

Few-Body systems

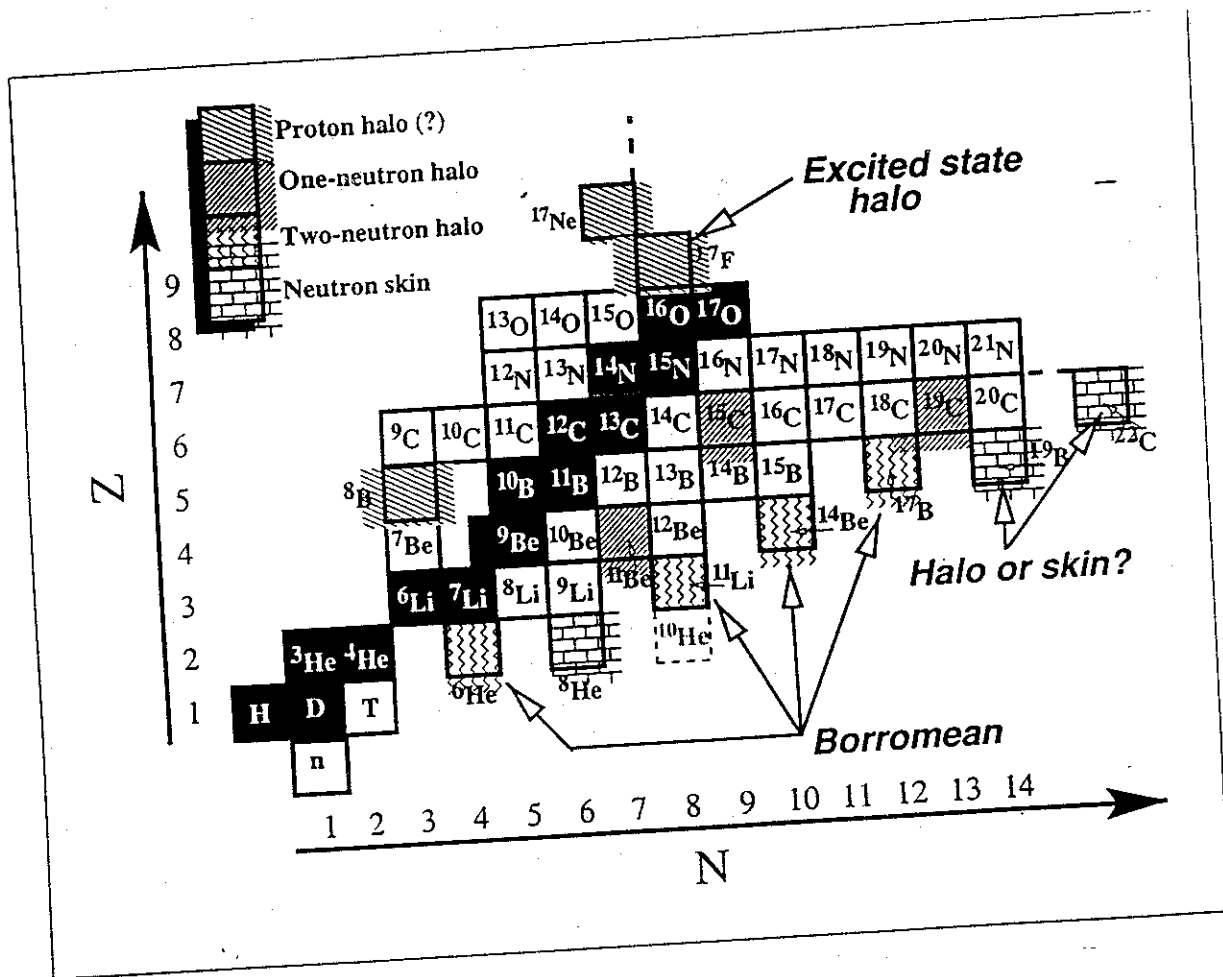
nuclear systems

atomic-molecular systems

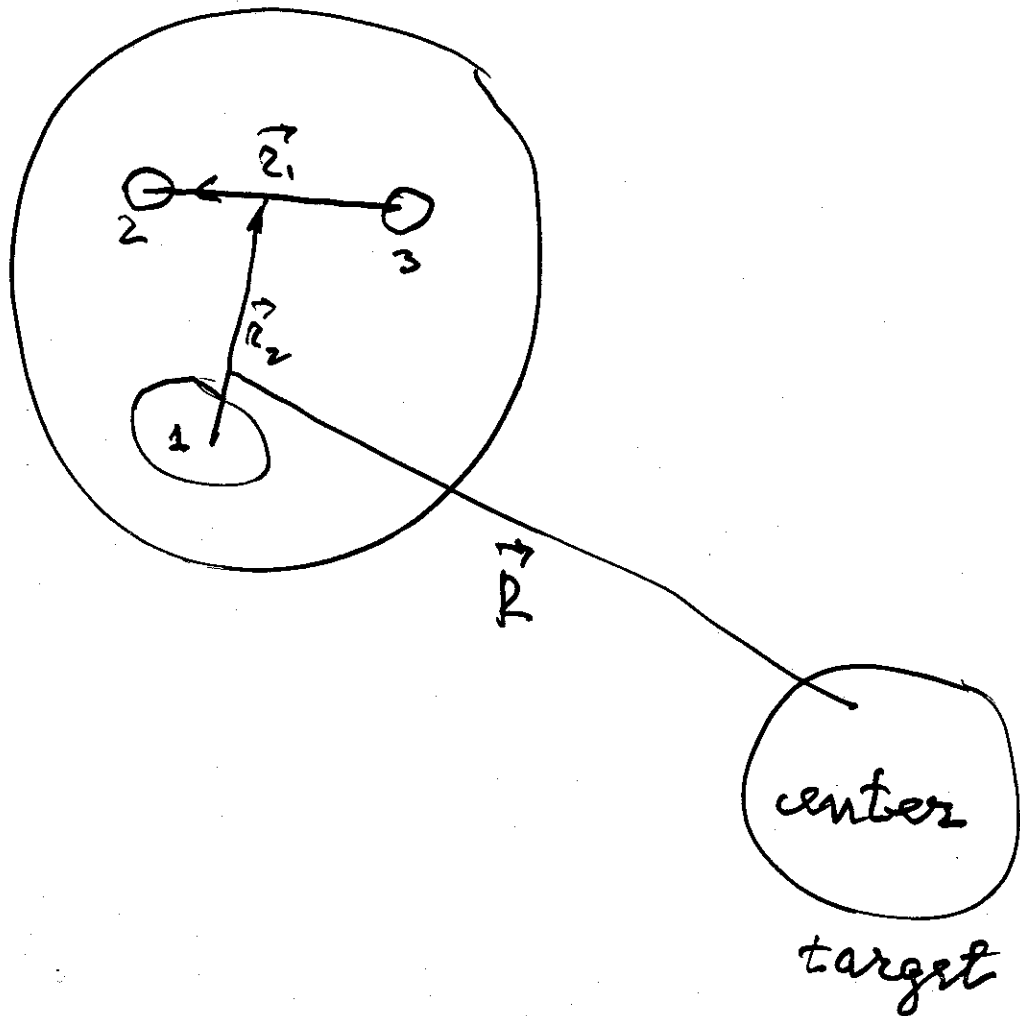
