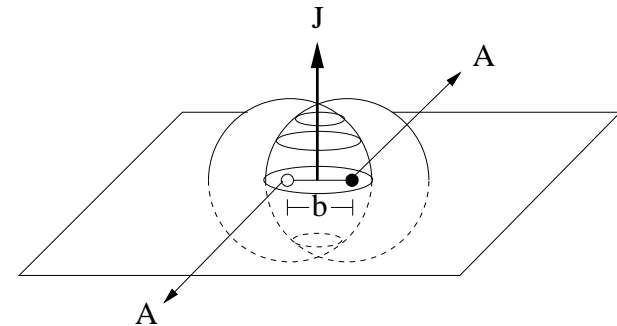
$$T(\mu)/T_0 = \frac{\sqrt{1 - (\mu/\mu_0)^4}}{(1 + \sqrt{1 - (\mu/\mu_0)^4})^2}$$



overly simplistic - include realistic baryon interaction

- Angular Momentum

Non-central  $AA$  collision  
impact parameter  $b$

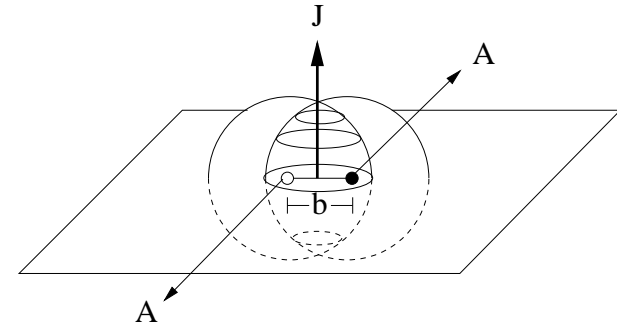


assume interaction region rotates

(collective effect  $\sim$  hydro)

- Angular Momentum

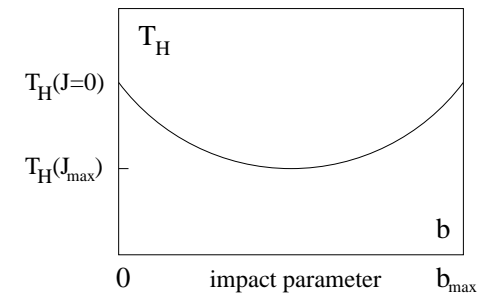
Non-central  $AA$  collision  
impact parameter  $b$



assume interaction region rotates

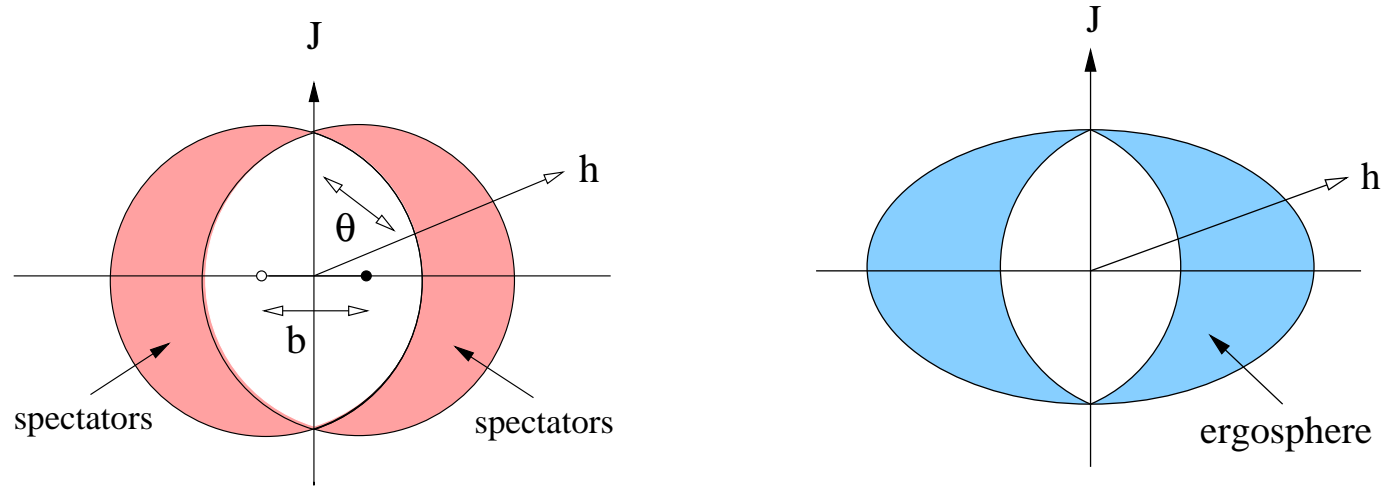
(collective effect  $\sim$  hydro)

