

# Correlation Signatures of a Second Order QCD Phase Transition

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**Introduction:**

3 milestones in Au+Au collisions at RHIC

**Critical opalescence:**

Experimental observation of a 2nd order phase transition

**Hard correlations:**

Direct  $\gamma$  + hadron jet

Critical opalescence and the disappearance of the punch-through jet

**Soft correlations:**

Exact (i.e. not numerical) integrals of fluid dynamics  
non-relativistic and relativistic solutions

Lévy stable source distributions

Measuring the critical exponent of the correlation function

# Lattice QCD: EoS of QCD Matter

Old idea: Quark Gluon Plasma

"Ionize" nucleons with heat

"Compress" them with density

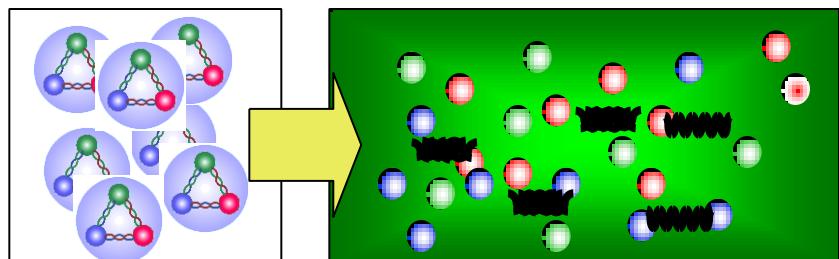
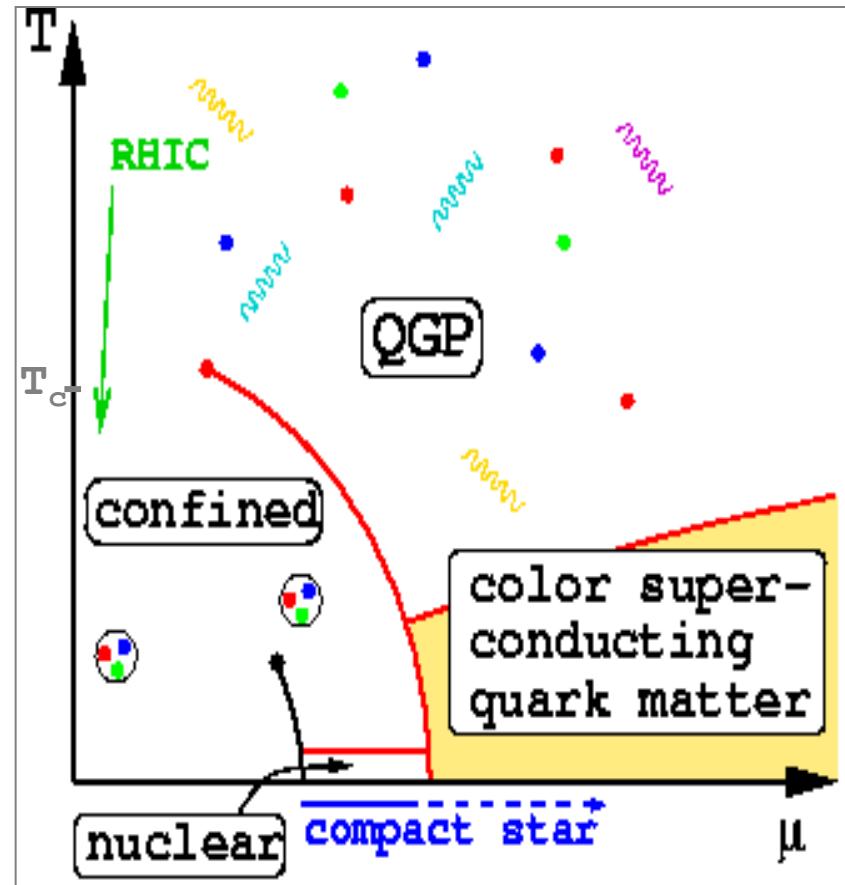
New state(s?) of matter



Z. Fodor and S.D. Katz:  
critical end point of 1st order phase tr  
even at finite baryon density,  
cross over like transition.

(hep-lat/0106002, hep-lat/0402006)

$T_c = 176 \pm 3$  MeV ( $\sim 2$  terakelvin)  
(hep-ph/0511166)



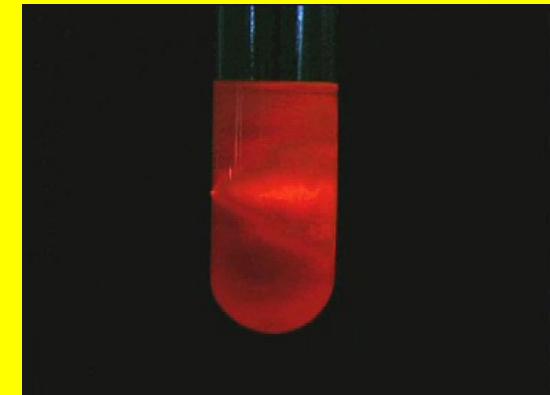
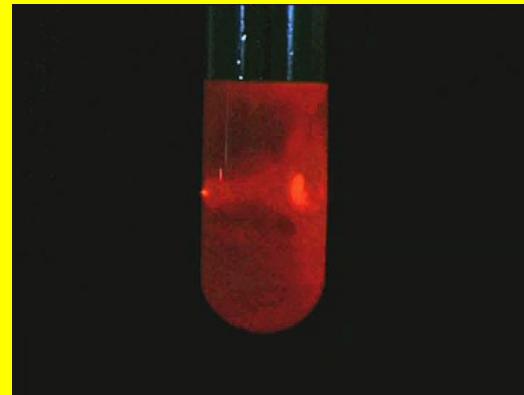
General input for hydro:  $p(\mu, T)$   
LQCD for RHIC region:  $p \sim p(T)$ ,  
 $c_s^2 = \delta p / \delta e = c_s^2(T) = 1/\kappa(T)$   
It's in the family analytic hydro solutions!

# Critical Opalescence

## Critical Opalescence: a laboratory method to observe a 2nd order PT

correlation length diverges, clusters on all scales appear incl. the wavelength of the penetrating (laser) probe

side view:



<http://www.msm.cam.ac.uk/doitpoms/tiplib/solidssolutions/videos/laser1.mov>

front view:

matter becomes opaque at the critical point (CP)



$T \gg T_c$

$T \geq \sim T_c$

$T = T_c$

# Critical Opalescence



**Suggests: the matter is most opaque at the critical point! (click on video)**  
**observation of a penetrating probe with fixed trigger**  
**(e.g. a trigger particle with high  $p_t > 5 \text{ GeV}$ )**  
**look for the broadening and disappearance of the punch-through jet**  
**as a function of  $\sqrt{s_{NN}}$ : max effect corresponds to hitting  $T_c$  (CP)**

# Critical point: punch-through is hardest

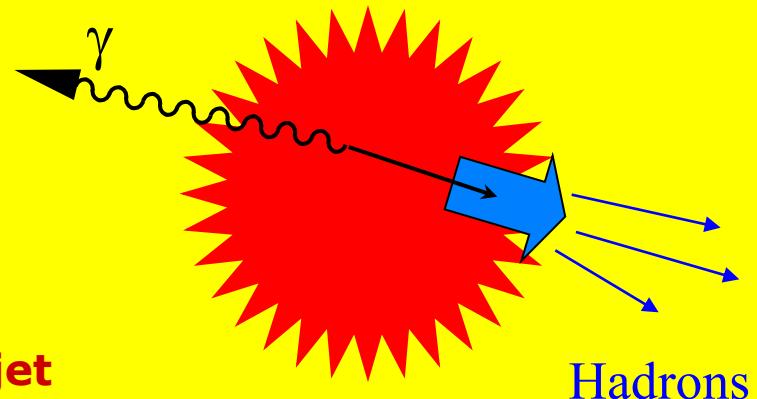
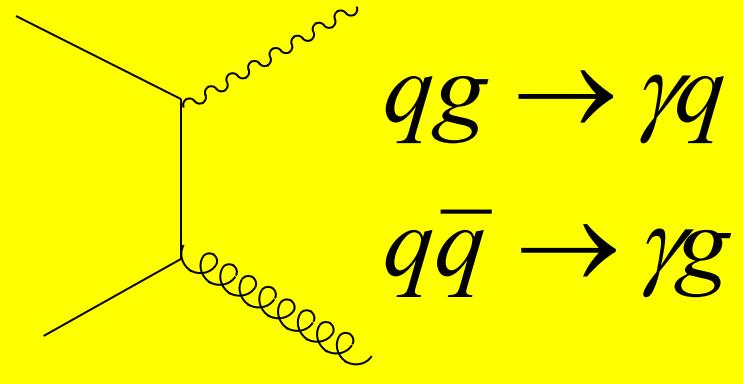
Direct  $\gamma$ -hadron jet correlations