"halo"-nuclei

atomcules: $Z + e^-(ze) + \bar{p}$

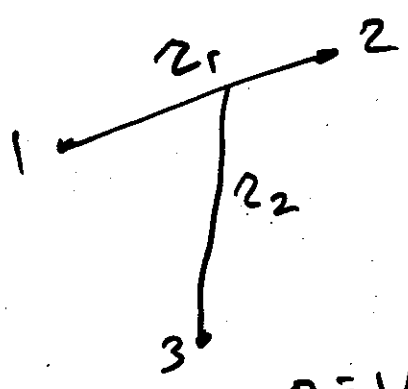
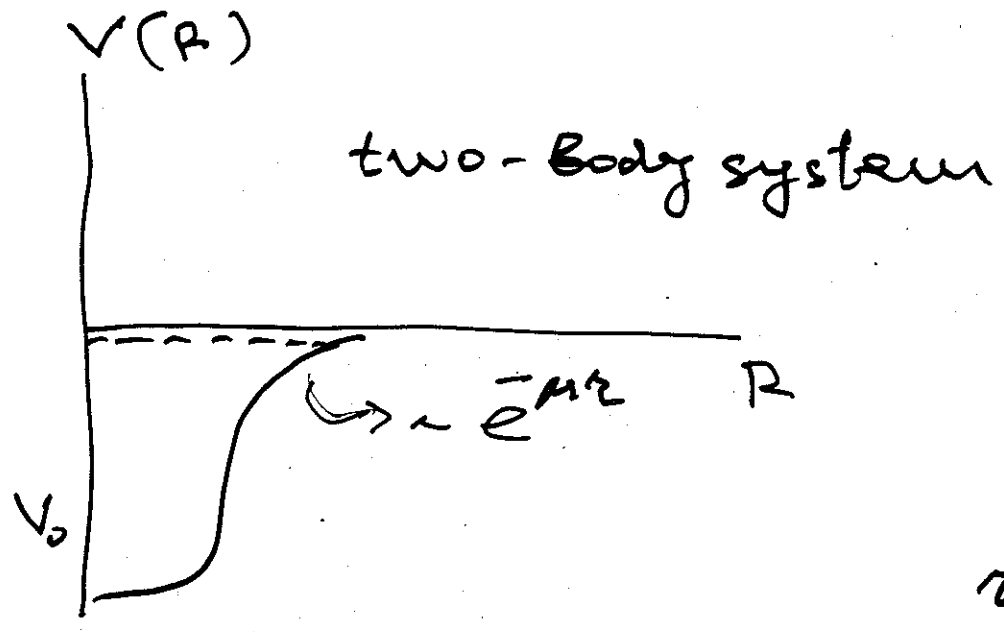