$\Rightarrow T_H$  decreases with centrality  
increases again when collectivity  
stops



test through species abundance ratios

ergosphere  $R_E(J \cos \theta) \rightarrow$   
 azimuthal dependence of hadron spectra



along polar axis: no “flow”,  $T_H(J) < T_H(J = 0)$

along equator: “flow”,  $T_H(J) < T_H(J = 0)$

test in simultaneous study of species abundances  
 and  $p_T$  spectra

## 5. Kinetic vs. Stochastic Thermalization

Kinetic thermalization:

time evolution of given non-equilibrium configuration  
(two parallel colliding parton beams)  
through multiple collisions  
to a time-independent equilibrium state  
(quark-gluon plasma)

requires

- many constituents
- sufficiently large interaction cross sections
- sufficiently long time

thermal hadron production in  $e^+e^-$ ,  $pp/pp\bar{p}$ ?

Hagedorn: *the emitted hadrons are “born into equilibrium”*



Hawking radiation:

final state produced at random from the set of all states  
corresponding to temperature  $T_H$   
determined by confining field

this set of all final states is same as that  
produced by kinetic thermalization

measurements cannot tell if the equilibrium was reached  
by thermal evolution or by throwing dice:

$\Rightarrow$  Thermodynamic Equivalence Principle  $\Leftarrow$

## 6. Summary

- The physical vacuum is an event horizon for coloured quarks and gluons; thermal hadrons are the Hawking radiation produced by quark tunnelling through this event horizon.

## 6. Summary

- The physical vacuum is an event horizon for coloured quarks and gluons; thermal hadrons are the Hawking radiation produced by quark tunnelling through this event horizon.
- The corresponding hadronization temperature  $T_H$  is determined by quark acceleration and deceleration in the colour field at the (quantum) horizon.

## 6. Summary

- The physical vacuum is an event horizon for coloured quarks and gluons; thermal hadrons are the Hawking radiation produced by quark tunnelling through this event horizon.
- The corresponding hadronization temperature  $T_H$  is determined by quark acceleration and deceleration in the colour field at the (quantum) horizon.
- Energy, baryon number and angular momentum of the QCD “black hole” provide the multiplicity of produced hadrons and the dependence of  $T_H$  on baryon density and collision centrality.

## 6. Summary

- The physical vacuum is an event horizon for coloured quarks and gluons; thermal hadrons are the Hawking radiation produced by quark tunnelling through this event horizon.
- The corresponding hadronization temperature  $T_H$  is determined by quark acceleration and deceleration in the colour field at the (quantum) horizon.
- Energy, baryon number and angular momentum of the QCD “black hole” provide the multiplicity of produced hadrons and the dependence of  $T_H$  on baryon density and collision centrality.
- The resulting scenario provides a common basis for thermal hadron production in QCD interactions, from  $e^+e^-$  annihilation to nuclear collisions.

NB:

In astrophysics/gravitation, Hawking radiation  
is not observed/observable ( $T_{BH} \ll 2.7^\circ\text{K}$ )

NB:

In astrophysics/gravitation, Hawking radiation  
is not observed/observable ( $T_{BH} \ll 2.7^\circ\text{K}$ )

Thermal hadron production:

first experimental confirmation of Hawking-Unruh  
radiation

God does play dice, but He sometimes throws them where they can't be seen.

Stephen Hawking