

Violation of k_{\perp} factorization in quark production from the Color Glass Condensate

H. Fujii,^a F. Gelis^b and R. Venugopalan^c

^aInstitute of Physics, University of Tokyo, Komaba, Tokyo 153-8902, Japan

^bCEA/DSM/SPhT, 91191 Gif-sur-Yvette cedex, France

^cPhysics Department, Brookhaven National Laboratory, Upton, New York 11973, USA

We examine the violation of the k_{\perp} factorization approximation for quark production in high energy proton-nucleus collisions. We comment on its implications for the open charm and quarkonium production in collider experiments.

1. Introduction

Semi-hard processes, where $\sqrt{s} \gg m_{q_{\perp}} \gg \Lambda_{\text{QCD}}$, contribute significantly to particle production in high-energy collider experiments due to the large density of the small- x gluons. The k_{\perp} factorization formalism[1] systematically resums corrections of $(\alpha_s \ln(s/q_{\perp}^2))^n$ from gluon branchings in perturbative QCD. In this framework, the particle production cross-section is expressed as a convolution of a hard matrix element and *unintegrated* distributions of gluons in the hadrons with definite transverse momentum $\mathbf{k}_{i\perp}$ and longitudinal fraction x_i in each projectile hadron ($i=1, 2$).

Multiple-scattering (higher twist) effects become important at small x due to the large density of small- x gluons. It is expected to be the origin of the Cronin enhancement and p_{\perp} broadening of hadrons observed in nuclear experiments. It is also relevant for the nuclear suppression of quarkonium production.

The simplest situation for studying the impact of higher twist effects on k_{\perp} factorization is in proton-nucleus (pA) collisions, wherein the proton is dilute and the nucleus is dense. The k_{\perp} factorization formalism was examined in the color glass condensate framework[2]. It is shown that the factorization is recovered when one keeps only the terms that are of the lowest order in the charge sources $\rho_{p,A}$ of the projectiles[3]. The cross-sections at the leading order in ρ_p , but at all orders in the dense source ρ_A of the nucleus are obtained analytically. Gluon production by the “2-to-1” processes is shown to be k_{\perp} -factorizable [4–6] whereas the quark production is generally not[7–9].

Here we report the numerical estimates for the k_{\perp} factorization breaking in quark production within the McLerran-Venugopalan (MV) model[10]. We briefly discuss open charm production and quarkonium suppression in pA collisions in this framework.

2. Violation of k_\perp factorization in quark pair production

The quark pair production cross-section is obtained as[7]:

$$\begin{aligned}
\frac{d\sigma}{d^2\mathbf{p}_\perp d^2\mathbf{q}_\perp dy_p dy_q} &= \frac{\alpha_s^2 N}{8\pi^4 (N^2 - 1)} \int_{\mathbf{k}_{1\perp}, \mathbf{k}_{2\perp}} \frac{\delta(\mathbf{p}_\perp + \mathbf{q}_\perp - \mathbf{k}_{1\perp} - \mathbf{k}_{2\perp})}{\mathbf{k}_{1\perp}^2 \mathbf{k}_{2\perp}^2} \\
&\times \left\{ \int_{\mathbf{k}_\perp, \mathbf{k}'_\perp} \text{tr}_d \left[(\not{q} + m) T_{q\bar{q}} (\not{p} - m) \gamma^0 T_{q\bar{q}}^\dagger \gamma^0 \right] \phi_A^{q\bar{q}, q\bar{q}}(\mathbf{k}_{2\perp}; \mathbf{k}_\perp, \mathbf{k}'_\perp) \right. \\
&\quad + \int_{\mathbf{k}_\perp} \text{tr}_d \left[(\not{q} + m) T_{q\bar{q}} (\not{p} - m) \gamma^0 T_g^\dagger \gamma^0 + \text{h.c.} \right] \phi_A^{q\bar{q}, g}(\mathbf{k}_{2\perp}; \mathbf{k}_\perp) \\
&\quad \left. + \text{tr}_d \left[(\not{q} + m) T_g (\not{p} - m) \gamma^0 T_g^\dagger \gamma^0 \right] \phi_A^{g, g}(\mathbf{k}_{2\perp}) \right\} \varphi_p(\mathbf{k}_{1\perp}), \quad (1)
\end{aligned}$$