halo-hypernuclei: $A + 2N(p) + \Lambda(\Sigma)$



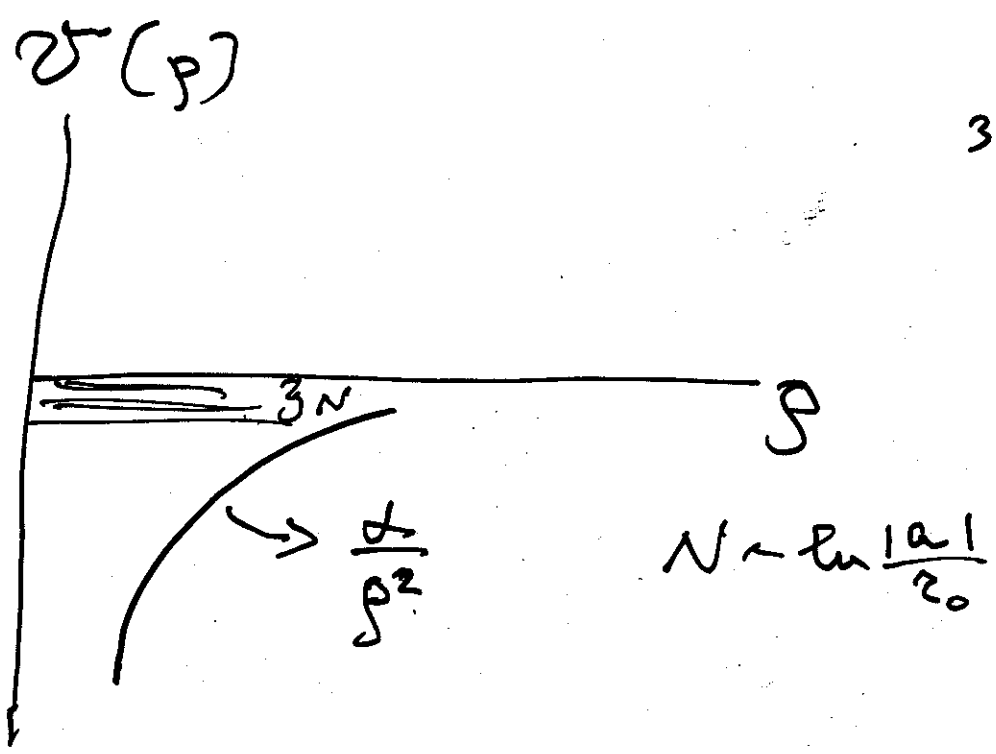
3-body projectile (cluster)



Efimov systems.