$\gamma$ : yields the energy of the jet  
penetrates matter

hadron jet: punches through  $T > T_c$   
punches through  $T < T_c$   
disappears near  $T_c$

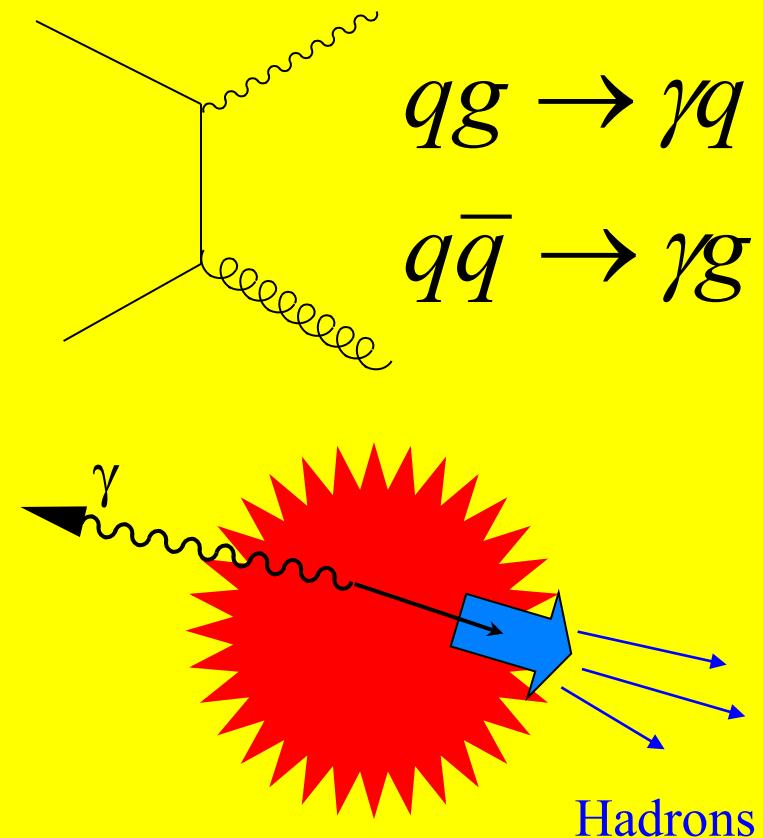
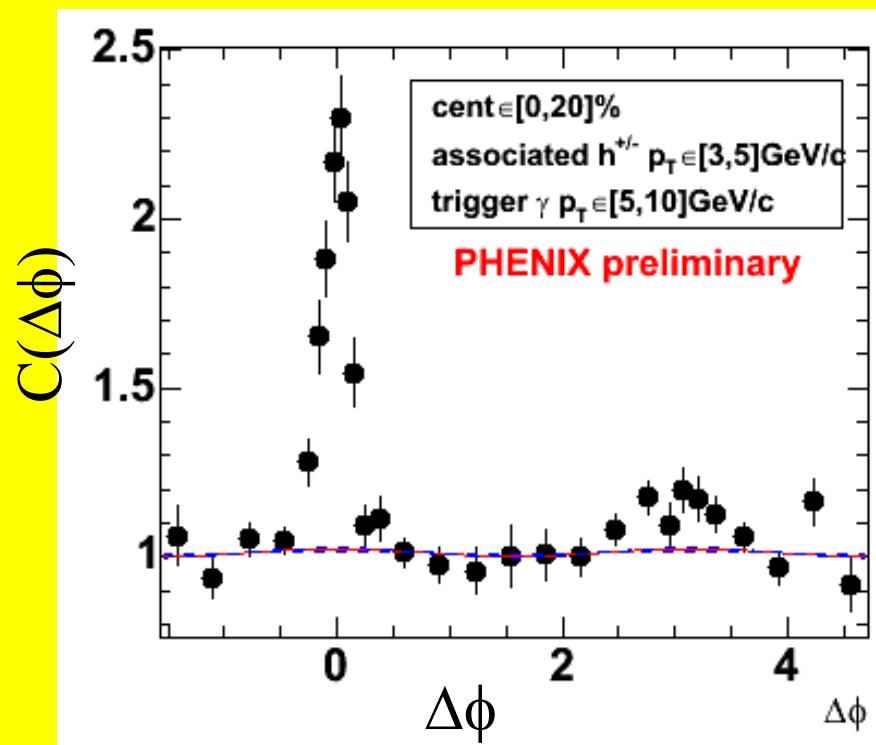
running down RHIC provides a  
unique  
opportunity to measure

( $\gamma$ , jet) correlation functions  
disappearance of the punch-through jet  
at the onset of the second order phase transition:  
signal of critical opalescence.  
(Minimum of  $R_{AA}$  is reached)



# PHENIX preliminary: $\gamma$ +jet correlations

Direct  $\gamma$ -hadron jet correlations  
valuable tool to pin down the  
critical point of QCD!



Comparison with  $\pi^0$  triggered data necessary to extract direct photon correlations. (N. Grau for the PHENIX Collaboration, WWND 2006, San Diego)