where the explicit forms for the Dirac matrices $T_{q\bar{q}}(\mathbf{k}_{1\perp}, \mathbf{k}_\perp)$ and $T_g(\mathbf{k}_{1\perp})$ are given in [7]. Here $\varphi_p(\mathbf{l}_\perp) \equiv (\pi^2 R_p^2 g^2 / l_\perp^2)$ F.T. $\langle \rho_p^a(\mathbf{0}) \rho_p^a(\mathbf{x}_\perp) \rangle$ is the unintegrated gluon distribution for the proton, and F.T. denotes the Fourier transformation. One needs, however, *three* nuclear distributions defined as (see Eqs. (42), (43) and (45) in [7])

$$\begin{aligned}
\phi_A^{g, g}(\mathbf{l}_\perp) &\equiv \frac{\pi^2 R_A^2 l_\perp^2}{g^2 N} \text{F.T. tr} \langle U(\mathbf{0}) U^\dagger(\mathbf{x}_\perp) \rangle, \\
\phi_A^{q\bar{q}, g}(\mathbf{l}_\perp; \mathbf{k}_\perp) &\equiv \frac{2\pi^2 R_A^2 l_\perp^2}{g^2 N} \text{F.T. tr} \langle \tilde{U}(\mathbf{x}_\perp) t^a \tilde{U}^\dagger(\mathbf{y}_\perp) t^b U_{ba}(\mathbf{0}) \rangle, \\
\phi_A^{q\bar{q}, q\bar{q}}(\mathbf{l}_\perp; \mathbf{k}_\perp, \mathbf{k}'_\perp) &\equiv \frac{2\pi^2 R_A^2 l_\perp^2}{g^2 N} \text{F.T. tr} \langle \tilde{U}(\mathbf{0}) t^a \tilde{U}^\dagger(\mathbf{y}_\perp) \tilde{U}(\mathbf{x}'_\perp) t^a \tilde{U}^\dagger(\mathbf{y}'_\perp) \rangle, \quad (2)
\end{aligned}$$

where U and \tilde{U} denote the path-ordered exponentials of the gauge fields in the nucleus in the adjoint and fundamental representations, respectively, and describe the multiple scatterings of the gluon and the quarks. The average $\langle \dots \rangle$ is taken over the Gaussian distribution of the color charge sources characterized by the saturation scale Q_s^2 .

k_\perp factorization is violated by the transverse structure of the quark pair probed by the momentum $\mathbf{k}_\perp^{(i)}$ from the nucleus since each quark from the pair can resolve and interact with several gluons from the nucleus. If any of the transverse masses m_{q_\perp} and m_{p_\perp} of the produced quarks is large compared with the typical rescattering scale, Q_s , we can neglect $\mathbf{k}_\perp^{(i)}$ in $T_{q\bar{q}}(\mathbf{k}_{1\perp}, \mathbf{k}_\perp^{(i)})$ and recover the k_\perp factorized formula thanks to the sum rule for ϕ_A 's: $\int_{\mathbf{k}_\perp, \mathbf{k}'_\perp} \phi_A^{q\bar{q}, q\bar{q}} = \int_{\mathbf{k}_\perp} \phi_A^{q\bar{q}, g} = \phi_A^{g, g}$.

In Fig. 1 we compare the exact result with the k_\perp factorized approximation for single charm quark production. The breaking is relatively small for the saturation momentum $Q_s^2=1 \text{ GeV}^2$, which may be the relevant scale for RHIC at central rapidity. At $Q_s^2=15, 25 \text{ GeV}^2$ (corresponding to very forward rapidities in the proton fragmentation region at RHIC and LHC) the correction can be as large as 40% at $q_\perp \sim Q_s$. For the bottom quark production the violation is smaller. To assess the model-dependence of our results, we compute them now, shown in Fig. 2, with a non-local Gaussian model known to be the

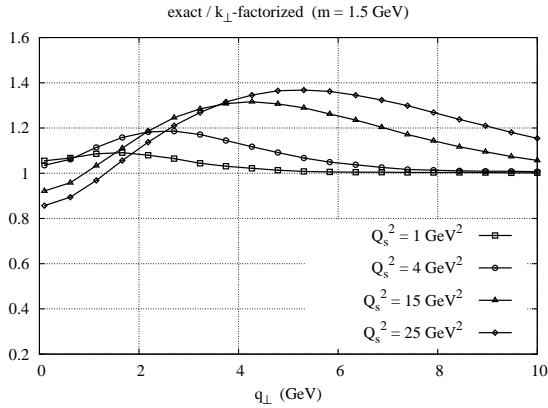


Figure 1. Breaking of k_{\perp} factorization in single charm quark production.