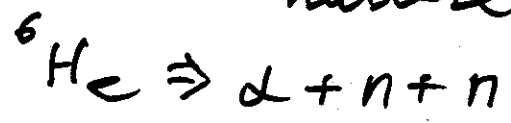
$$\rho = \sqrt{r_1^2 + r_2^2}$$



Peculiarities of halo-systems

1. Short range interaction and long tail in W. f.: $\bar{r} \sim 5-6 \text{ fm}$
 $\bar{r}_d \sim 3.8 \text{ fm}$
(Probably not Efimov-type systems)

2. Weak Binding and few-Body nature:



3. Strong influence of continuum

4. Strong recoil effects in the reactions due to few-cluster structure

Physics to be extracted: exotic substructures like:

$N_1 n + N_2 p$

$N_1 n + N_2 p + \Lambda(\Sigma)$

Core

New generation of facilities:

- ISOL, SPIRAL-GANIL,
- REX-ISOLDE, ISAC-TRIUMF,
- HRIBF (Oak-Ridge)

How to study halo-nuclei?

1. Total crosssection

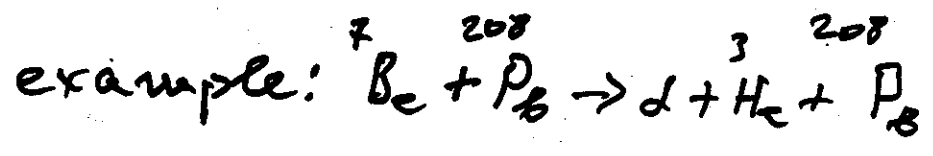
→ violation of scaling

$$\sqrt{\langle r^2 \rangle} \sim A^{1/3}$$

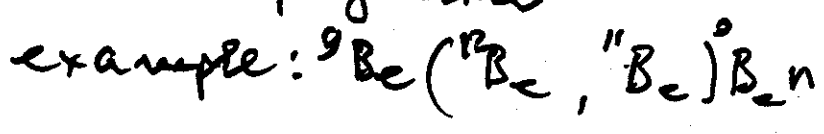
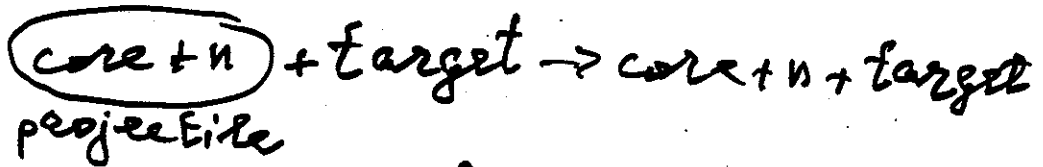
2. Elastic + inelastic scattering,

example: ${}^6\text{He} + {}^{12}\text{C}$

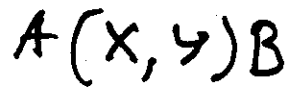
3. Breakup processes,



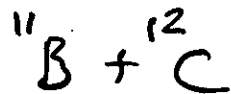
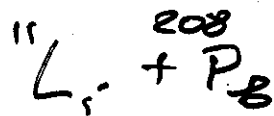
4. Knockout reactions:



5. Transfer reactions (recent history)

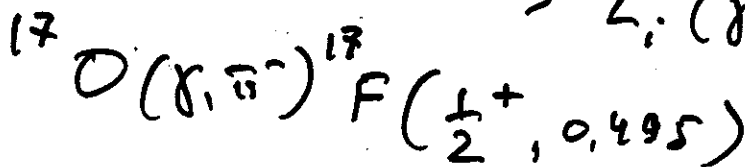
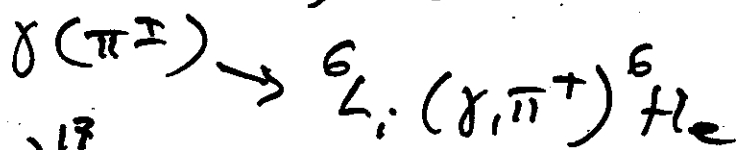
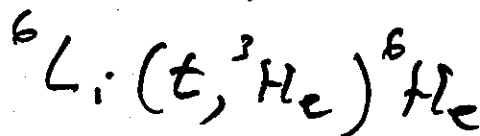
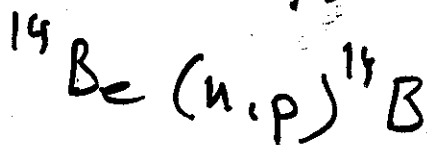