# Soft two-particle correlations

Single particle spectrum:  
averages over space-time information

$$E \frac{dN}{dp} = \int dx^4 S(x, p)$$

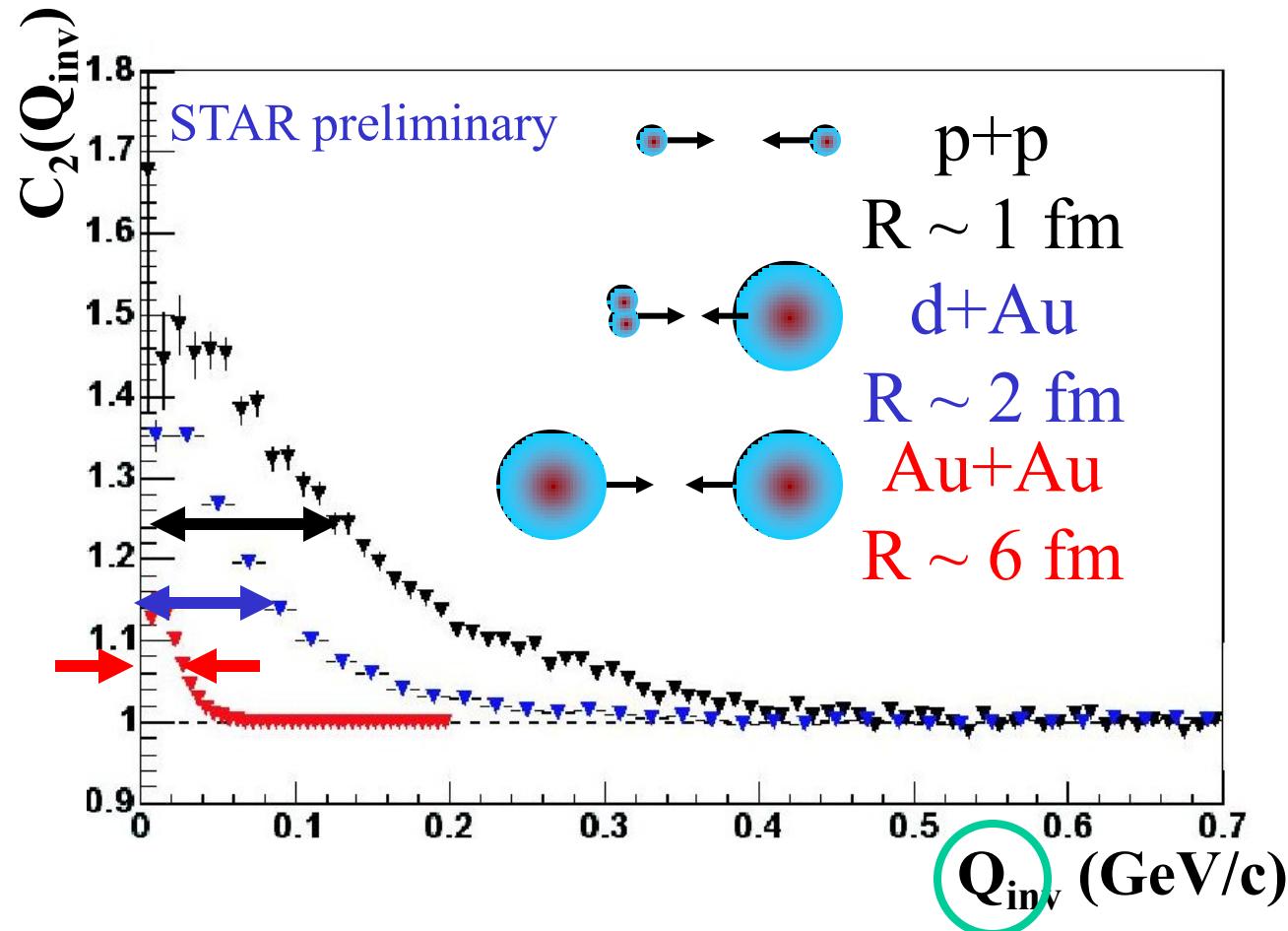
Correlations:  
sensitivity to space-time information

$$C_2(\mathbf{q}) = \frac{dN_2 / d\mathbf{p}_1 d\mathbf{p}_2}{(dN_1 / d\mathbf{p}_1)(dN_1 / d\mathbf{p}_2)} \approx \int d\mathbf{r} |\Phi(\mathbf{r}, \mathbf{q})|^2 S(\mathbf{r}, \mathbf{q})$$

**FSI**      **Source function**

Intensity interferometry, HBT technique, femtoscopy ....

# Correlation functions for various collisions



Correlations have more information (3d shape analysis)  
Use advanced techniques & extract it (S. Panitkin, Moriond'05)

# Search for a 1st order QCD phase transition

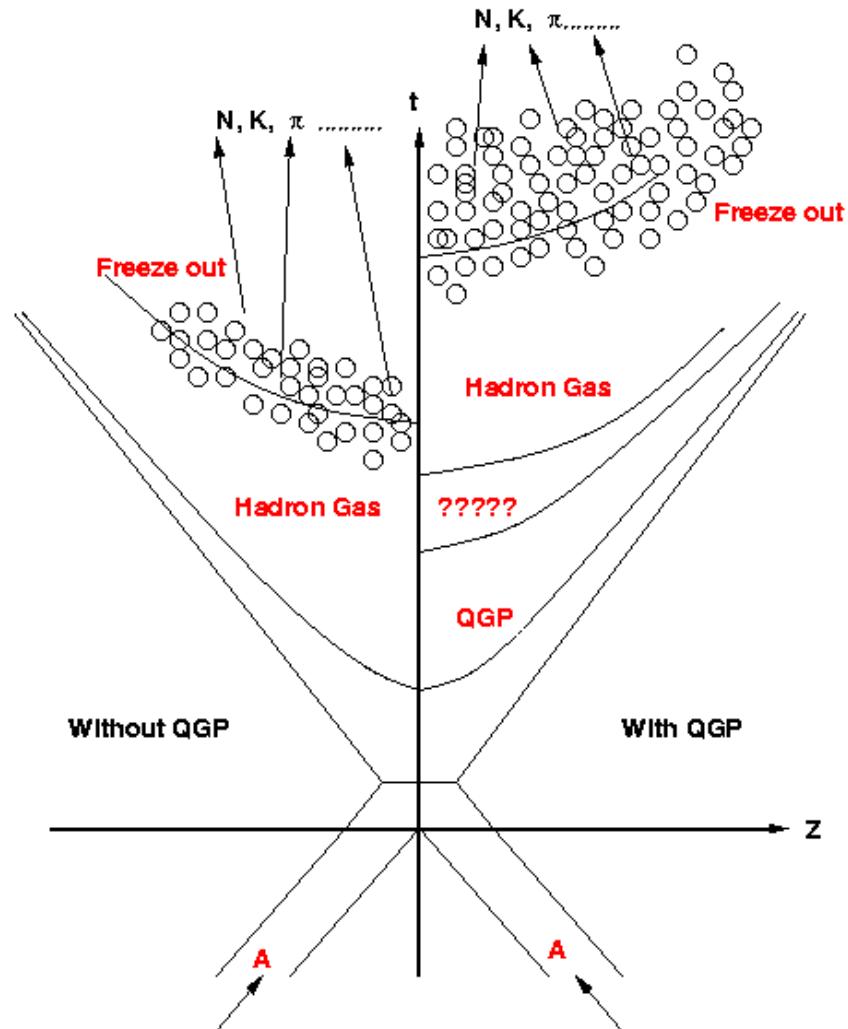
**QGP has more degrees of freedom than pion gas**

**Entropy should be conserved during fireball evolution**

**Hence:  
Look in *hadronic* phase for signs of:**

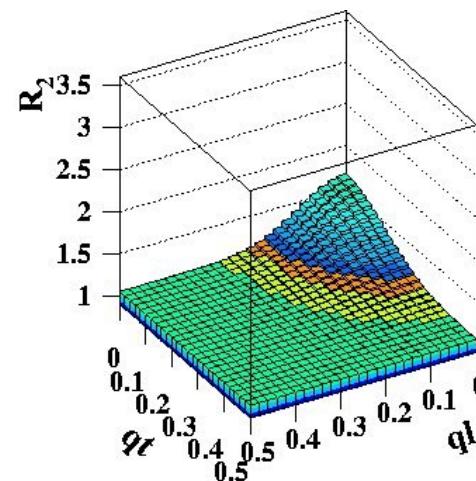
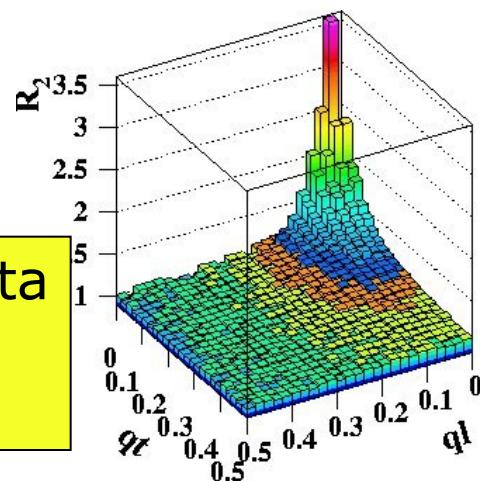
**Large size,  
Large lifetime,  
Softest point of EOS**