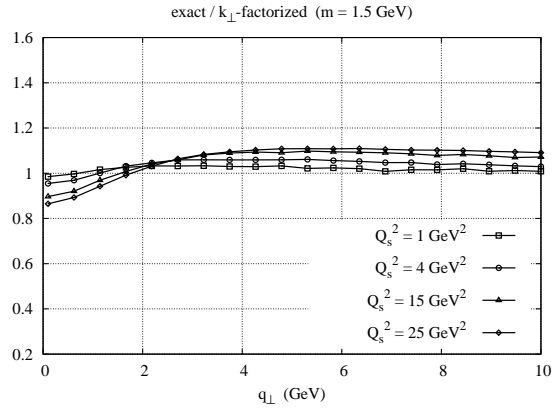


Figure 2. The same as in Fig. 1 but in the nonlocal Gauss model.

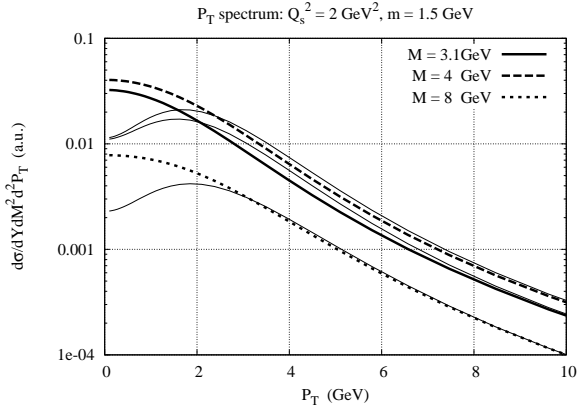


Figure 3. P_{\perp} spectrum of the quark pair with fixed invariant mass M .

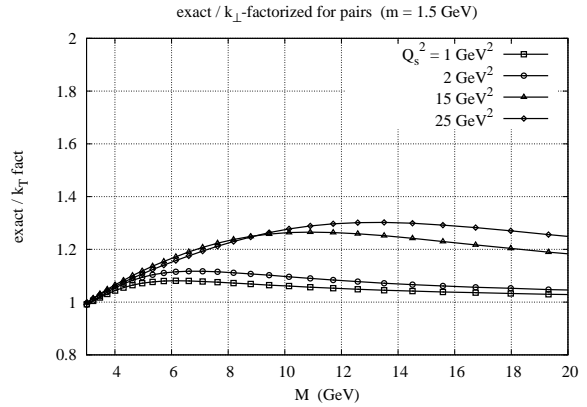


Figure 4. Breaking of k_{\perp} factorization in charm quark pair production.

asymptotic solution of renormalization equations for x evolution[11]; non-linear evolution effects reduce the magnitude of the violation of k_{\perp} factorization.

In Fig. 3 shown is the total P_{\perp} distribution of the charm quark pair with the fixed invariant masses $M=3.1, 4, 8$ GeV. In the k_{\perp} factorized approximation (thin curves), either quark or antiquark exchanges all the momentum from the nucleus and we see the bump structure near Q_s , reflecting the gluon distribution of the nucleus. The bump is smeared out due to multiple scatterings of both the quark and antiquark in the full formula. Integrating over P_{\perp} , we show in Fig. 4, the magnitude of factorization breaking in the invariant mass spectrum of the pair.