6. Fusion,



7. Charge exchange and photonuclear reactions,

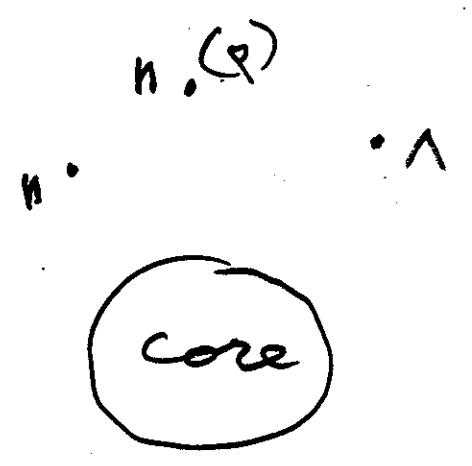
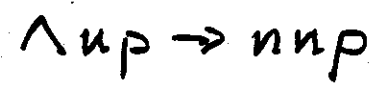
examples:



Nonmesonic decay hypernuclei
(due to transition $\Lambda N \rightarrow nN$)

$$\frac{\Gamma_n}{\Gamma_p} \equiv \frac{\Gamma(\Lambda n \rightarrow nn)}{\Gamma(\Lambda p \rightarrow np)}$$

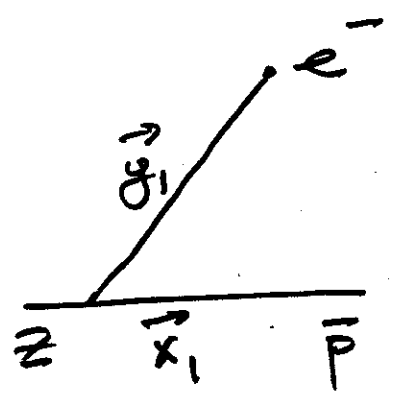
3-Body weak transitions: ^{in ${}^3\text{He}$, ${}^{13}\text{C}$}



Atomcules, peculiarity.

$$Z + e^- (2e^-) + \bar{p} \quad \text{for } Z=2, R \sim 10^{-6} \text{ sec.}$$

Coulomb-Fourier transformation



$$H = -\Delta_{\vec{x}} - \Delta_{\vec{y}} + \frac{n_1}{x_1} + \frac{n_2}{x_2} + \frac{n_3}{x_3}$$

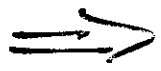
where

$$H(\vec{p}, \vec{p}') \equiv \langle \psi_{\vec{p}_1}^o \psi_{\vec{k}_1}^c | H | \psi_{\vec{p}'_1}^o \psi_{\vec{k}'_1}^c \rangle \Rightarrow$$

$$\psi_{\vec{p}_1}^o(y_1) = \frac{1}{(2\pi)^{3/2}} e^{i\vec{p}_1 \cdot \vec{y}_1}$$

$$\psi_{\vec{k}_1}^c(x_1) = \frac{1}{(2\pi)^{3/2}} e^{i\vec{k}_1 \cdot \vec{x}_1} e^{-\pi\eta_1/2} \Gamma(1+i\eta_1)$$

$\Phi(-i\eta_1, 1, i\kappa_1 \xi_1)$
 $\eta_1 = n_1 / 2\kappa_1$ - Sommerfeld parameter
 $\xi_1 = x_1 - (\vec{x}_1 \cdot \vec{\kappa}_1)$



$$(k_1^2 + p_1^2) \delta(\vec{k} - \vec{k}_1) \delta(\vec{p}_1 - \vec{p}_1') + W_2(\vec{p}_1, \vec{p}_1') + W_3(\vec{p}_1, \vec{p}_1')$$

$$W_j(\vec{p}_1, \vec{p}_1') \approx \frac{n_j}{|\vec{p}_1 - \vec{p}_1'|^2} \mathcal{L}_j(\vec{p}_1, \vec{p}_1')$$

$$\mathcal{L}_j(\vec{p}_1, \vec{p}_1') = \lim_{\lambda \rightarrow +0} \int d\vec{x}_1 e^{i\vec{E}_j \cdot \vec{x}_1 (\vec{p}_1 - \vec{p}_1') - \lambda x_1}$$

$$\psi_{\vec{k}_1}^{c*}(\vec{x}_1) \psi_{\vec{k}_1}^c(\vec{x})$$