**signals of a 1st order (!) phase trans.**

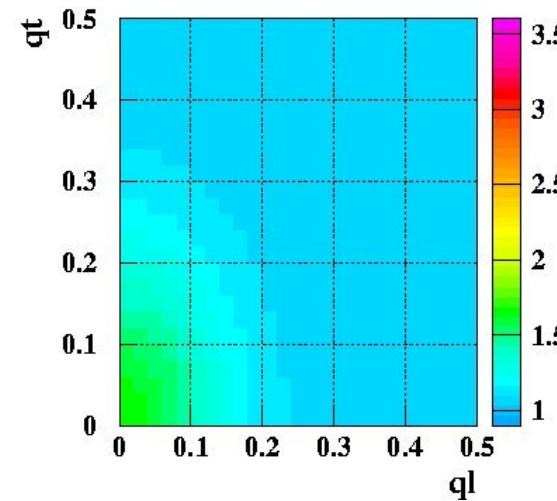
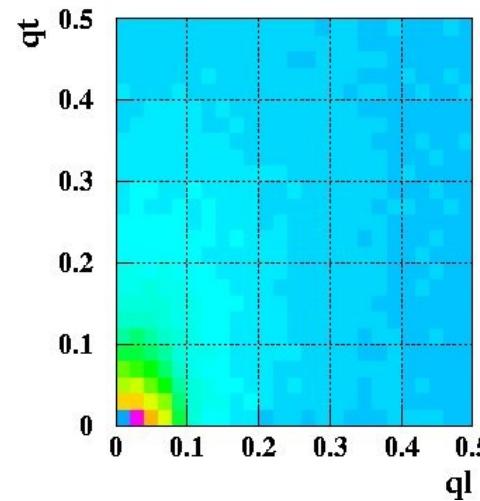


# Non-Gaussian structures, 2d, UA1 data

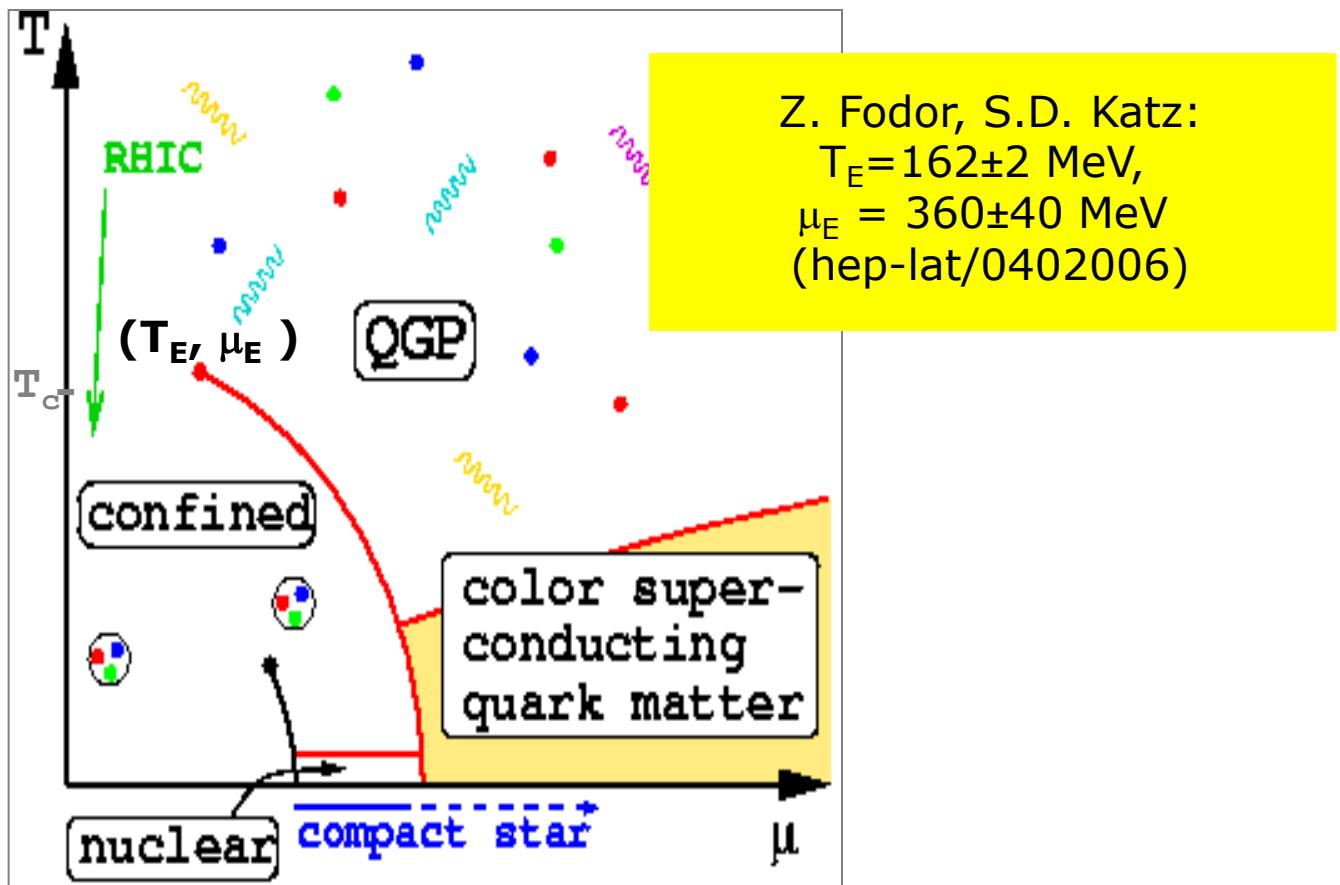
UA1 ( $p + \bar{p}$ ) data  
B. Buschbeck  
PLB (2006)



Best Gaussian  
bad shape



# Lattice QCD: EoS of QCD Matter



**At the Critical End Point, the phase transition is of 2nd order.**

Stepanov, Rajagopal, Shuryak:

Universality class of QCD  $\rightarrow$  3d Ising model PRL 81 (1998) 4816

# Critical phenomena

Order parameter of QCD - quark condensate:

$$c = \langle \bar{q} q \rangle$$

Correlation function of quark condensate:

$$\rho(R) = \langle c(r+R)c(r) \rangle - \langle c \rangle^2$$

measures spatial correlations of pions,  
it decreases for large distances as:

$$\rho(R) \propto R^{-(d-2+\eta)}$$

d: dimension = 3

critical exponent of the correlation function

$$\eta$$

For the d=3 Ising model (QCD @ CEP):  $\eta(3\text{d Ising}) = 0.50 \pm 0.05$   
(Rieger, Phys. Rev. B52 (1995) 6659)

# Scale invariant (Lévy) sources

Fluctuations appear on many scales,  
final position is a sum of many random shifts:

$$x = \sum_{i=1}^n x_i, \quad f(x) = \int \prod_{i=1}^n dx_i \prod_{j=1}^n f_j(x_j) \delta(x - \sum_{k=1}^n x_k).$$

correlation function measures a Fourier-transform,  
that of an n-fold convolution:

$$\tilde{f}(q) = \int dx \exp(iqx) f(x),$$

$$\tilde{f}(q) = \prod_{i=1}^n \tilde{f}_i(q),$$

Lévy: generalized central limit theorems

adding one more step in the convolution does not change the shape

$$\begin{aligned} \tilde{f}_i(q) &= \exp(iq\delta_i - |\gamma_i q|^\alpha), & \prod_{i=1}^n \tilde{f}_i(q) &= \exp(iq\delta - |\gamma q|^\alpha) \\ \gamma^\alpha &= \sum_{i=1}^n \gamma_i^\alpha, & \delta &= \sum_{i=1}^n \delta_i. \end{aligned}$$

# Correlation functions for Lévy sources

Correlation funct of stable sources:

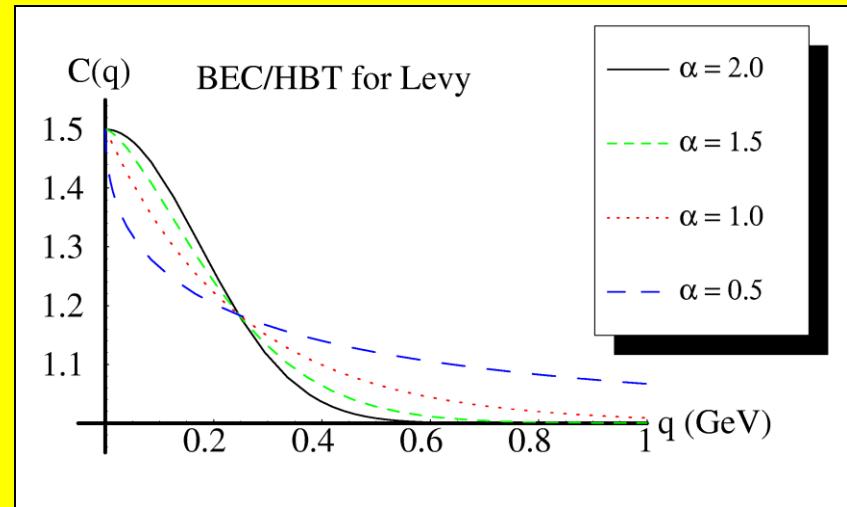
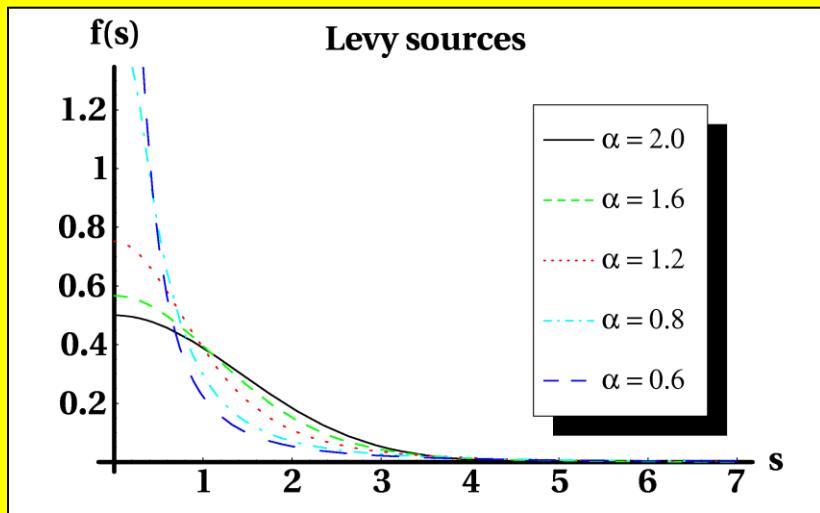
$$C(q; \alpha) = 1 + \lambda \exp(-|qR|^\alpha)$$

R: scale parameter

$\alpha$ : shape parameter or Lévy index of stability

$\alpha = 2$  Gaussian,  $\alpha = 1$  Lorentzian sources

Further details: T. Cs, S. Hegyi and W. A. Zajc, EPJ C36 (2004) 67



# Correlation signal of the CEP

If the source distribution at CEP is a Lévy, it decays as:

$$\rho(R) \propto R^{-(1+\alpha)}$$

at CEP, the tail decreases as:

$$\rho(R) \propto R^{-(d-2+\eta)}$$

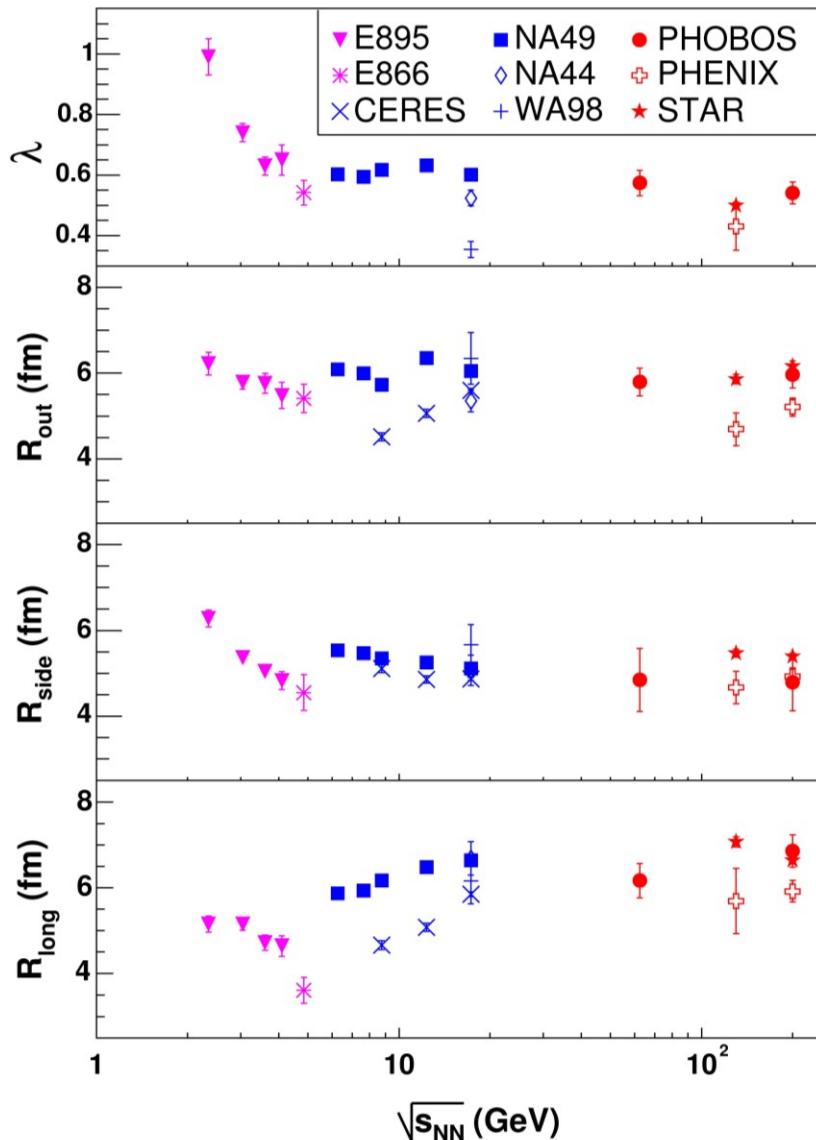
hence:

& excitation of  $\alpha$  as a function of  $\tau = |T - T_c| / T_c$

$$\alpha(\text{Lévy}) = \eta(3\text{d Ising}) = 0.50 \pm 0.05$$

T. Cs, S. Hegyi, T. Novák, W.A.Zajc,  
Acta Phys. Pol. B36 (2005) 329-337

# Excitation of 3d Gaussian fit parameters



These data exclude:

1st order phase trans.  
(assumed in many hydro codes)

For a second order PT:

excitation function of  
non-Gaussian parameter  $\alpha$

New analysis /  
new data are needed

# Correlation signal, VARIOUS Quark Matters

Transition to hadron gas may be:

- (strong) 1st order
- second order (Critical Point, CP)
- cross-over
- from a supercooled state (scQGP)

Type of phase transition:

Strong 1st order QCD phase transition:

(Pratt, Bertsch, Rischke, Gyulassy)

Second order QCD phase transition:

(T. Cs, S. Hegyi, T. Novák, W.A. Zajc)

Cross-over quark matter-hadron gas transition:

(lattice QCD, Buda-Lund hydro fits)

Supercooled QGP (scQGP) -> hadrons:

(T. Cs, L.P. Csernai)

its correlation signature:

$R_{\text{out}} >> R_{\text{side}}$

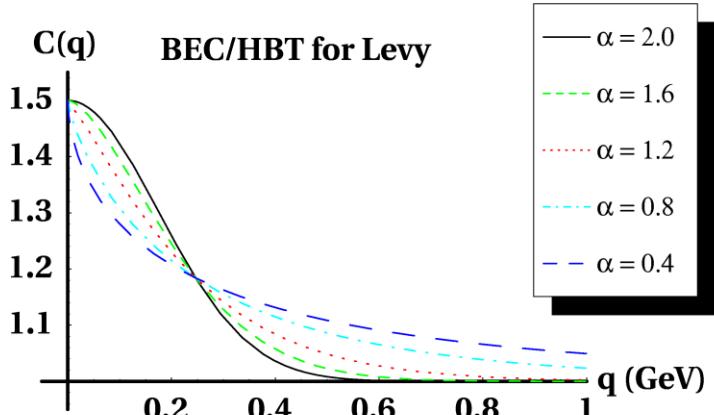
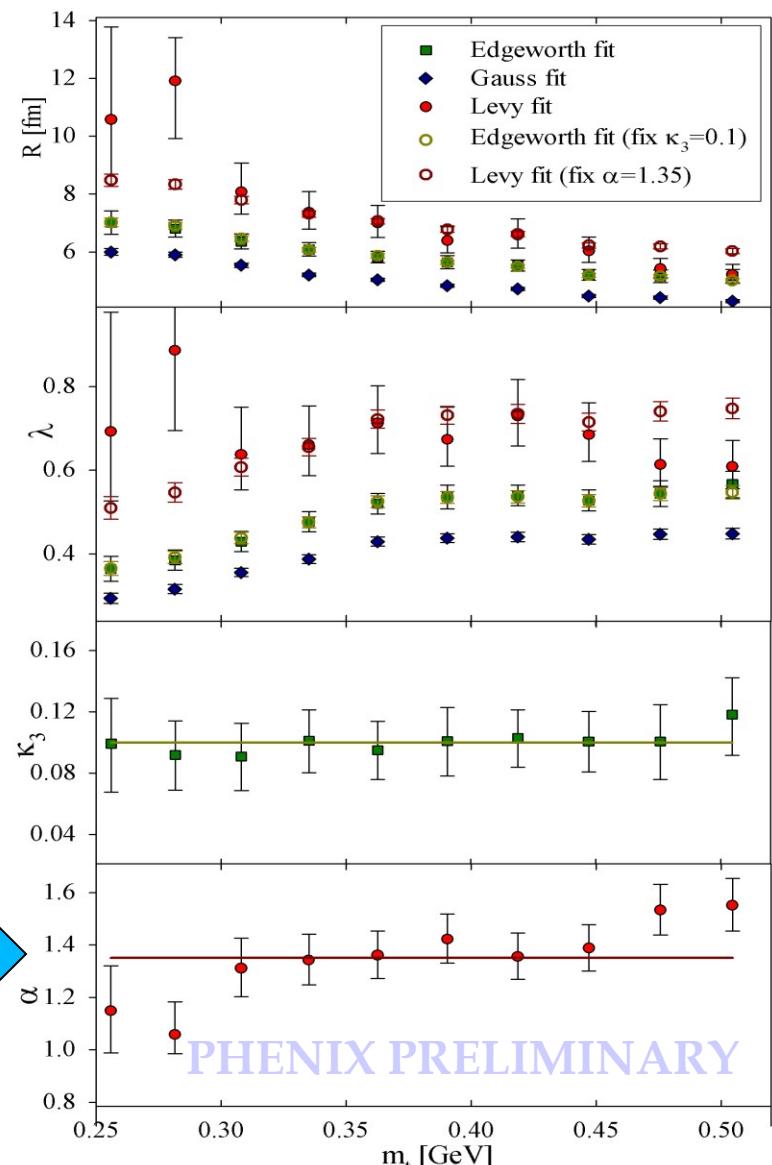
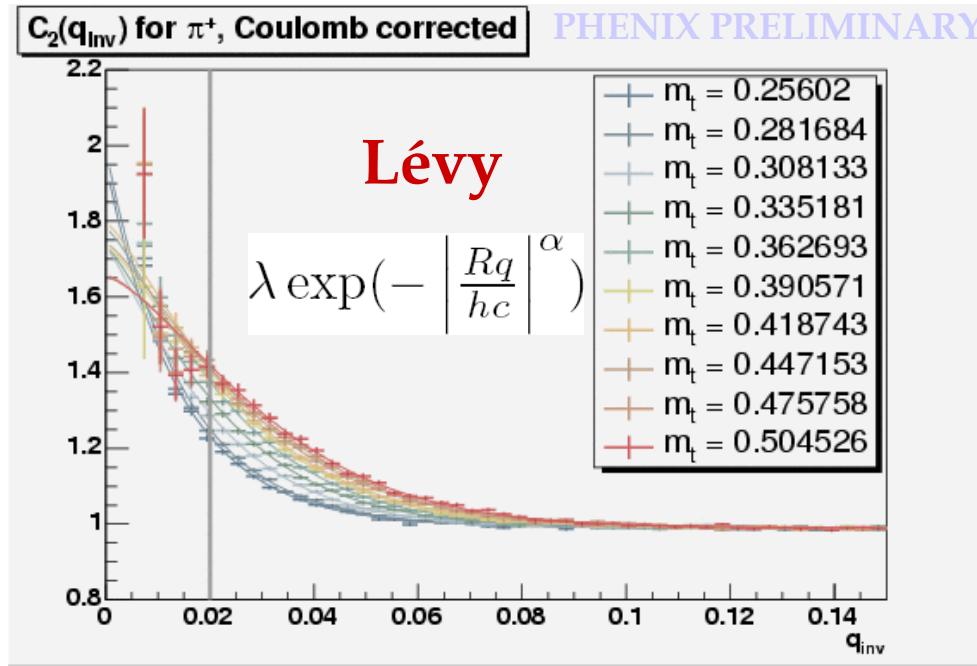
non-Gaussian shape  
 $\alpha(\text{Lévy})$  decreases to 0.5

hadrons appear from  
a region with  $T > T_c$

pion flash ( $R_{\text{out}} \sim R_{\text{side}}$ )  
same freeze-out for all  
strangeness enhancement  
no mass-shift of  $\phi$

scQGP predicted in hep-ph/9406365 -  
not inconsistent with RHIC Au+Au data in 2006 (!)

# Lévy fits to prelim. Au+Au @ QM 2005



# Summary

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**High transverse momentum  $\gamma$  + jet correlations:  
maximal opalescence  
promising signal for the critical end point**

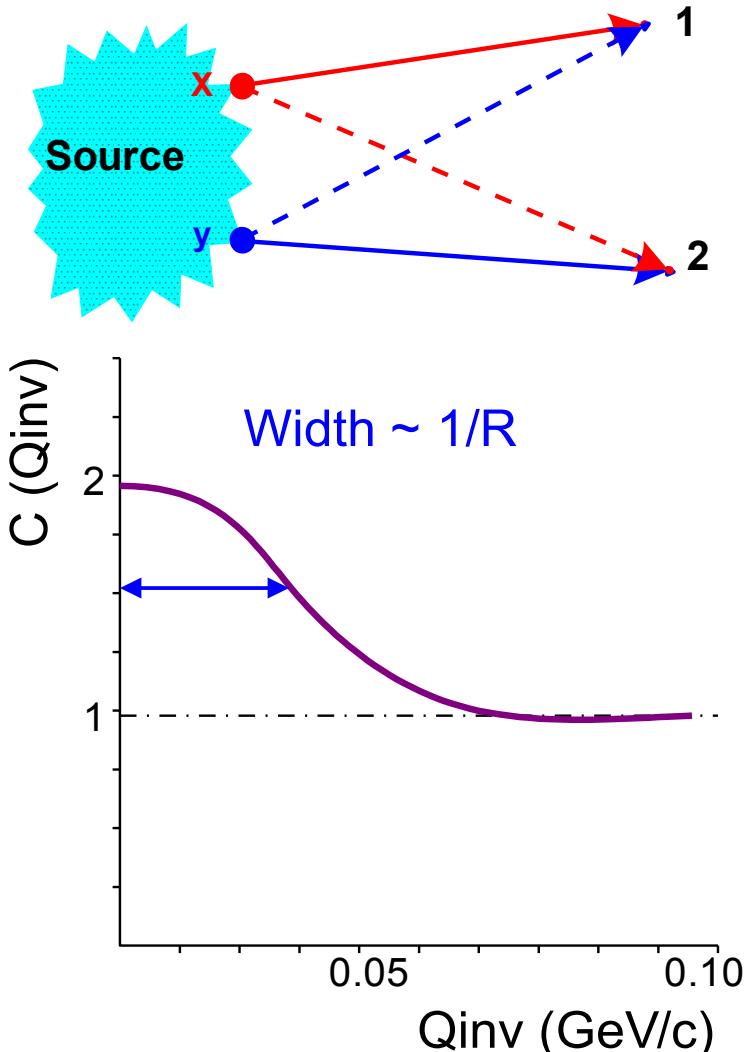
**Soft Bose-Einstein correlations:**  
**measure the excitation function of a  
non-Gaussian parameter: Lévy index of stability,  $\alpha$   
 $\alpha = \eta$  : critical exponent of the correlation function**