3. Phenomenology

We study the importance of small- x distributions in D meson production by convoluting the single quark spectrum with an appropriate fragmentation function[12]. We find, however, the production spectrum is determined not by the quark distribution with $q_{\perp} \lesssim Q_s$, but largely by the tail part $\propto 1/q_{\perp}^4$ of the MV model. Moreover, in order to assess

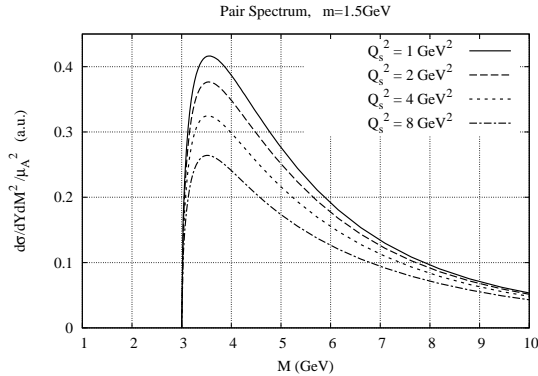


Figure 5. Q_s^2 dependence of the charm pair production.

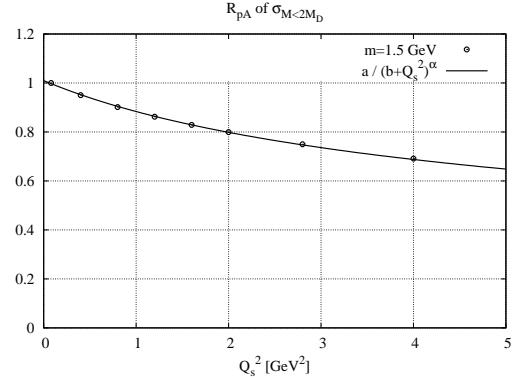


Figure 6. Suppression of low mass pairs in pA collisions.

the rapidity dependence of open charm production, the x -dependence of the unintegrated gluon distributions should be taken into account, which requires going beyond the MV model. Our results on open charm production will be reported elsewhere[13].

The Q_s^2 -dependence of the pair spectrum (divided by the charge density μ_A^2) is displayed in Fig. 5. At larger M , where the high-density effects are diminished, all curves converge to a single one. The multiple scatterings of the pair quarks suppress the yield in the low M region. (The overall cross-section is of course enhanced with increasing Q_s^2 .) One can get an idea about the normal suppression of the quarkonium production in the pA collisions, relying on the color evaporation picture. We show the nuclear modification ratio, R_{pA} , for the pairs with M less than the open charm threshold $2M_D$, as a function of Q_s^2 . The suppression pattern fits the form $1/(Q_s^2)^\alpha$ with $\alpha \sim 0.42$, and not the frequently assumed exponential form. One should note here that $Q_s^2 \sim A^{1/3}$ in the MV model.

REFERENCES

1. S. Catani, M. Ciafaloni, F. Hautmann, Nucl. Phys. **B 366**, 135 (1991); J.C. Collins, R.K. Ellis, Nucl. Phys. **B 360**, 3 (1991).
2. E. Iancu, R. Venugopalan, hep-ph/0303204; K. Itakura, these proceedings.
3. F. Gelis, R. Venugopalan, Phys. Rev. **D 69**, 014019 (2004).
4. Yu.V. Kovchegov, A.H. Mueller, Nucl. Phys. **B 529**, 451 (1998); A. Dumitriu, L.D. McLerran, Nucl. Phys. **A 700**, 492 (2002).
5. J.P. Blaizot, F. Gelis, R. Venugopalan, Nucl. Phys. **A 743**, 13 (2004).
6. Yu.V. Kovchegov, K. Tuchin, Phys. Rev. **D 65**, 074026 (2002); D. Kharzeev, Yu. Kovchegov, K. Tuchin, Phys. Rev. **D 68**, 094013 (2003).
7. J.P. Blaizot, F. Gelis, R. Venugopalan, Nucl. Phys. **A 743**, 57 (2004).
8. K. Tuchin, Phys. Lett. **B 593**, 66 (2004).
9. N. N. Nikolaev and W. Schafer, Phys. Rev. **D 71**, 014023 (2005).
10. H. Fujii, F. Gelis and R. Venugopalan, Phys. Rev. Lett. to appear [hep-ph/0504047].
11. E. Iancu, K. Itakura, L.D. McLerran, Nucl. Phys. **A 724**, 181 (2003).
12. D. Kharzeev and K. Tuchin, Nucl. Phys. **A 735**, 248 (2004).
13. H. Fujii, F. Gelis and R. Venugopalan, in preparation.