**Universality class argument:**  
 **$\alpha$  decreases from 2 (or 1.4) to 0.5 at the critical point  
signals the 2nd order phase transition**

# Backup slides

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# Two particle Interferometry for non-interacting identical bosons



$$A_{12} = \frac{1}{\sqrt{2}} [e^{ip_1 \cdot (r_1 - \mathbf{x})} e^{ip_2 \cdot (r_2 - \mathbf{y})} + e^{ip_1 \cdot (r_1 - \mathbf{y})} e^{ip_2 \cdot (r_2 - \mathbf{x})}]$$

so that

$$\mathcal{P}_{12} = \int d^4\mathbf{x} d^4\mathbf{y} |A_{12}|^2 \rho(\mathbf{x}) \rho(\mathbf{y}) = 1 + |\tilde{\rho}(q)|^2 \equiv C_2(q)$$

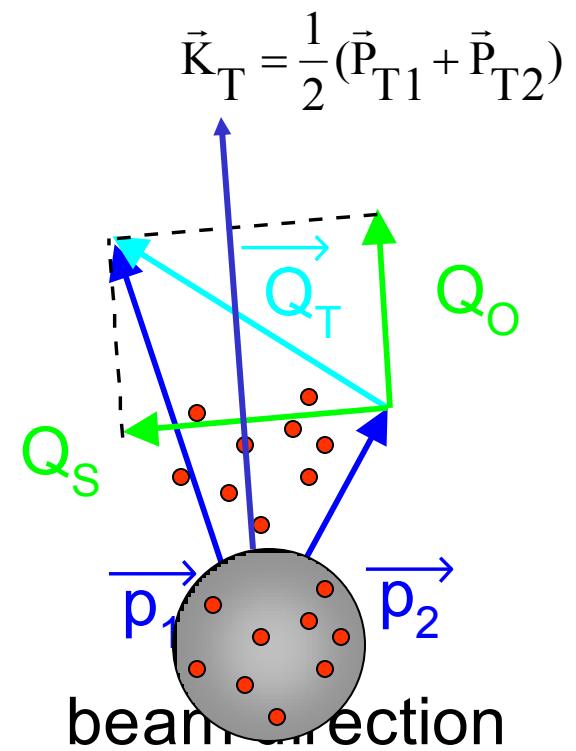
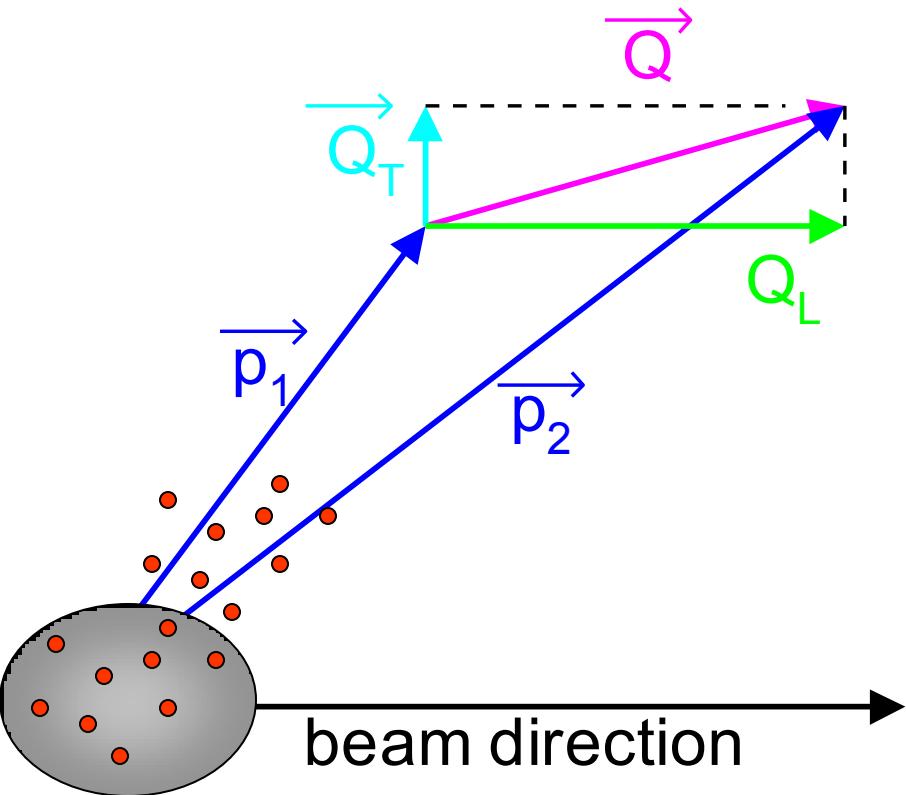
$\downarrow$   
**emission function**

$$C(p_1, p_2) = 1 + \frac{\left| \int d^4x \cdot S(x, K) \cdot e^{iq \cdot x} \right|^2}{\left| \int d^4x \cdot S(x, K) \right|^2}$$

$$q = p_1 - p_2 \quad K = \frac{1}{2}(p_1 + p_2)$$

# Pratt-Bertsch coordinate system

$$C(\vec{q}, \vec{k}) = 1 + \lambda(\vec{k}) e^{-q_{\text{out}}^2 R_{\text{out}}^2 - q_{\text{side}}^2 R_{\text{side}}^2 - q_{\text{long}}^2 R_{\text{long}}^2}$$

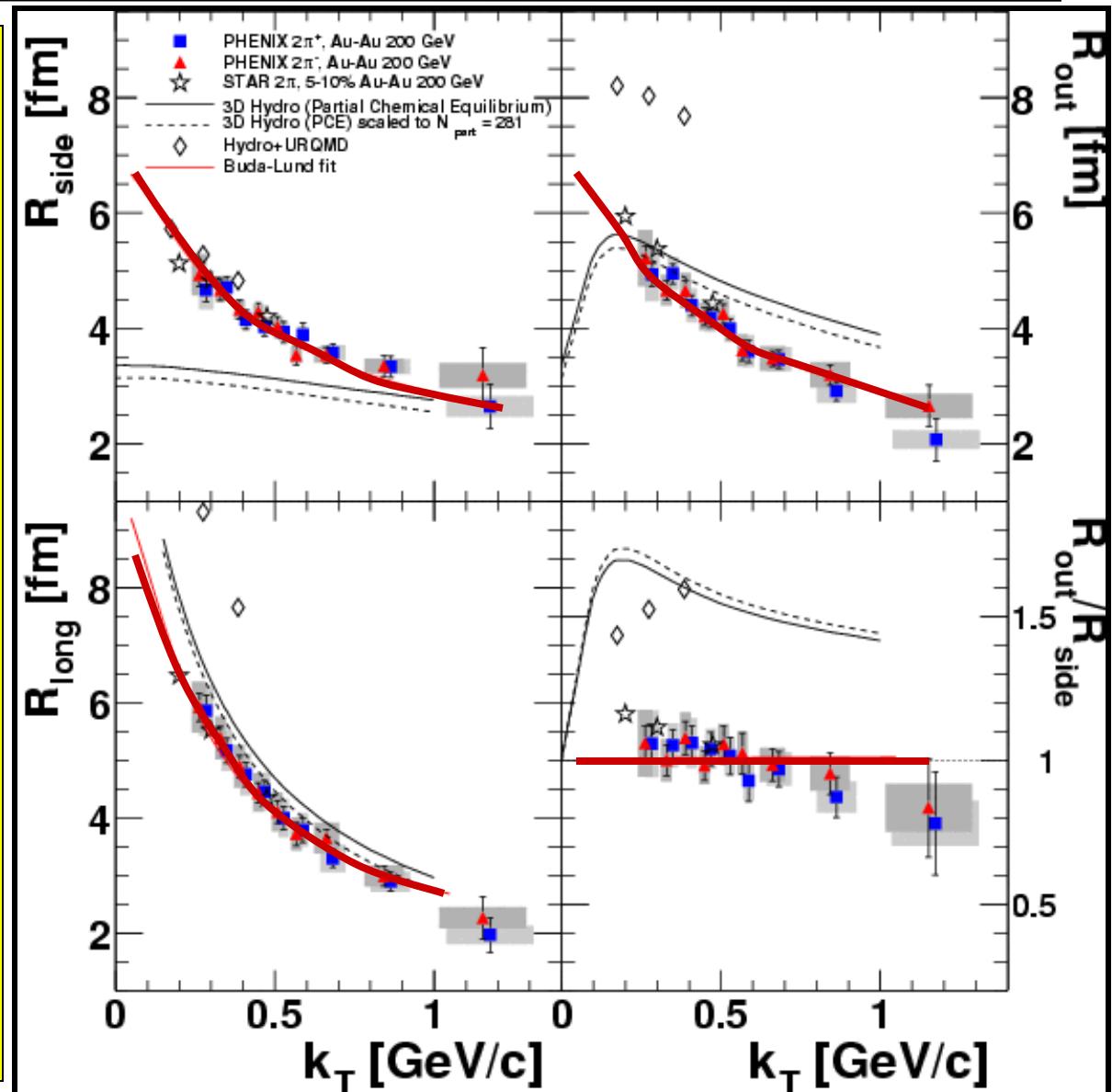


# Femtoscopy signal of sudden hadronization

Buda-Lund hydro:  
RHIC data  
follow the  
predicted  
(1994-96)  
scaling of HBT radii

T. Cs, L.P. Csernai  
hep-ph/9406365  
T. Cs, B. Lörstad  
hep-ph/9509213

Hadrons with  $T > T_c$  :  
1st order PT excluded  
hint of a cross-over  
M. Csanad, T. Cs, B.  
Lorstad and A. Ster,  
nucl-th/0403074



# But are the correlation data Gaussian?

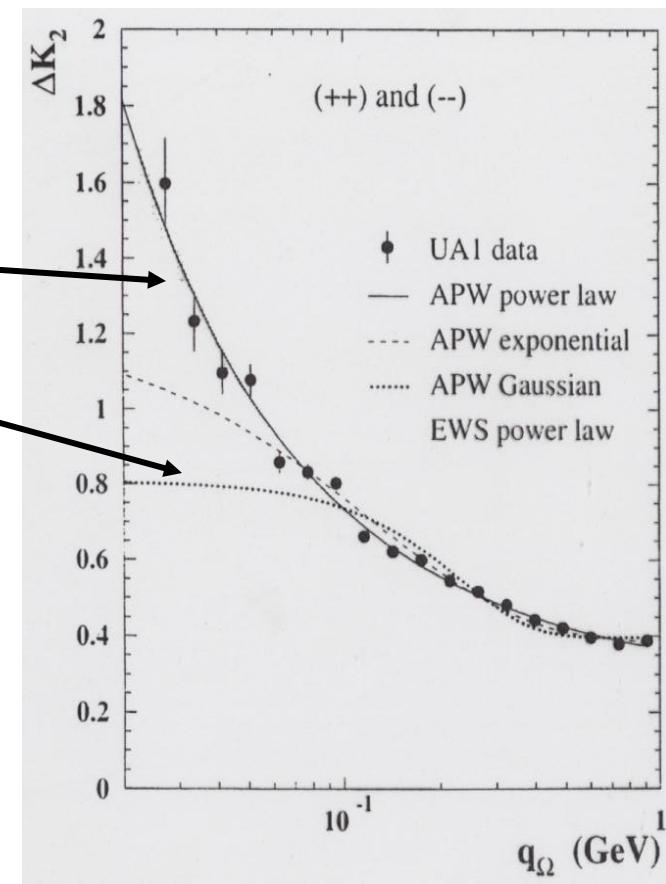
**1 dimensional correlations:**  
typically more peaked  
than a Gaussian

if a Gaussian fit  
does not describe the data

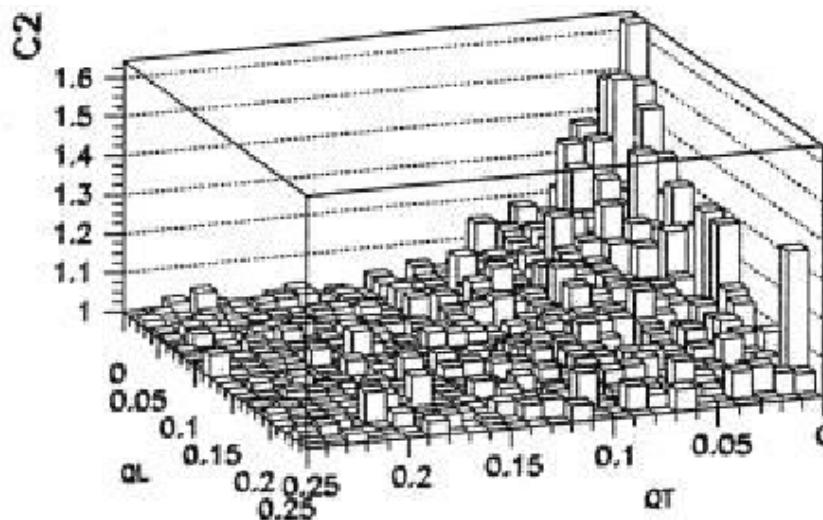
then have the parameters  
any meaning?

**Example:**  
like sign correlation data  
of the UA1 collaboration

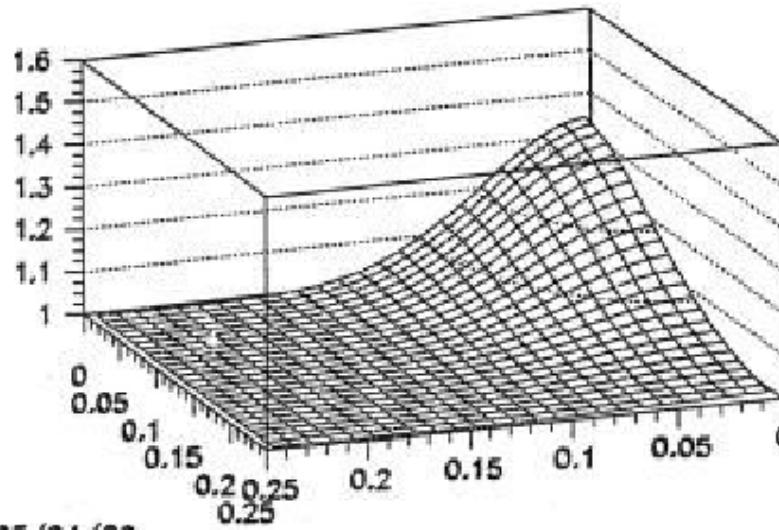
**p + pbar @  $E_{cms} = 630$  GeV**



# Non-Gaussians, 2d E802 Si+Au data



E802 Si+Au data,  
 $\sqrt{s_{NN}} = 5.4 \text{ GeV}$



Best Gaussian:  
bad shape

93/04/29